

Lect 8: Parallelization

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**CS 2281: How to Train Your Foundation Model
Fall 2024**

Today

- Recap++:
- Pipeline Parallelism
- FSDP
- Theoretical Considerations
- Tensor Parallelism

Recap++

Today

- Recap++:



- hardware

- communication primitives

- Distributed Data Parallelism (DDP)

- Pipeline Parallelism

- FSDP

- Theoretical Considerations

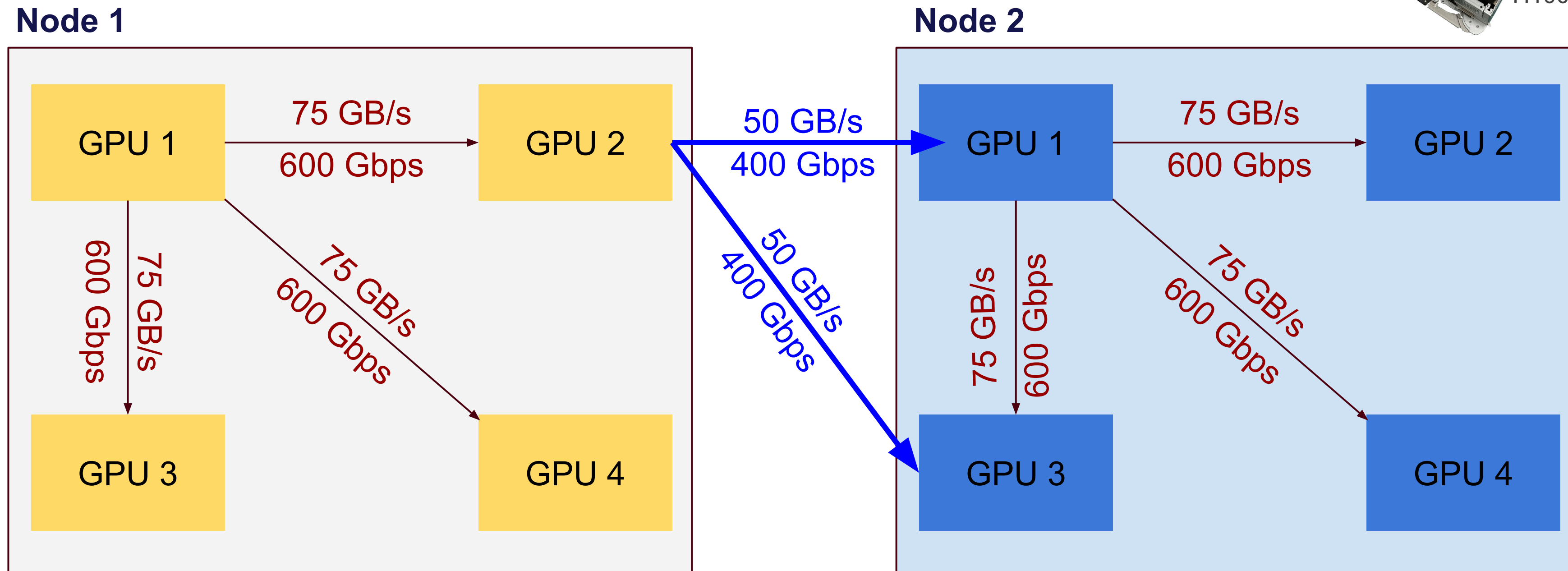
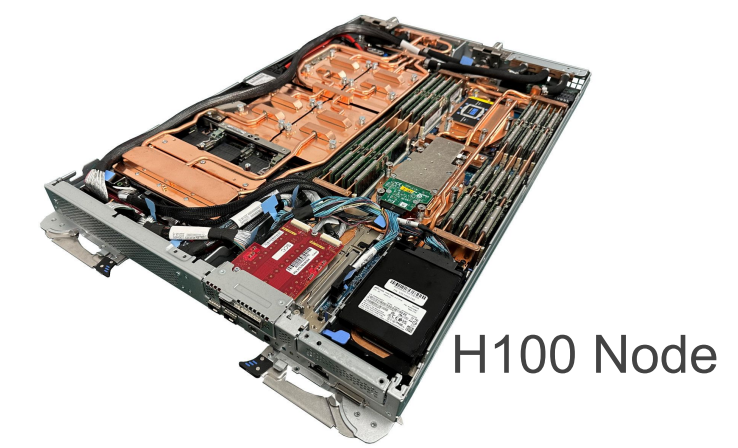
- Tensor Parallelism

Scales of Some Foundation Models

note: 1b, 8b, 70B, 405B, “big”

- A100/H100: let's say 80gb memory on each chip.
- LLMs (??):
 - GPT4.0: 1.6T (8x200B MoE model), $\approx 10T$ tokens, (flop equiv) 30K for several months
 - GPT4o: 16(or 32)x30B MoE model, $\approx 30T$ text tokens,
 - Gemini: 2T param model (also MoE?), $\approx 10T$ tokens (trained on TPUs)
 - **Llama 3.1**: 8B, 70B, 405B (dense), $\approx 10T$ tokens
- Code: Copilot $\approx 10-20B$ (?),
- Images/Video: MidJourney/Sora $\approx 10-20B$ (?), 10K gpu for 1 month (?)
- Bio: AlphaFold

GPU-to-GPU Communication



Inside Node (NVLINK): Each GPU talks to other three GPUs at 75 GB/s (single direction). This sums up to 900 GB/s all GPU-GPU bidirectional speed. $75 \text{ GB/s} * 6 * 2 = 900 \text{ GB/s}$

Outside Node (InfiniBand Network NDR): Each GPU communicates to other GPUs in another node at 400 Gbps (50 GB/s).

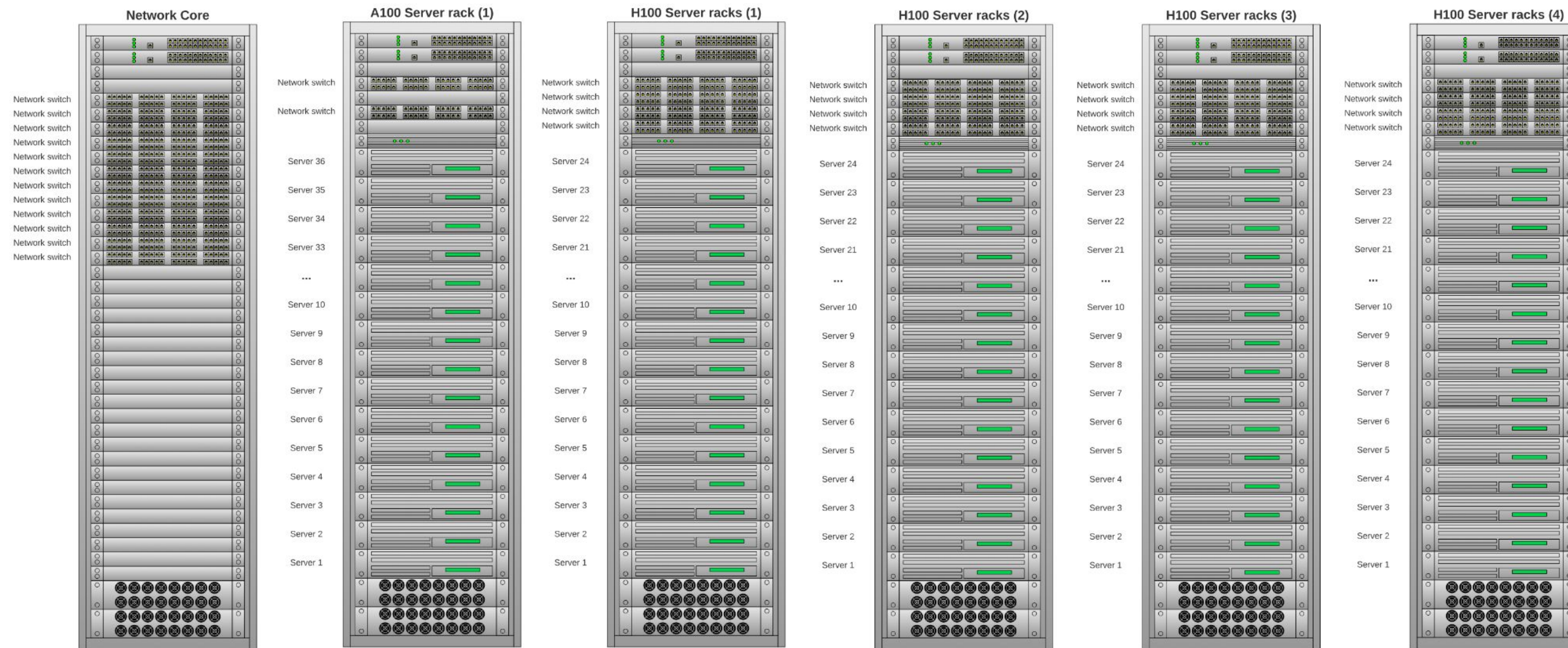
Modern nodes: usually **8 gpus per node**.

Intra node communication (**FAST**): nvlink, basically **1tb/sec (total)**

Inter node communication (**SLOW**): infiniband, **50GB/sec**

Nodes connected in a “tree” structure.

HPC Cluster



In Production (144 x A100 40 GB, 384 x H100 80 GB)

Nodes sit in racks.

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Inter node communication (**SLOW**): infiniband, **50GB/sec**

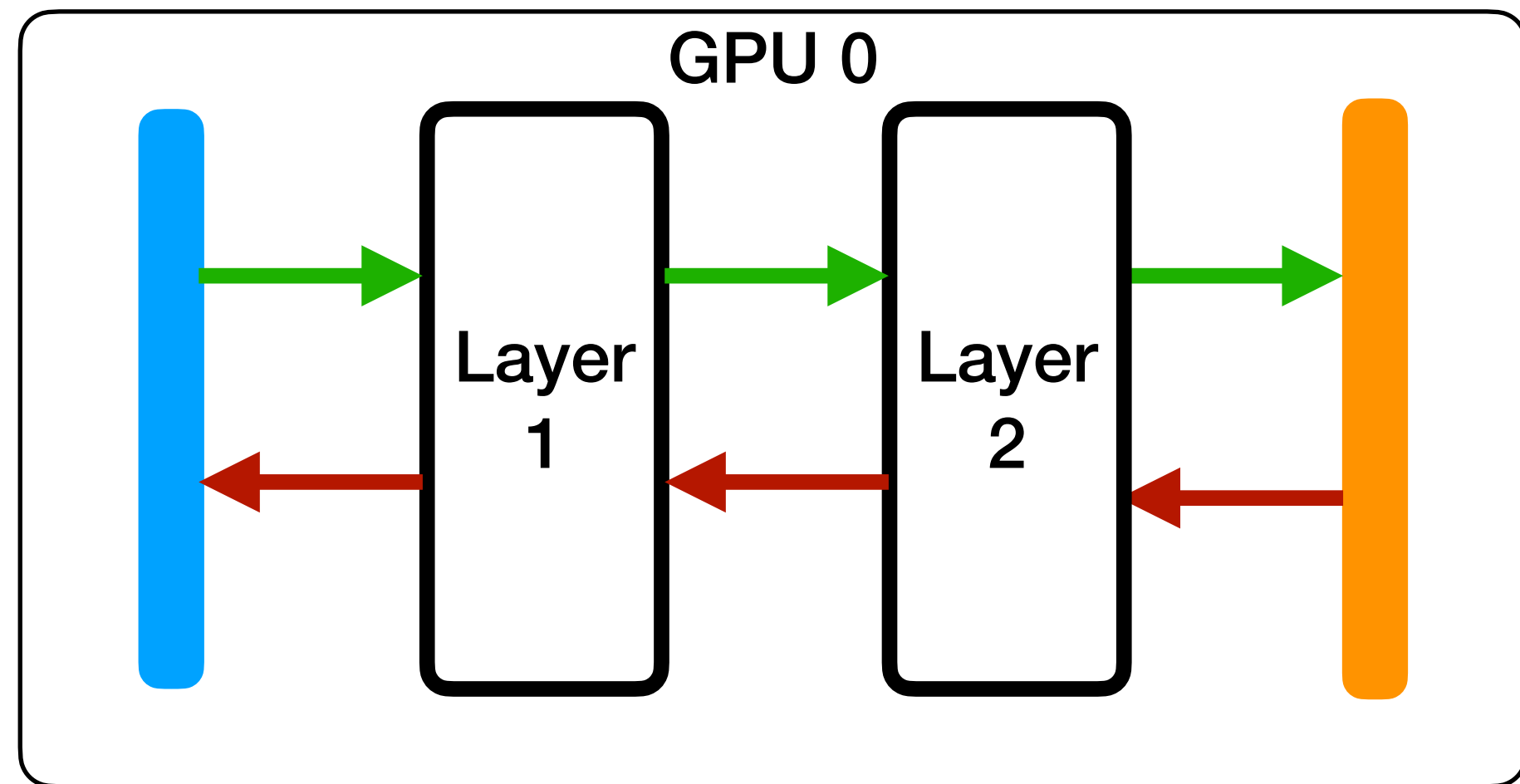
Nodes connected in a “tree” structure.

[Figure credit: Yasin Mazloumi]

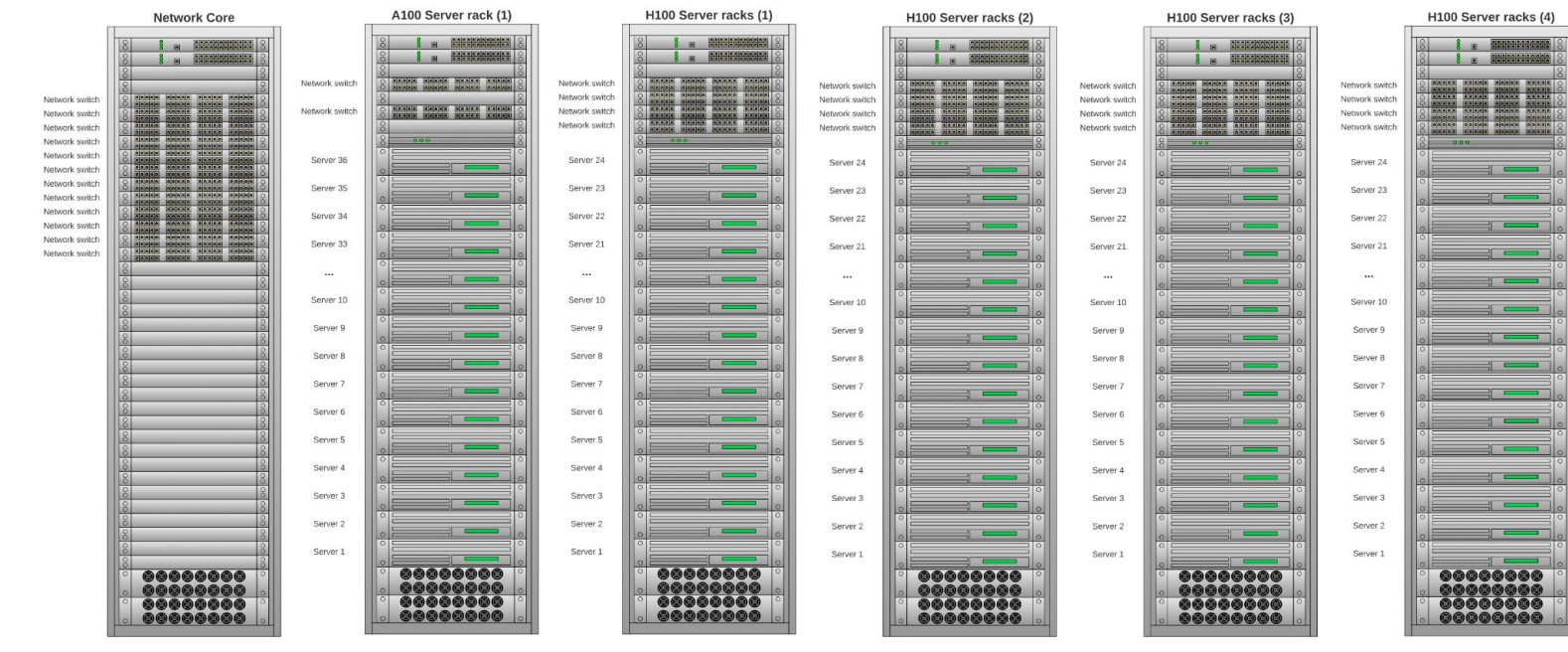


Kempner Racks

Today: Single GPU -> Distributed Training



HPC Cluster



In Production (144 x A100 40 GB, 384 x H100 80 GB)

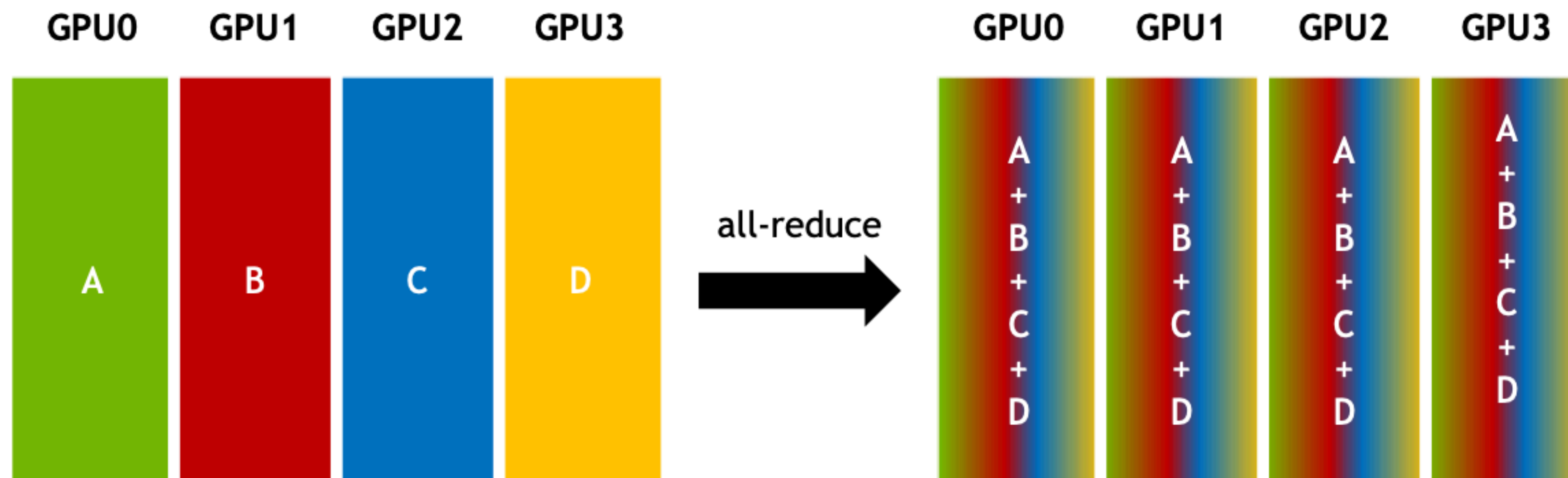
$$M_{\text{train}} = P_{\text{transformer}} + M_{\text{optimizer}} + M_{\text{activations}}$$

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NCCL communication primitives

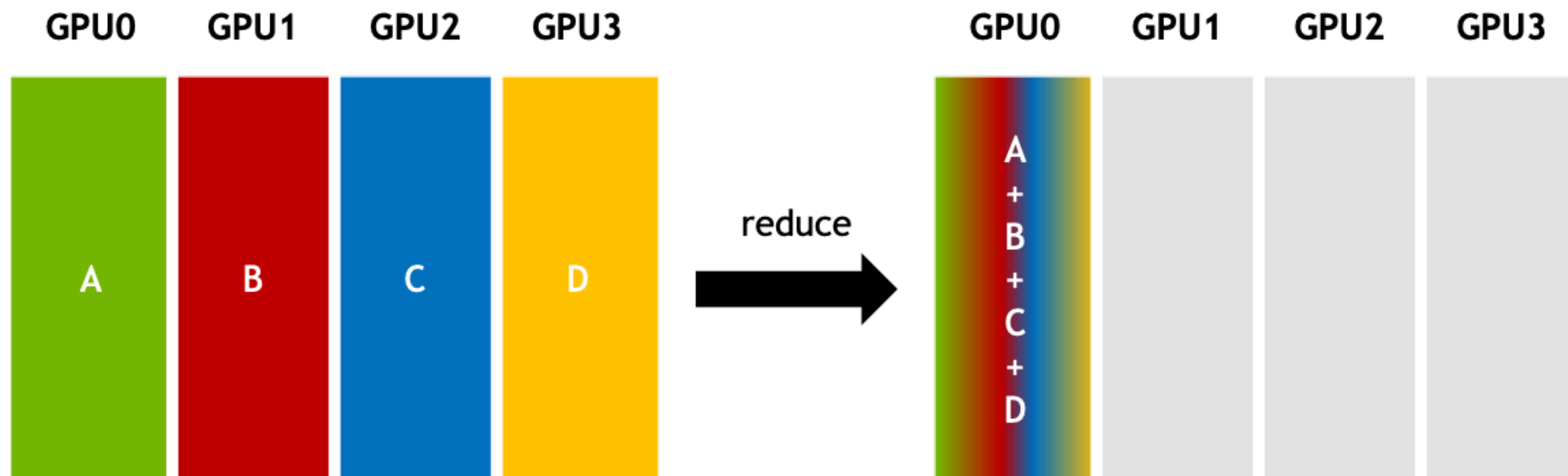
AllReduce



There are many possible implementations! E.g., compute in a ring

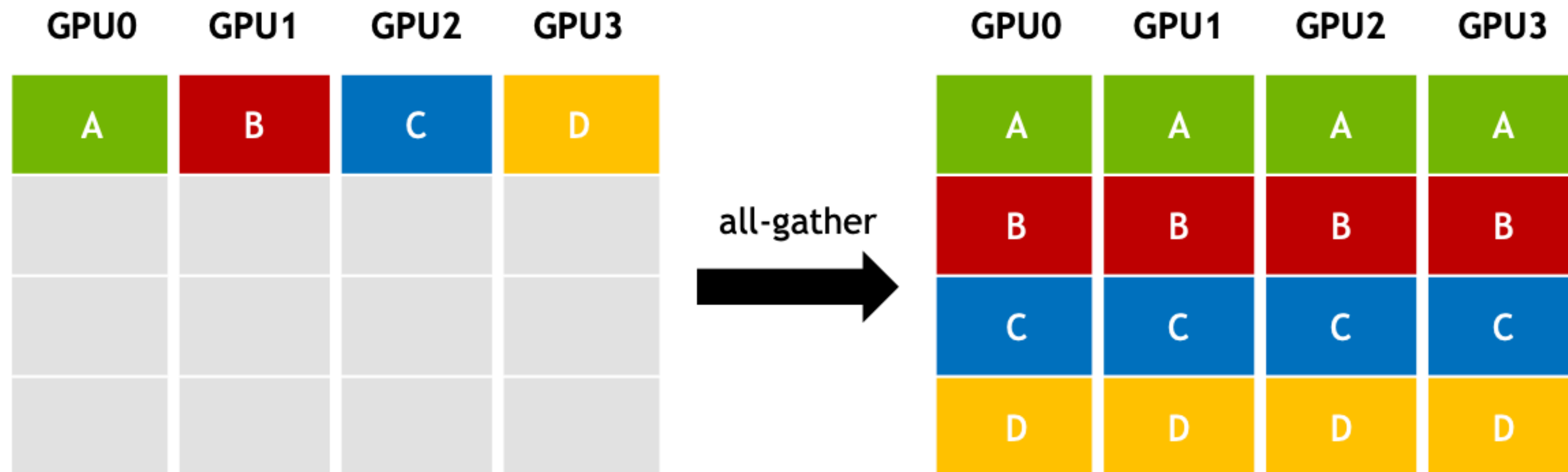
NCCL communication primitives

Reduce



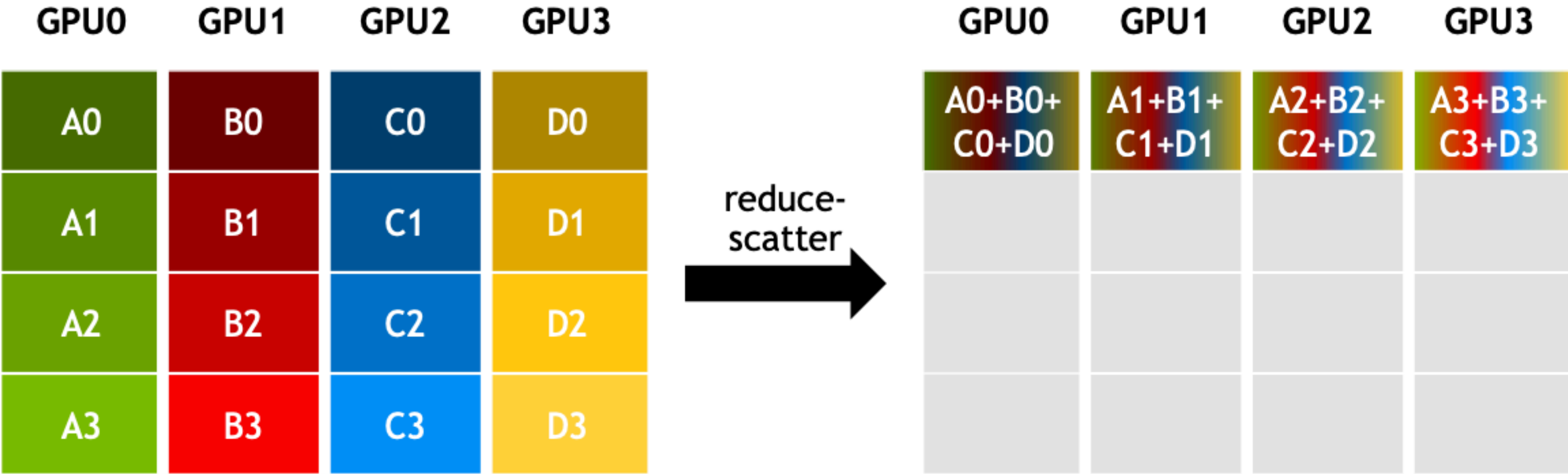
NCCL communication primitives

AllGather



NCCL communication primitives

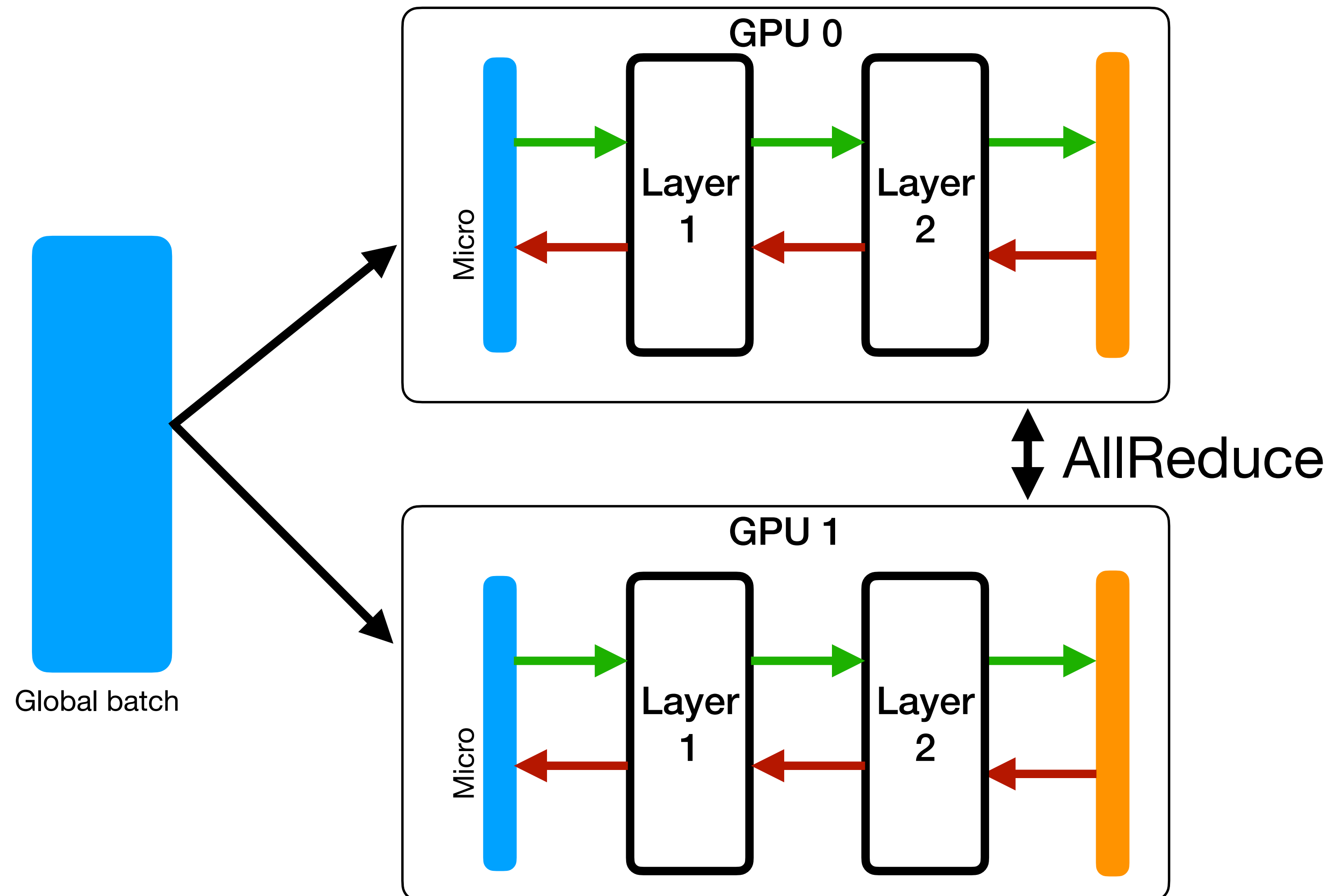
ReduceScatter



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Multi GPU Training: DDP



When is DDP useful?

- When a model fits on a single GPU, and we want to increase data throughput i.e. train faster
- When it makes sense to keep inter-GPU communication as simple as possible (e.g., smaller scale experiments)
- Models that are large enough that cannot be fit on a single GPU are trained with other distributed frameworks (FSDP, etc.)

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Before this, let's consider linear nets as our model (i.e. matrix multiplies)

Our Computational Model

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- (batch) Linear Network: $Y = W^{L-1} \dots W^0 X$
 - $W^\ell \in R^{d \times d}, X \in R^{d \times m}$,
layers have input/output dimension d , batch size is m

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 - Activation memory: Ldm
- Important: note that param memory \gg activation memory, when $d \gg m$
- Other considerations:
 - Total flops: # gpus * time gpus run for * flops/gpu
 - Serial runtime: we want our job to finish soon (in a few months?)

Now lets look at LLama 3.1

	8B	70B	405B
Layers	32	80	126
Model Dimension	4,096	8192	16,384
FFN Dimension	14,336	28,672	53,248
Attention Heads	32	64	128
Key/Value Heads	8	8	8
Peak Learning Rate	3×10^{-4}	1.5×10^{-4}	8×10^{-5}
Activation Function		SwiGLU	
Vocabulary Size		128,000	
Positional Embeddings		RoPE ($\theta = 500,000$)	

Table 3 Overview of the key hyperparameters of Llama 3. We display settings for 8B, 70B, and 405B language models.

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140gb 2TB

H100

80gb.

seq length

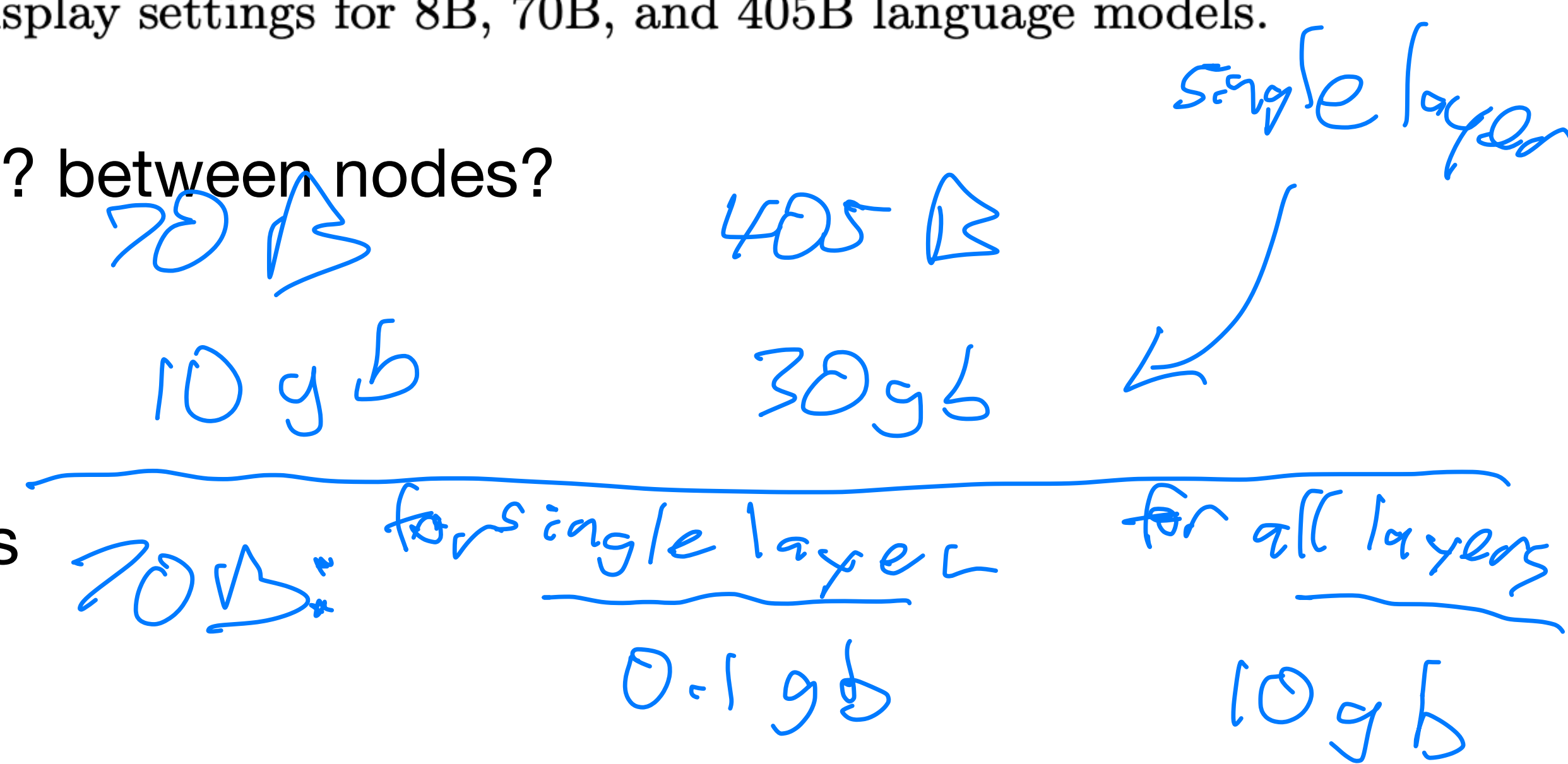
8192

Nodes

8 gpus/node

Table 3 Overview of the key hyperparameters of Llama 3. We display settings for 8B, 70B, and 405B language models.

- Concepts: what fits on a gpu? on a node? between nodes?
- Params/transformer block: $10d^2$
 - Bytes/block: $2 \cdot 10d^2$
- Activation Memory for batch size 1: $2 \cdot \text{seq_length} \cdot d \cdot \text{num_layers}$ bytes



all layers

GPUs	TP	CP	PP	DP	Seq. Len.	Batch size/DP	Tokens/Batch	TFLOPs/GPU	BF16 MFU
8,192	8	1	16	64	8,192	32	16M	430	43%
16,384	8	1	16	128	8,192	16	16M	400	41%
16,384	8	16	16	4	131,072	16	16M	380	38%

Table 4 Scaling configurations and MFU for each stage of Llama 3 405B pre-training. See text and Figure 5 for descriptions of each type of parallelism.

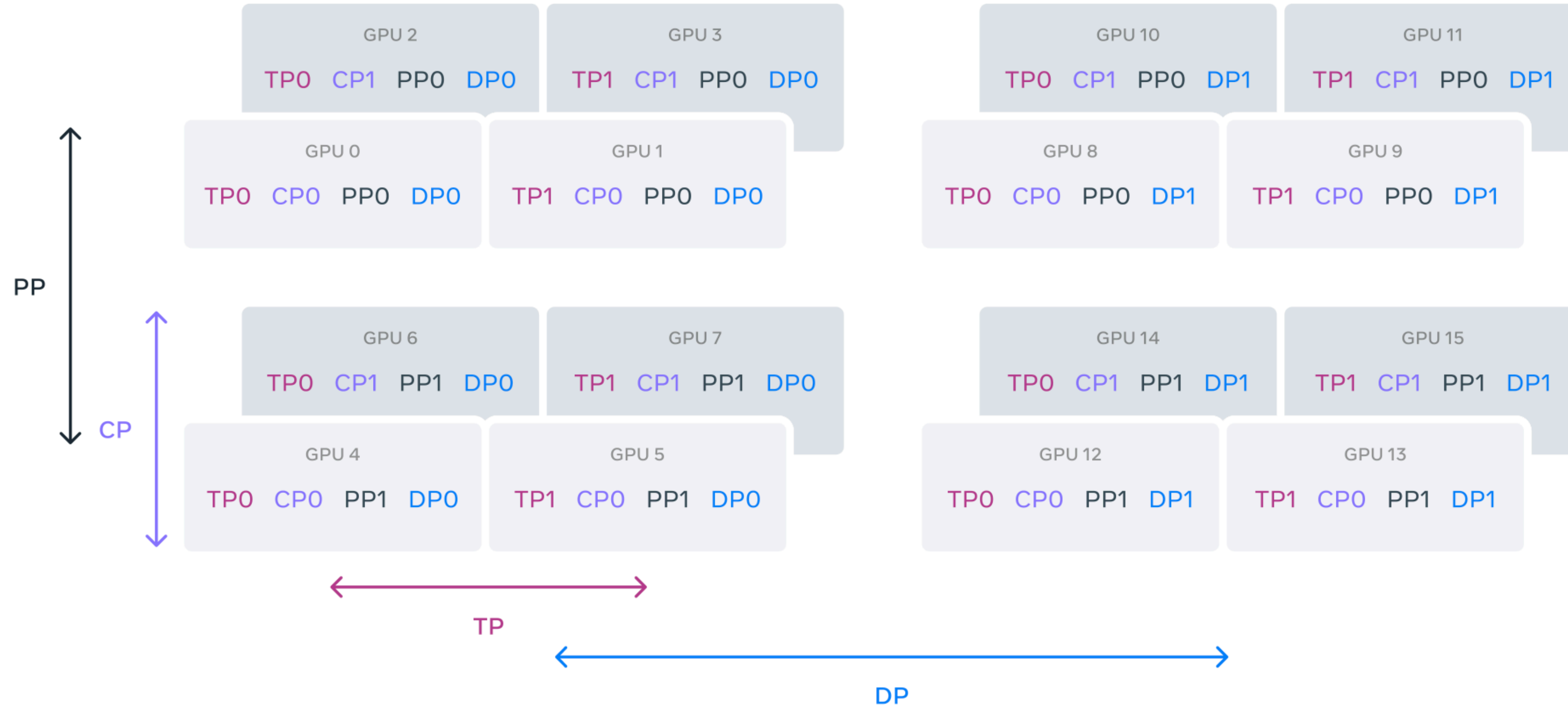
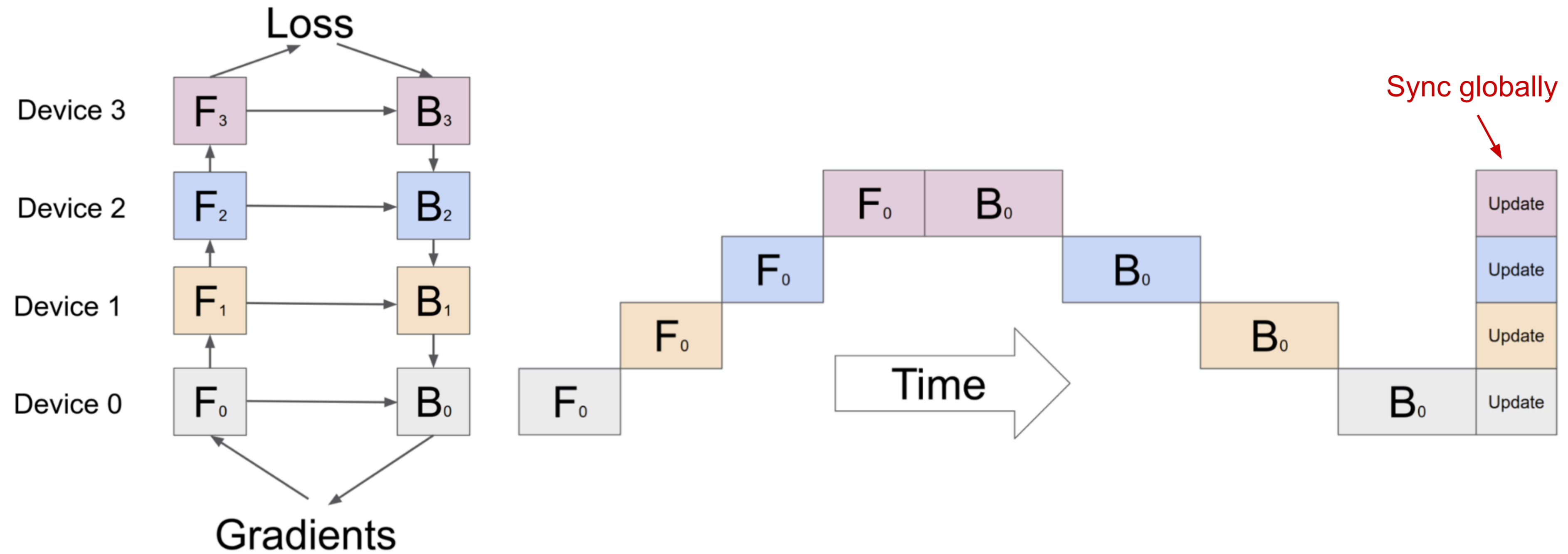


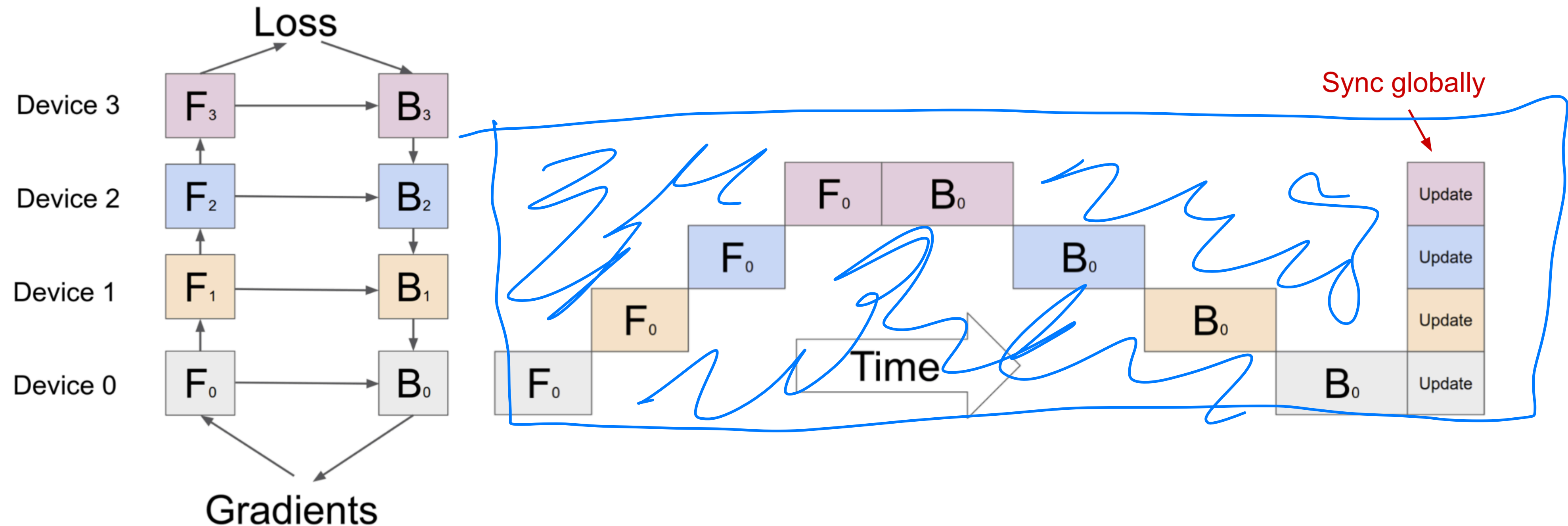
Figure 5 Illustration of 4D parallelism. GPUs are divided into parallelism groups in the order of [TP, CP, PP, DP], where DP stands for FSDP. In this example, 16 GPUs are configured with a group size of $|\text{TP}|=2$, $|\text{CP}|=2$, $|\text{PP}|=2$, and $|\text{DP}|=2$. A GPU's position in 4D parallelism is represented as a vector, $[D_1, D_2, D_3, D_4]$, where D_i is the index on the i -th parallelism dimension. In this example, GPU0[TP0, CP0, PP0, DP0] and GPU1[TP1, CP0, PP0, DP0] are in the same TP group, GPU0 and GPU2 are in the same CP group, GPU0 and GPU4 are in the same PP group, and GPU0 and GPU8 are in the same DP group.

Pipeline Parallelism

Naive Model Parallelization

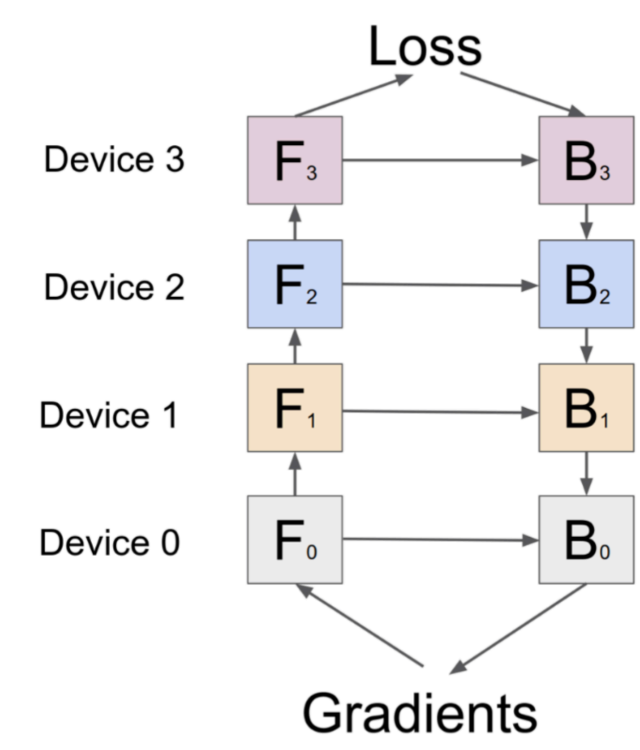


Naive Model Parallelization

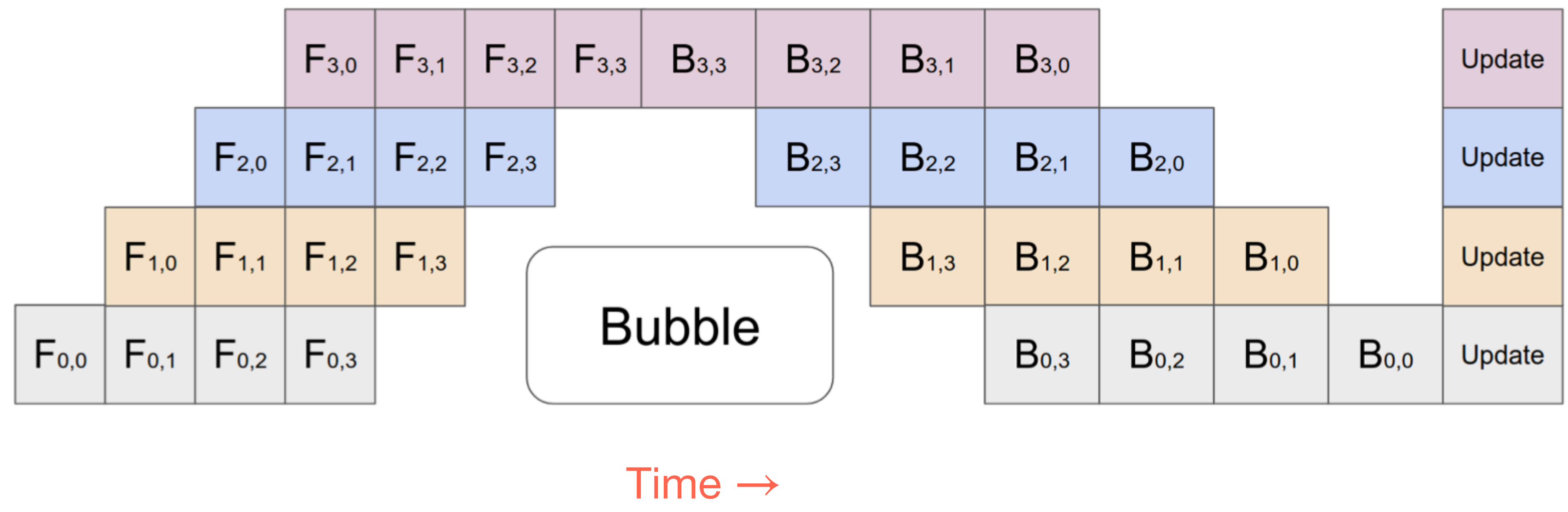


- Shard model into k partitions, e.g. $k = 4$, $W^{0:L/4}$, $W^{L/4+1:L/2}$, $W^{L/2+1:3L/4}$, $W^{3L/4+1:L-1}$
- Assume: each device can hold a model partition, which is of size $Ld^2/4$
- **What is the problem?**

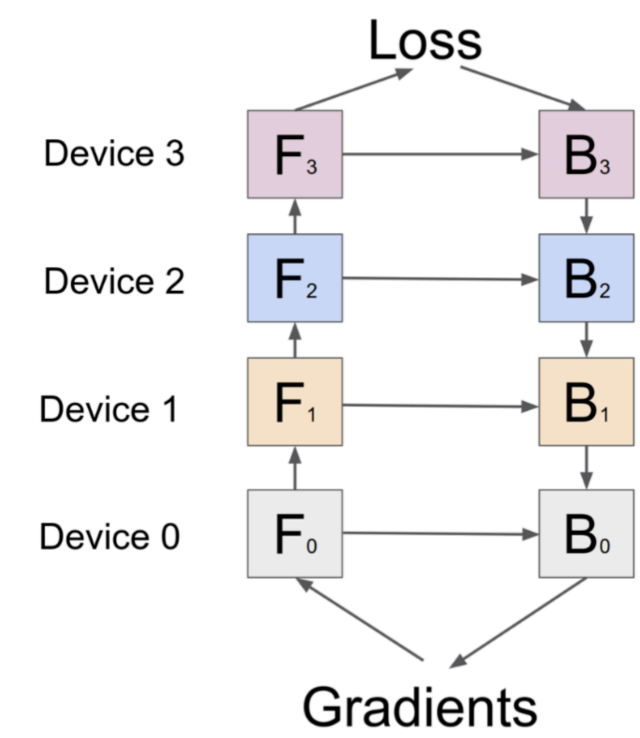
The pipeline approach:



Device 3
 Device 2
 Device 1
 Device 0



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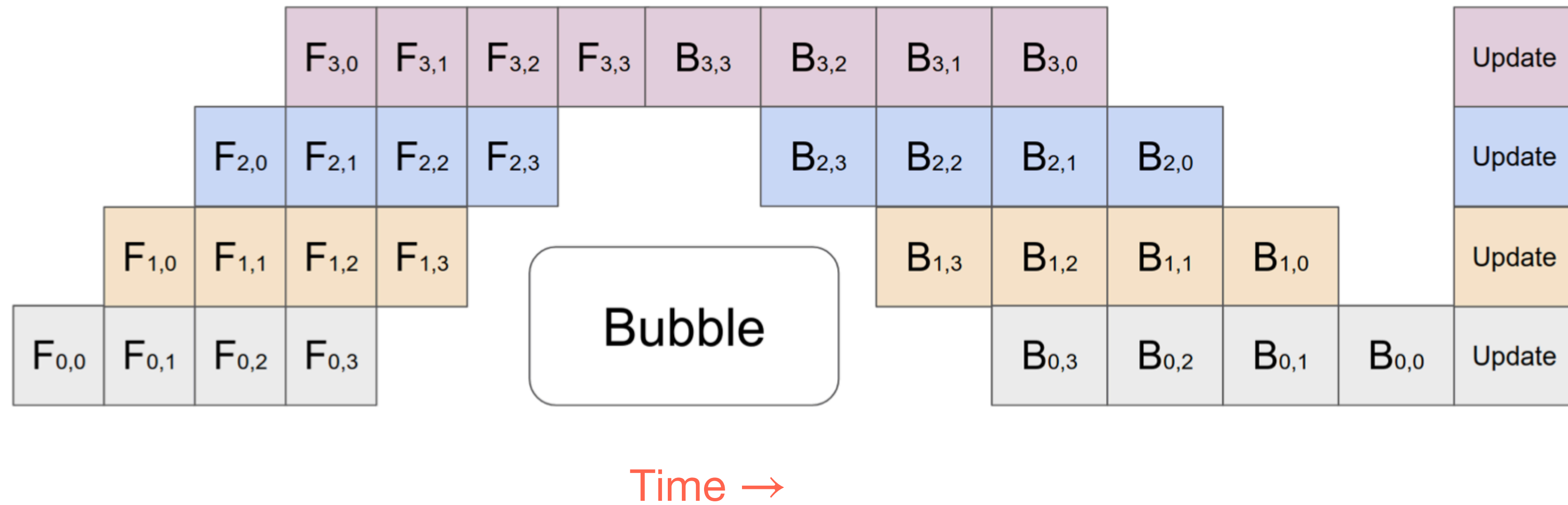


Device 3

Device 2

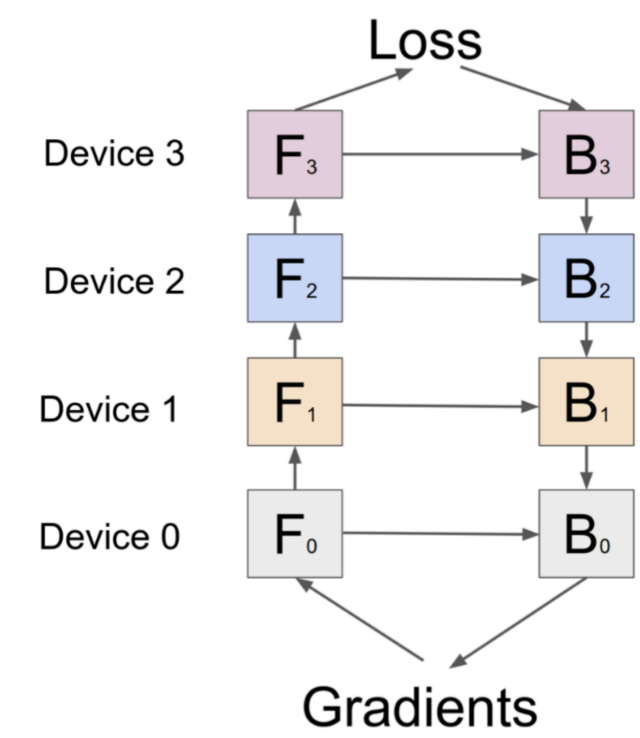
Device 1

Device 0



- Shard model into p partitions and place these on p devices, i.e. $p = 4$ example, where device 0 contains $W^{0:L/4}$, device 1 contains $W^{L/4+1:L/2}$, ...
- Split mini-batch T , of size m , into k “micro-batches”, $\{T_0, \dots, T_{k-1}\}$, each of size m/k

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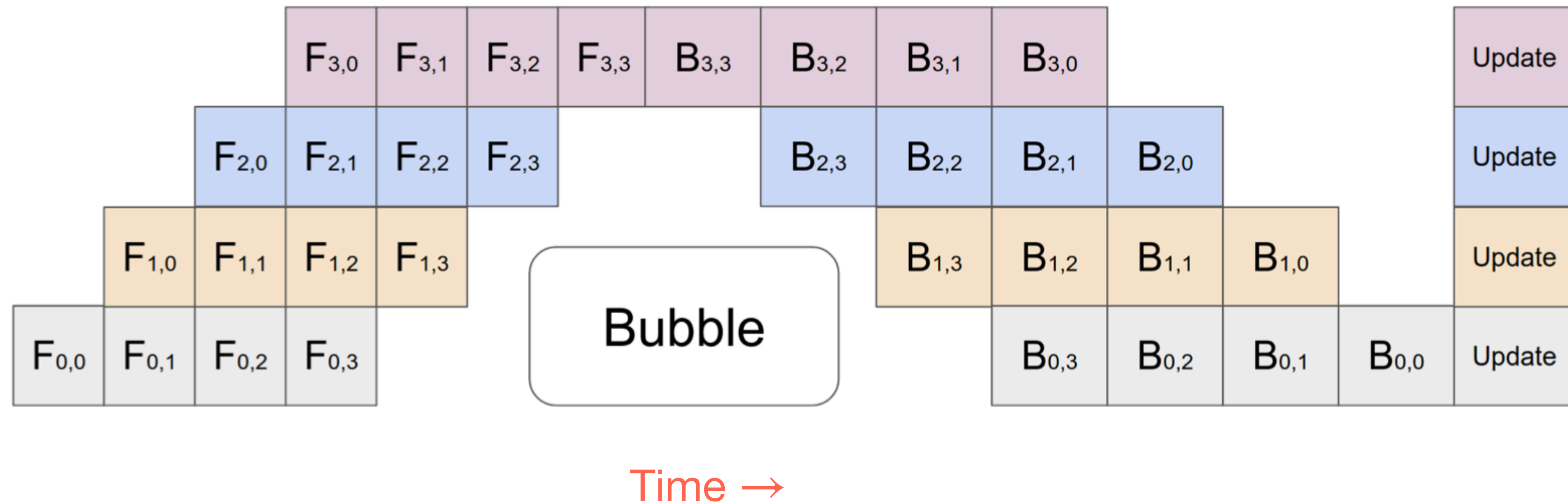


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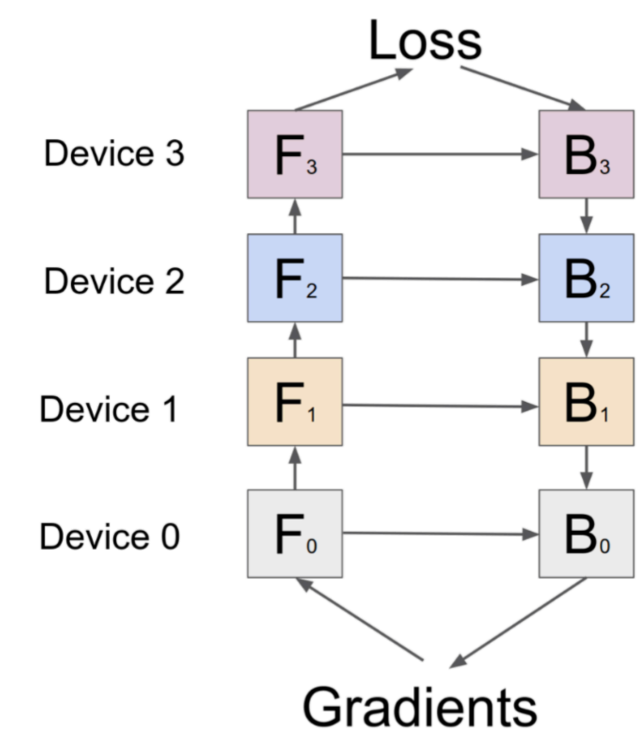
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- Split mini-batch T , of size m , into k “micro-batches”, $\{T_0, \dots, T_{k-1}\}$, each of size m/k
- The pipeline approach tries to avoid the idle time, by sending the next micro-batch when it can.
- Assume devices can hold: a model shard of size $Ld^2/4$ and the activation checkpoints, of total size $Ldm/4$

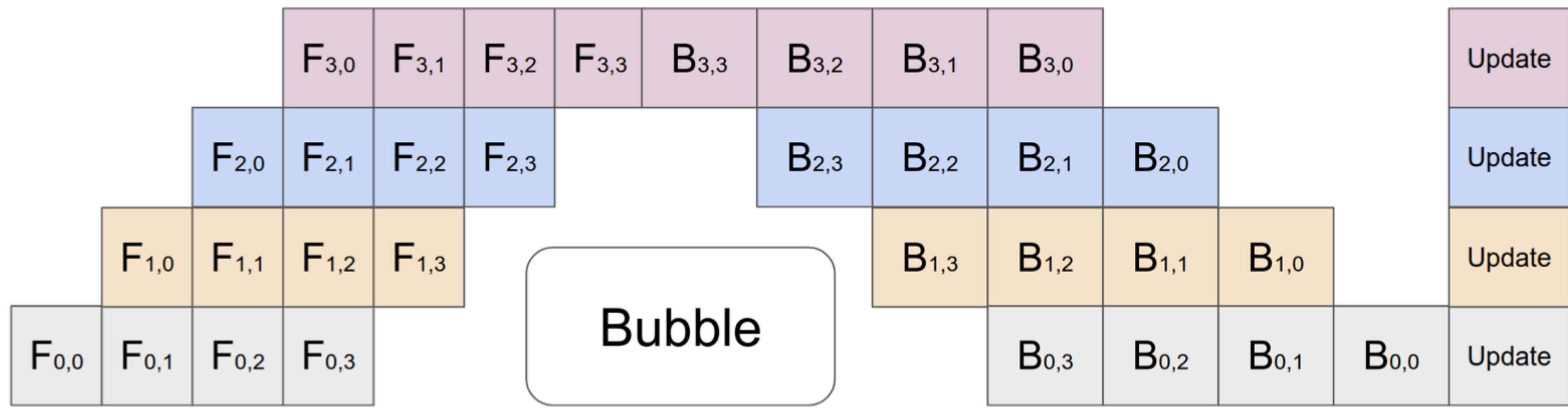


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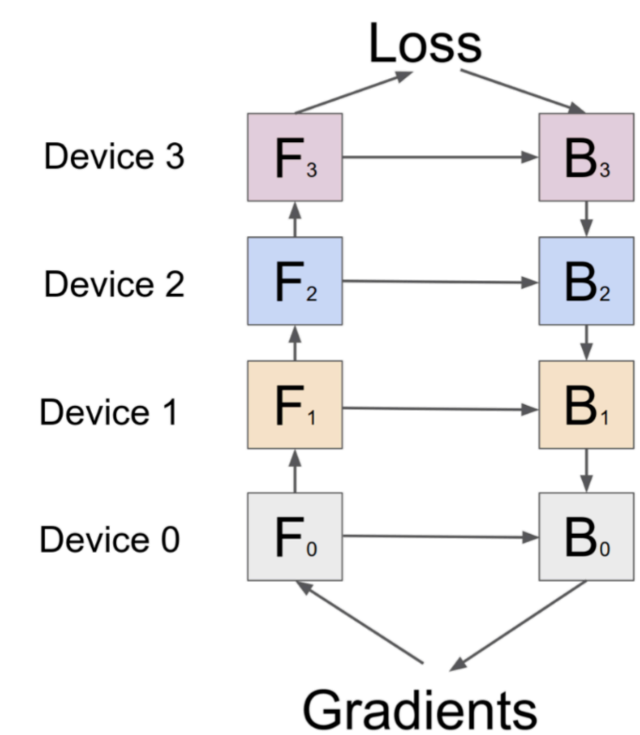
Device 2

Device 1

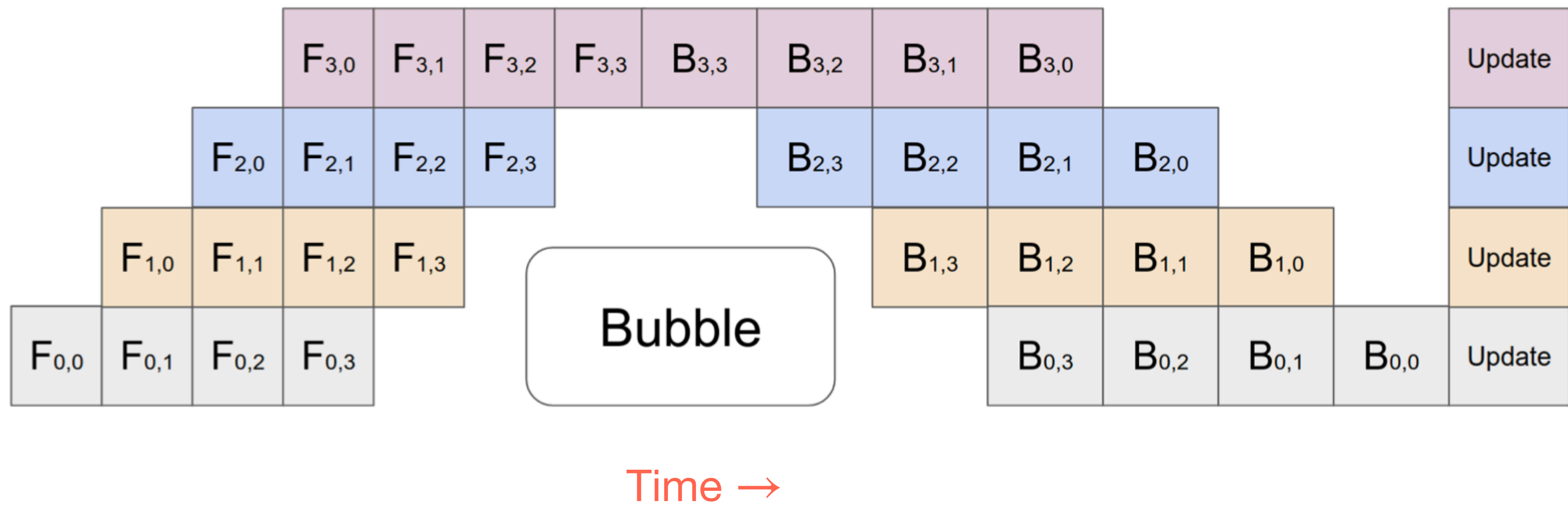
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Time →

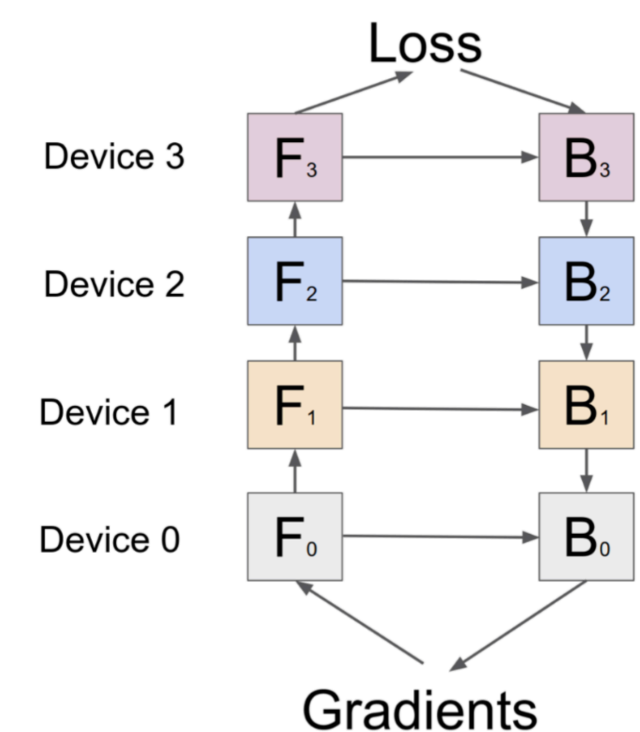


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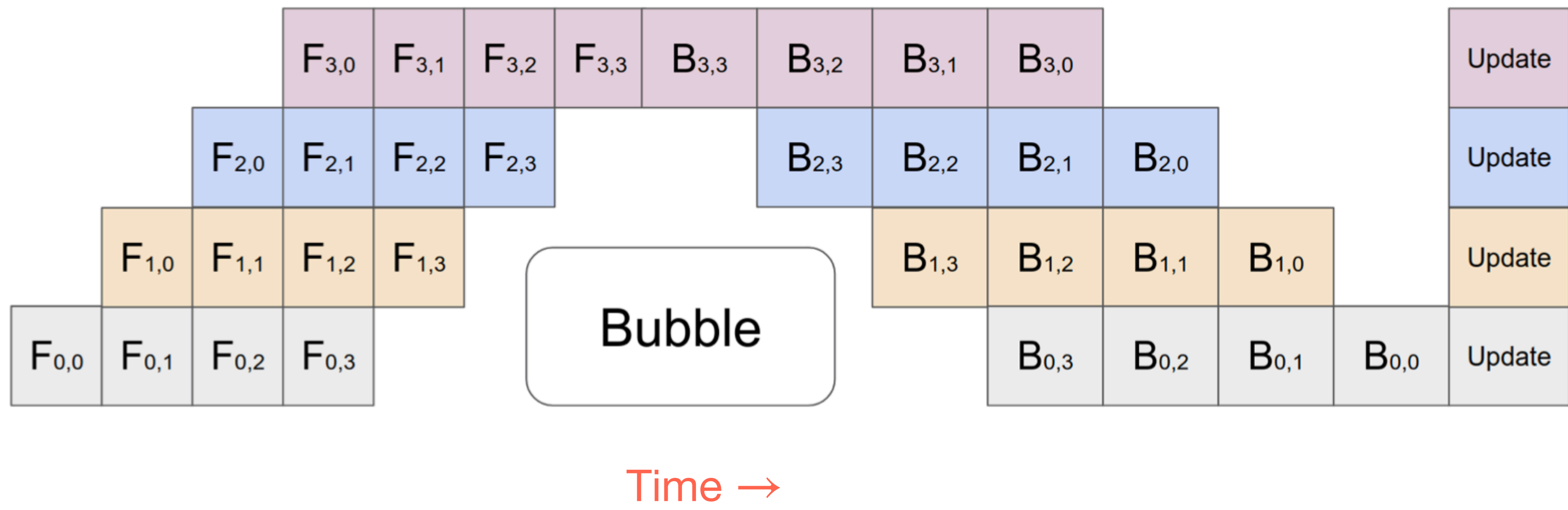


Time →

- Notation: $F_{i,j}$ denotes the forward pass computed by device i on micro-batch T_j (analogous def for $B_{i,j}$) recall that device i contains a model shard, containing some of the layers.

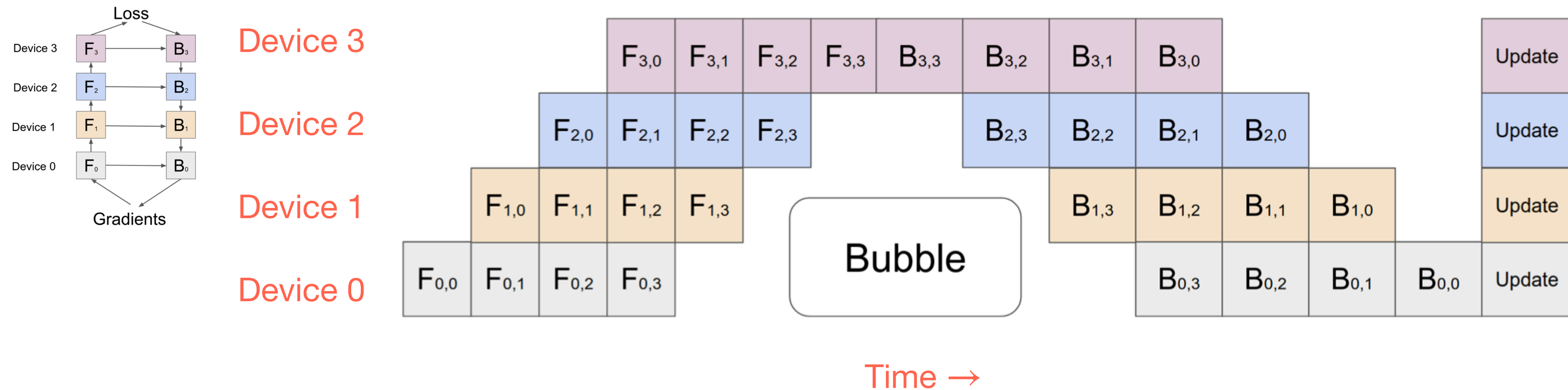


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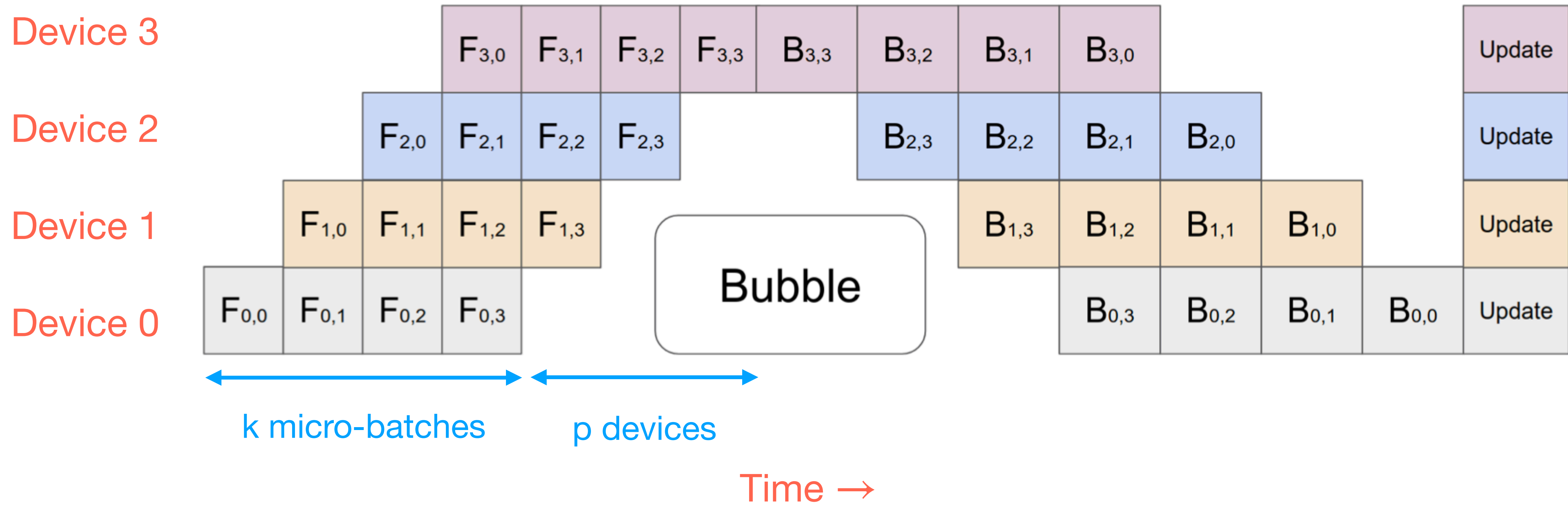
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- **Forward:**
 - Device i computes the forward pass on data T_j , after receiving the input activations from device $i - 1$.
 - All activations are checkpointed on their corresponding device.
- After all the forward passes are done, we can begin the backward pass. One approach is to start with $B_{3,3}$

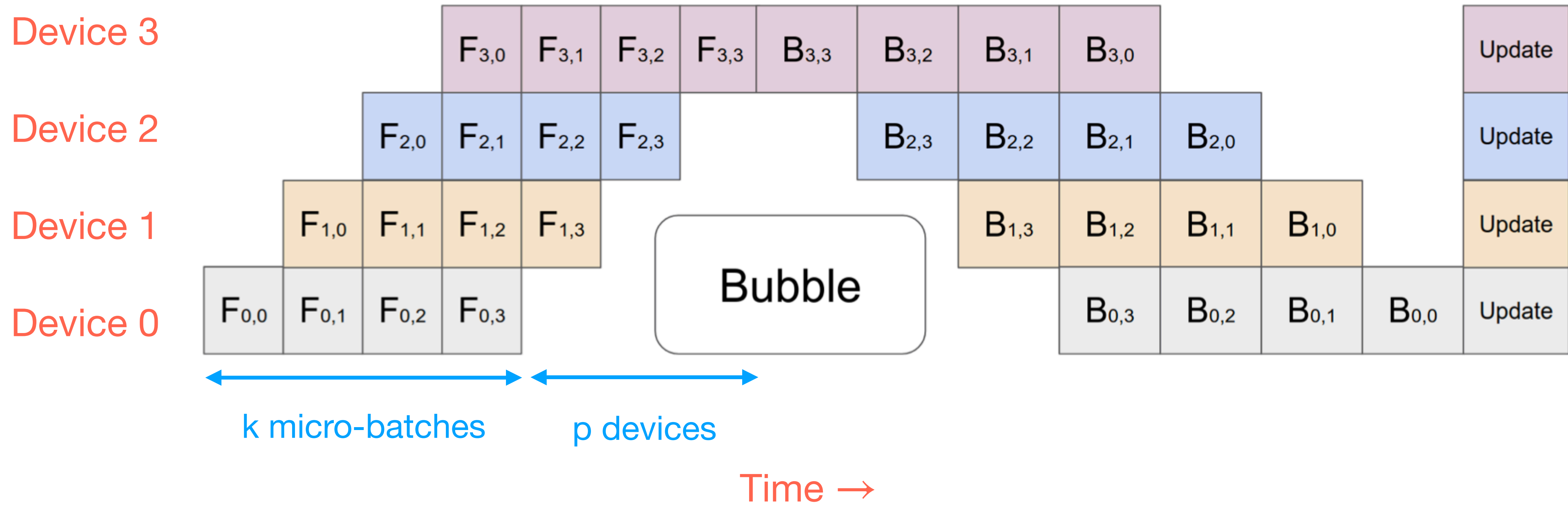


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- **Backward:**
 - Device i computes the backward pass on data T_j , after receiving the activation grads from device $i + 1$.
 - Each gradient can be all-reduced.

Idle Time & MFU

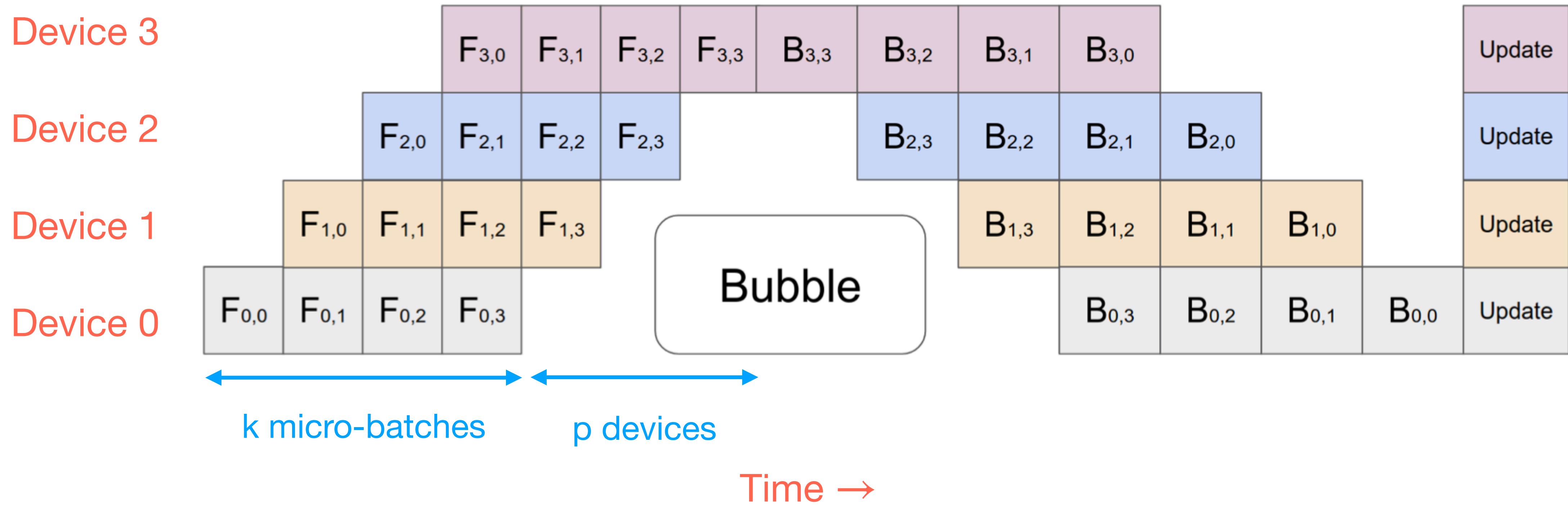


Idle Time & MFU



What fraction of time is IDLE?

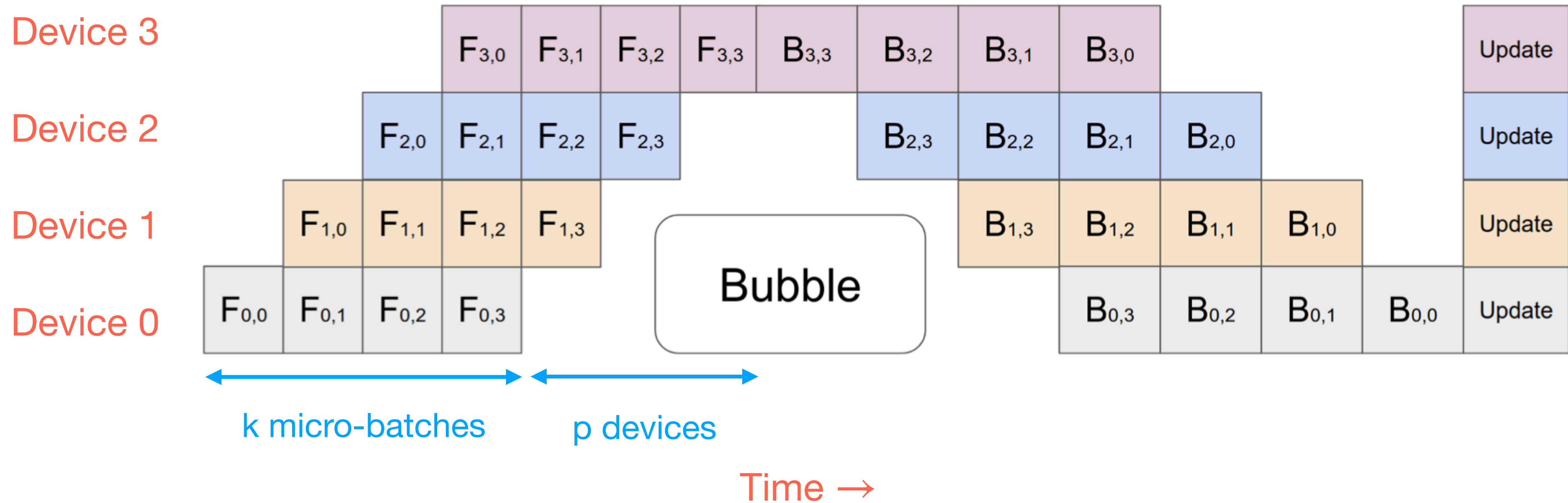
Idle Time & MFU



What fraction of time is IDLE?

$$\frac{p}{p + k}$$

Idle Time & MFU



What fraction of time is IDLE?

$$\frac{p}{p+k}$$

$\Rightarrow \frac{1}{4}$ idle time

So if $k \approx 3p$, then ...

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 - Suppose V layers can fit on a device and their activations, so we have $Vd^2 + Vdm$ free memory.
 - With p devices, we can get a model with $L = pV$ and width d .

$$\# \quad pVd^2$$

$$V^2 d_m + 2 d_m$$

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- We need to **ensure communication and compute overlap** between the nodes/devices
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 - Need to all-reduce model params: need to communicate Vd^2 (per backward step in the pipe)

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- **Take aways:** (assume Chinchilla where tokens $\approx 20 \cdot$ model size)
 - Depth scaling: **serial processing time of pipeline grows linearly** with model size, fixing m .
 - This means that serial run time grows quadratically (serial runtime is $O(\text{tokens} \cdot \text{time_per_iter})$)
 - We pay a serial factor of 3 (the amortization factor) over to pure DDP (i.e. using batch size one).

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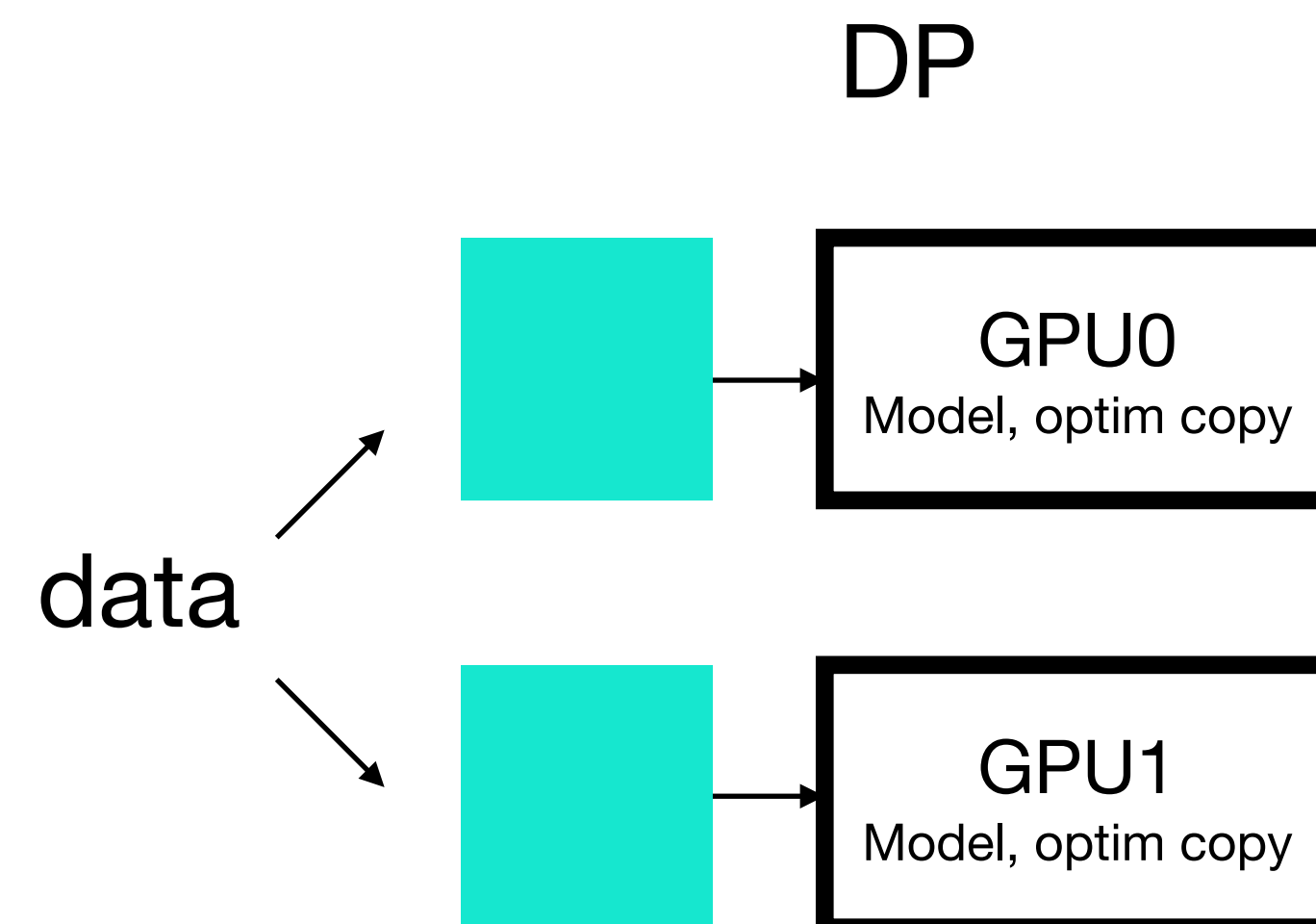
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 - We pay a serial factor of 3 (the amortization factor) over to pure DDP (i.e. using batch size one).
- Even if we make the per-device-batchsize- m smaller (+DDP over the pipelines), we still have a communication bottleneck due to the model params on the backward pass.

Today

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- ✓ • FSDP
- Theoretical Considerations
- Tensor Parallelism

Fully Sharded Data Parallel (FSDP)

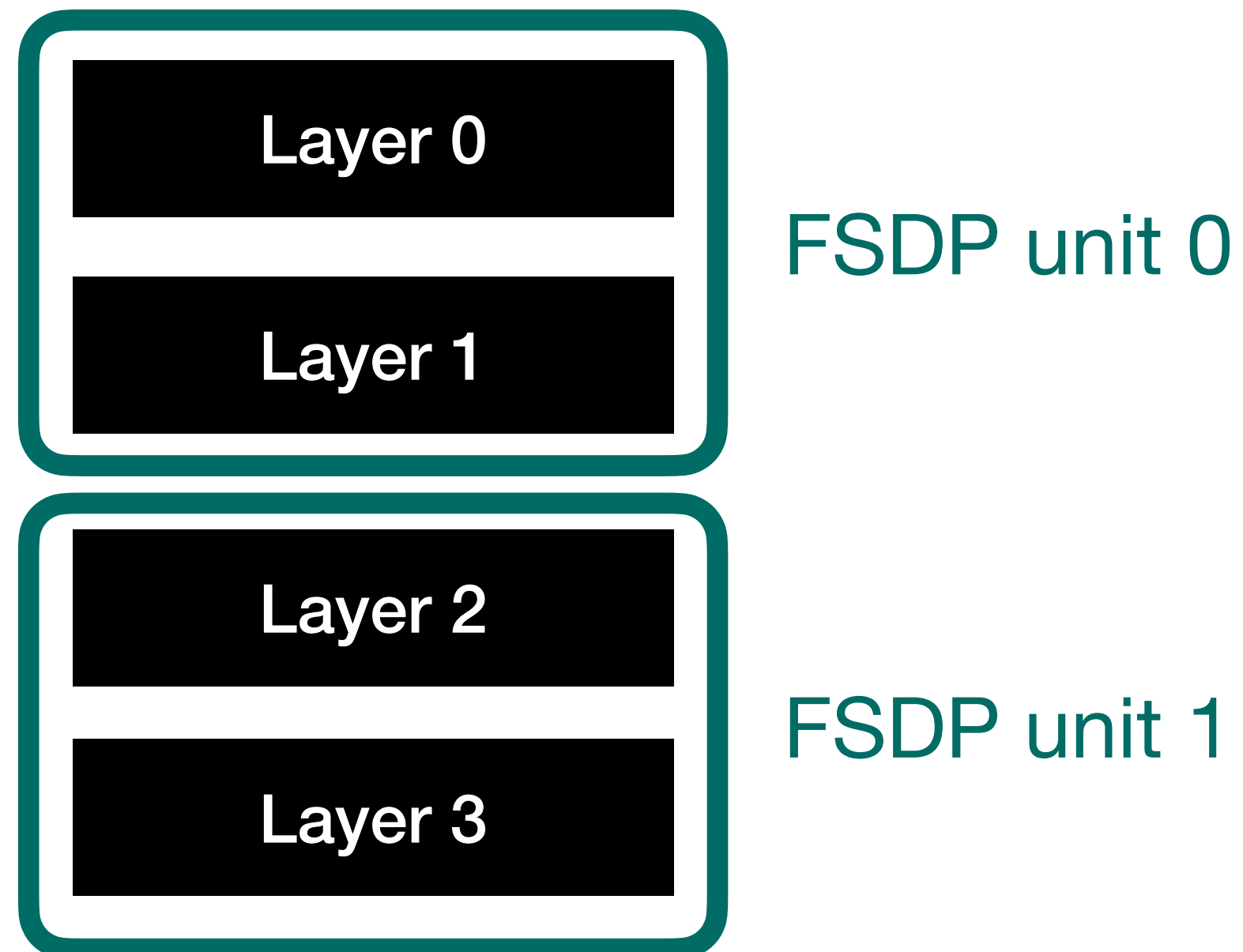
- Motivation: we want to do data distributed training *without* a pipeline
- **Fully** sharded = shard model, optimizer, and data across GPUs (can be seen as a kind of successor to DDP.)
- Inspired by “ZeRO” algorithm (particularly ZeRO-3), but some specifics are different



How is the model stored? Terminology: shards and units

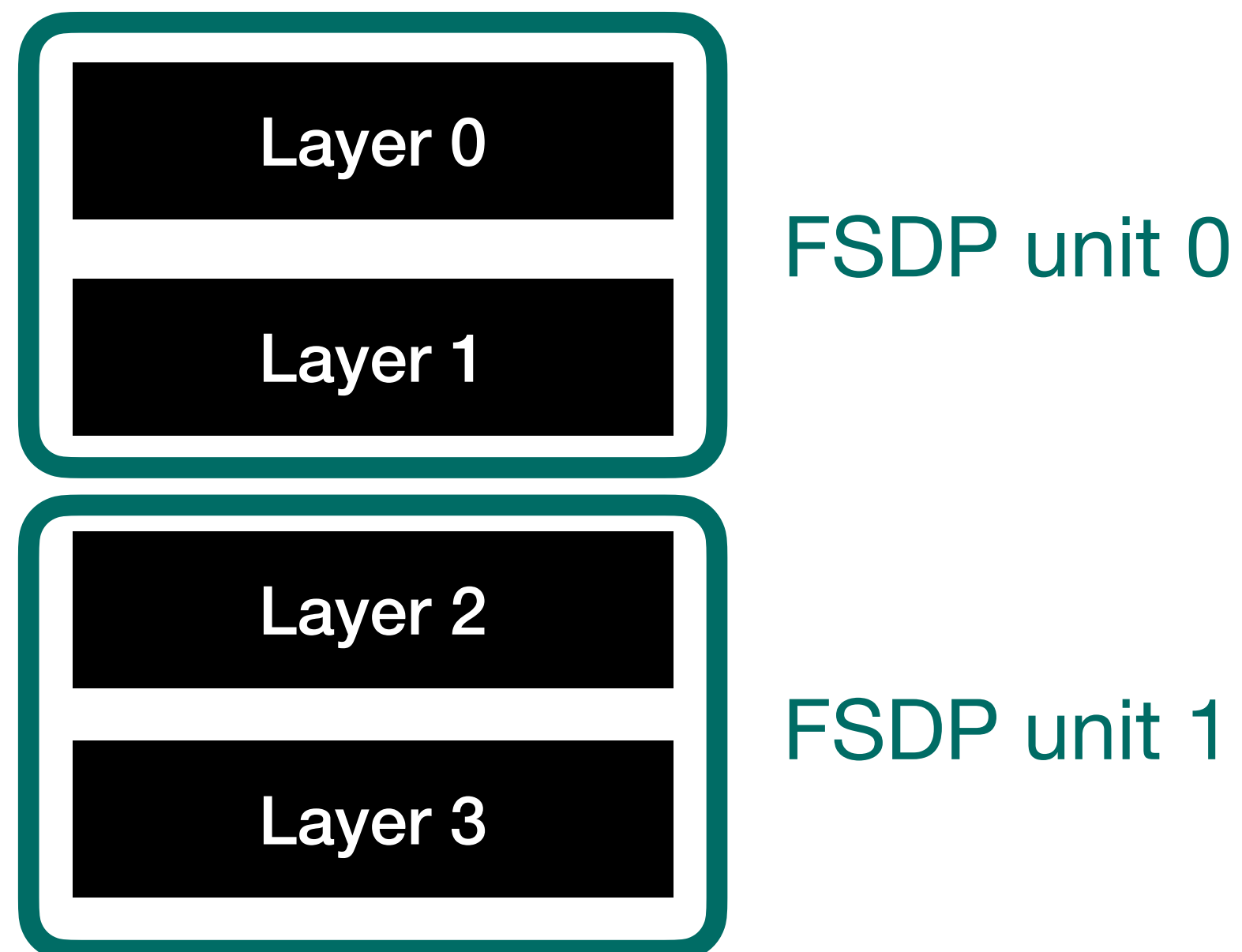
- Let's forget about optimizer states for a second, how is the model even stored?
- An **FSDP unit** is an abstraction that determines how the model will be split. We have flexibility in how to define it!
- For example, an FSDP unit could be a single layer (or a series of layers). Practically, it is a `torch.nn.Module` or collection of layers
- Units are broken down further into **shards**, which is how the units will be stored across the GPUs, i.e. each FSDP unit is **sharded** across GPUs.

How is the model stored? Terminology: shards and units



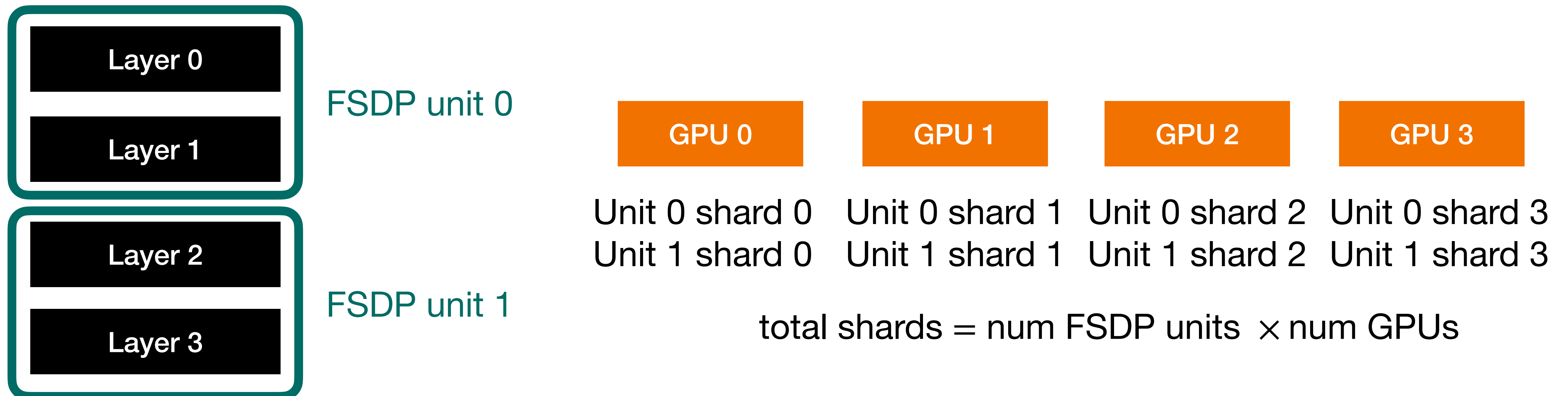
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- **Note:** “unit” is some piece of the model that we want to load. (e.g. loading unit 0 onto gpu 3, means layers 0/1 are on gpu 3)



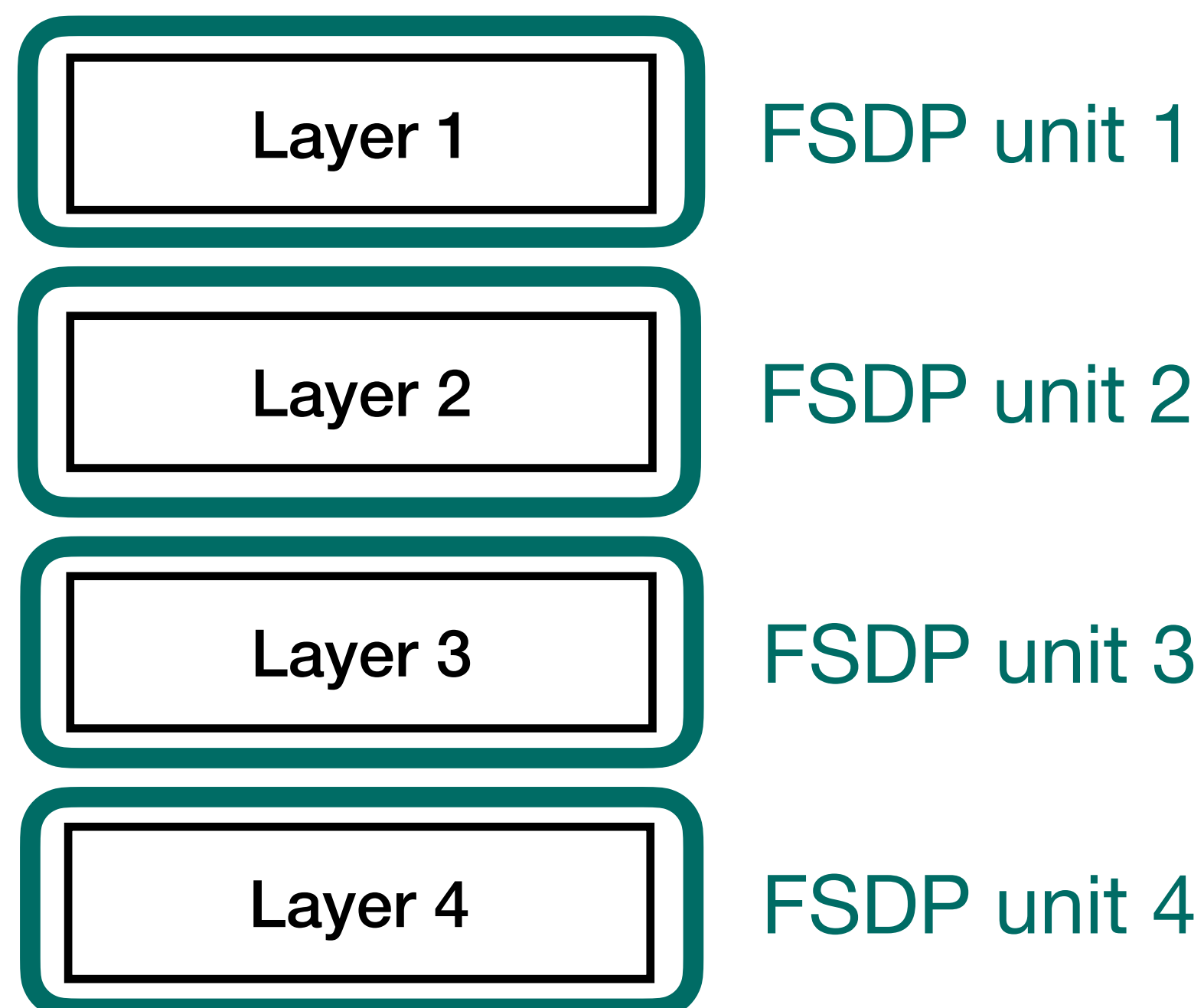
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- **Note:** “unit” is some piece of the model that we want to load. (e.g. loading unit 0 onto gpu 3, means layers 0/1 are on gpu 3)
- A fundamental operation will be to load a unit onto multiple GPUs
 - Conceptually, **we will only load units** so we can ignore the shards.



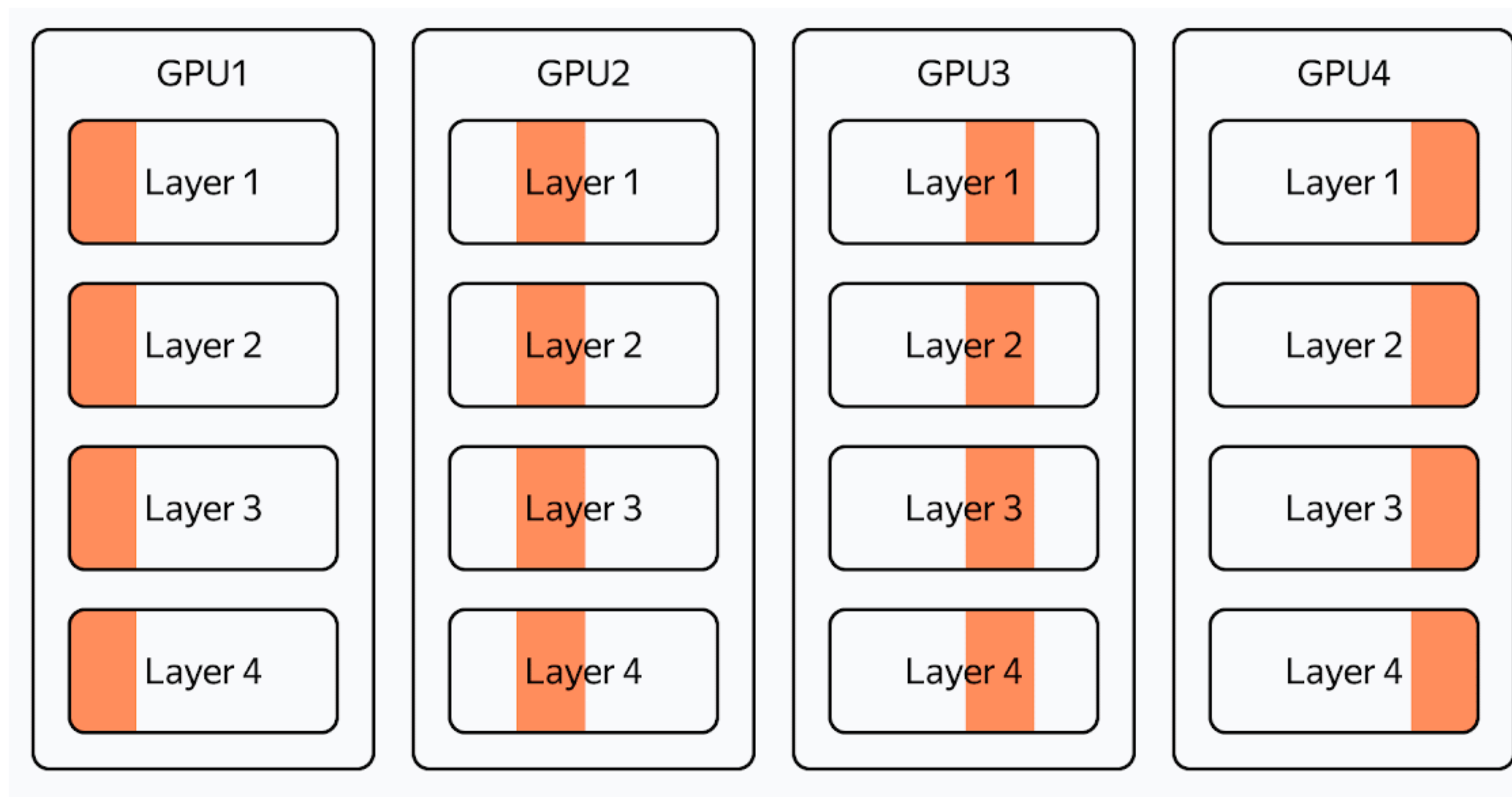
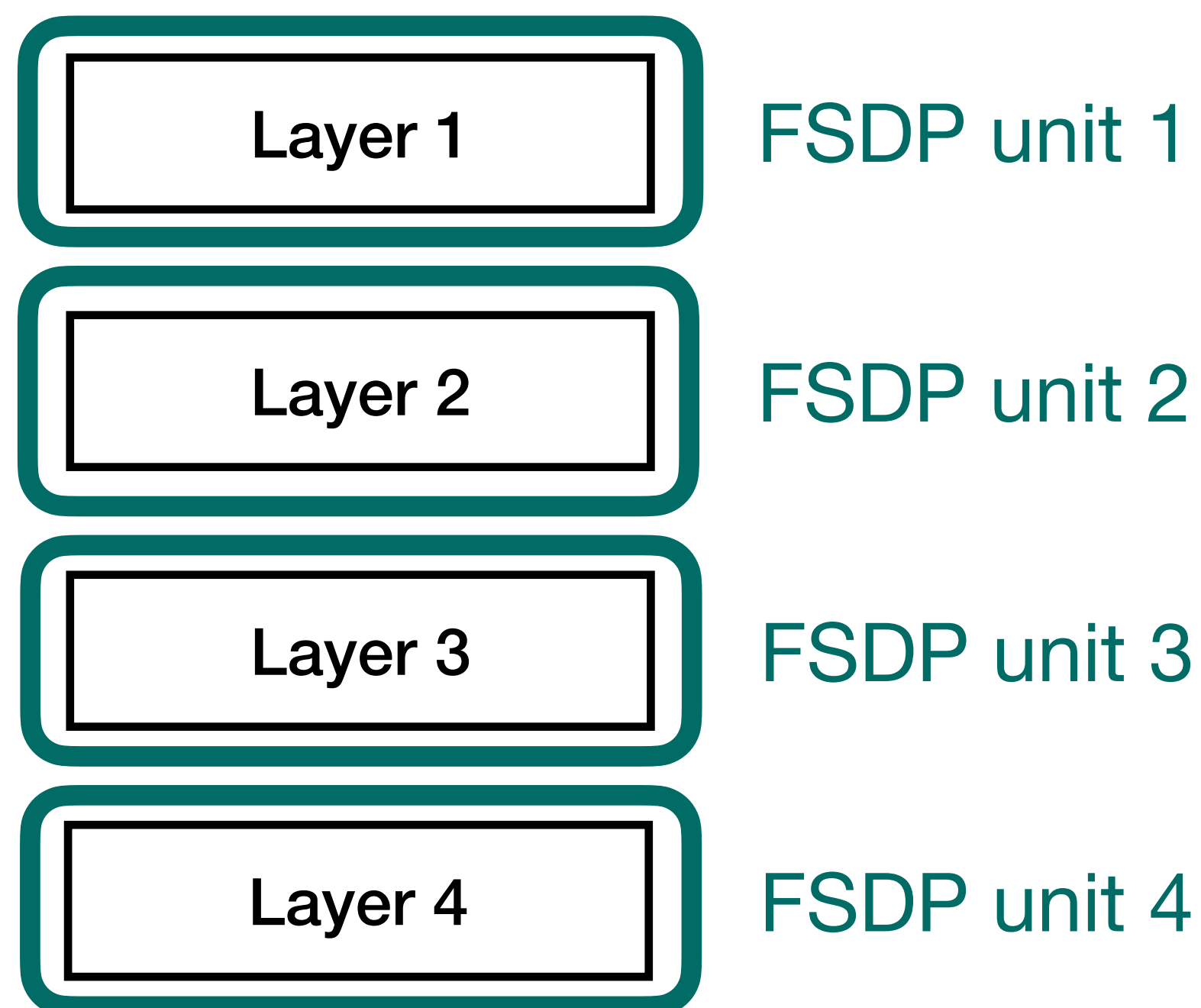
How does the computation work?

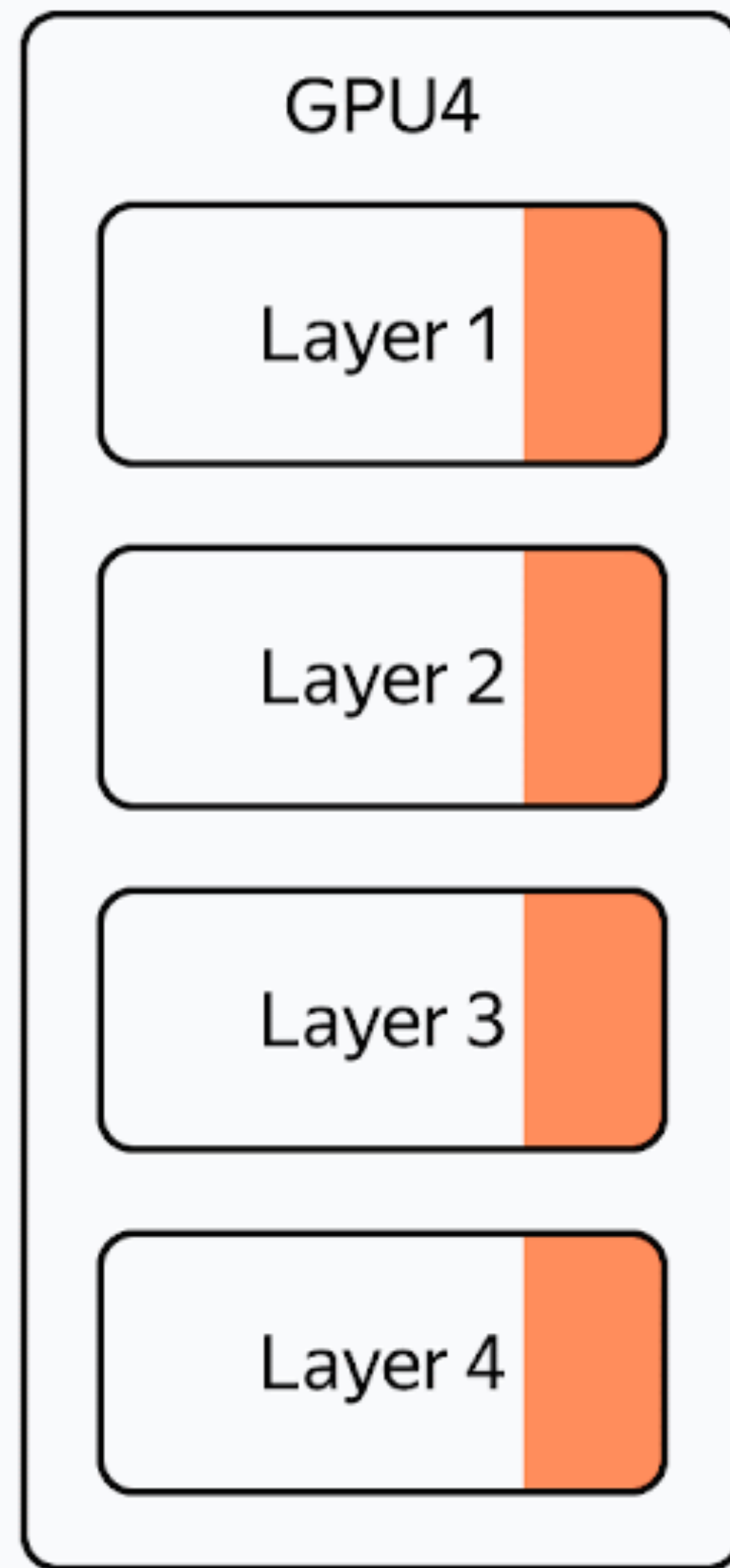
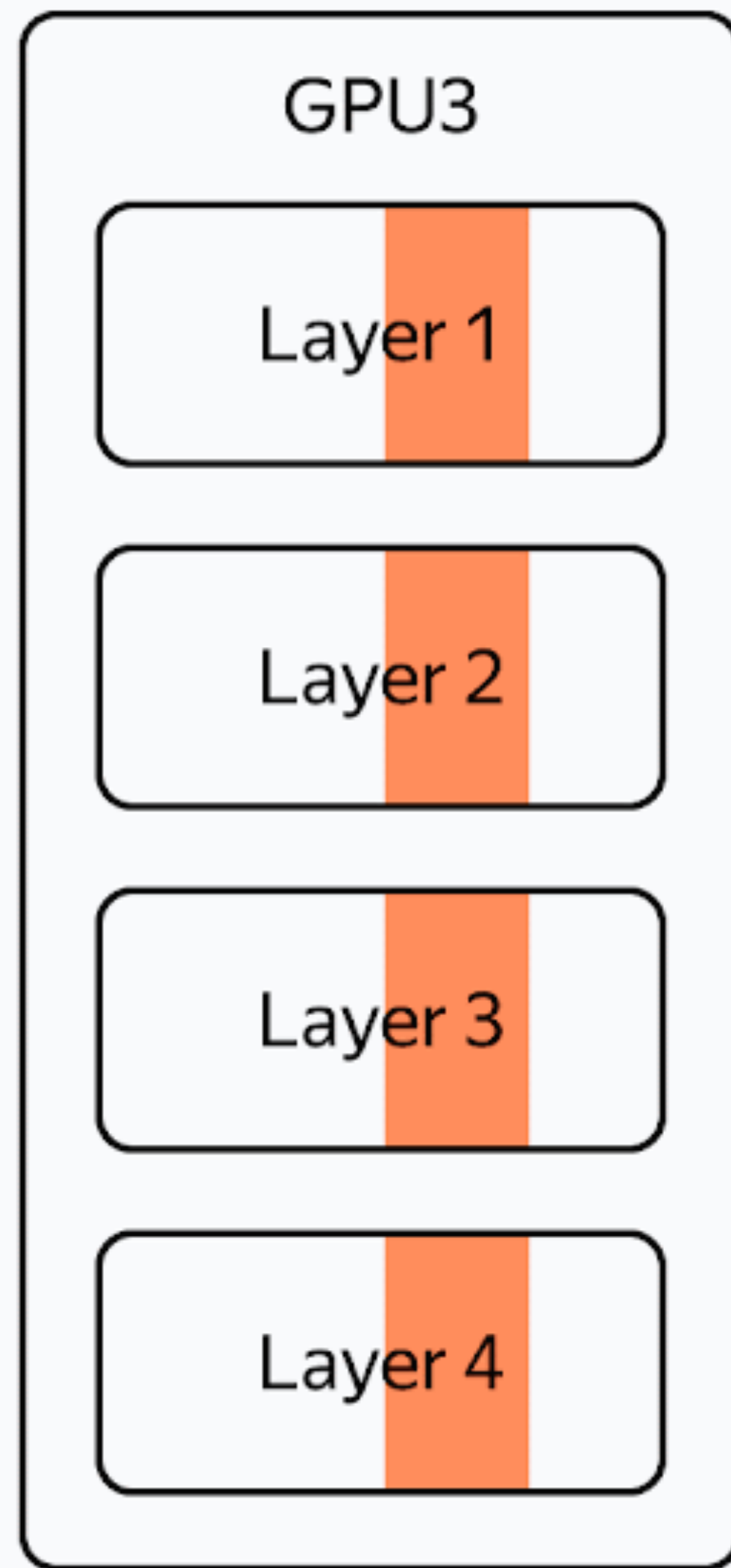
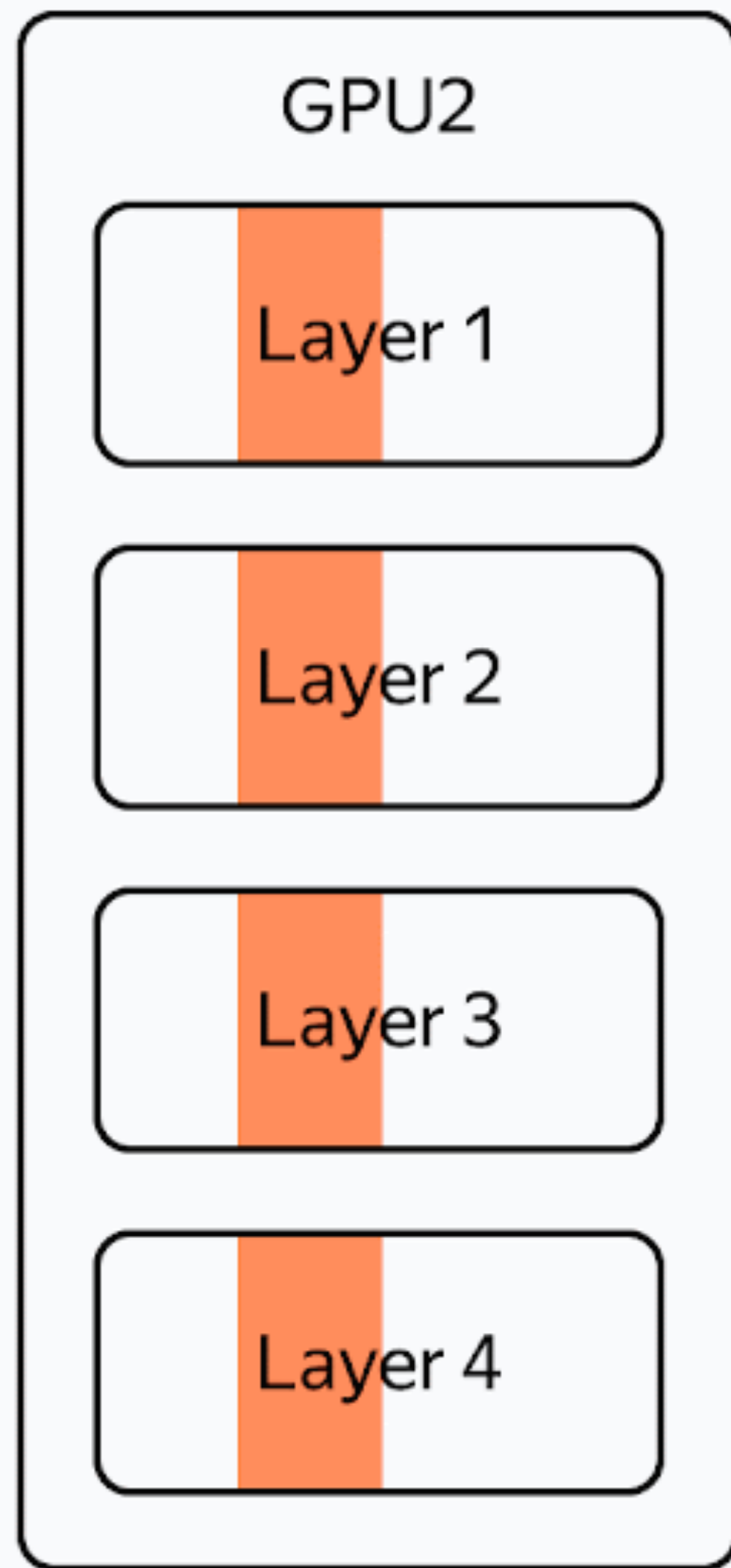
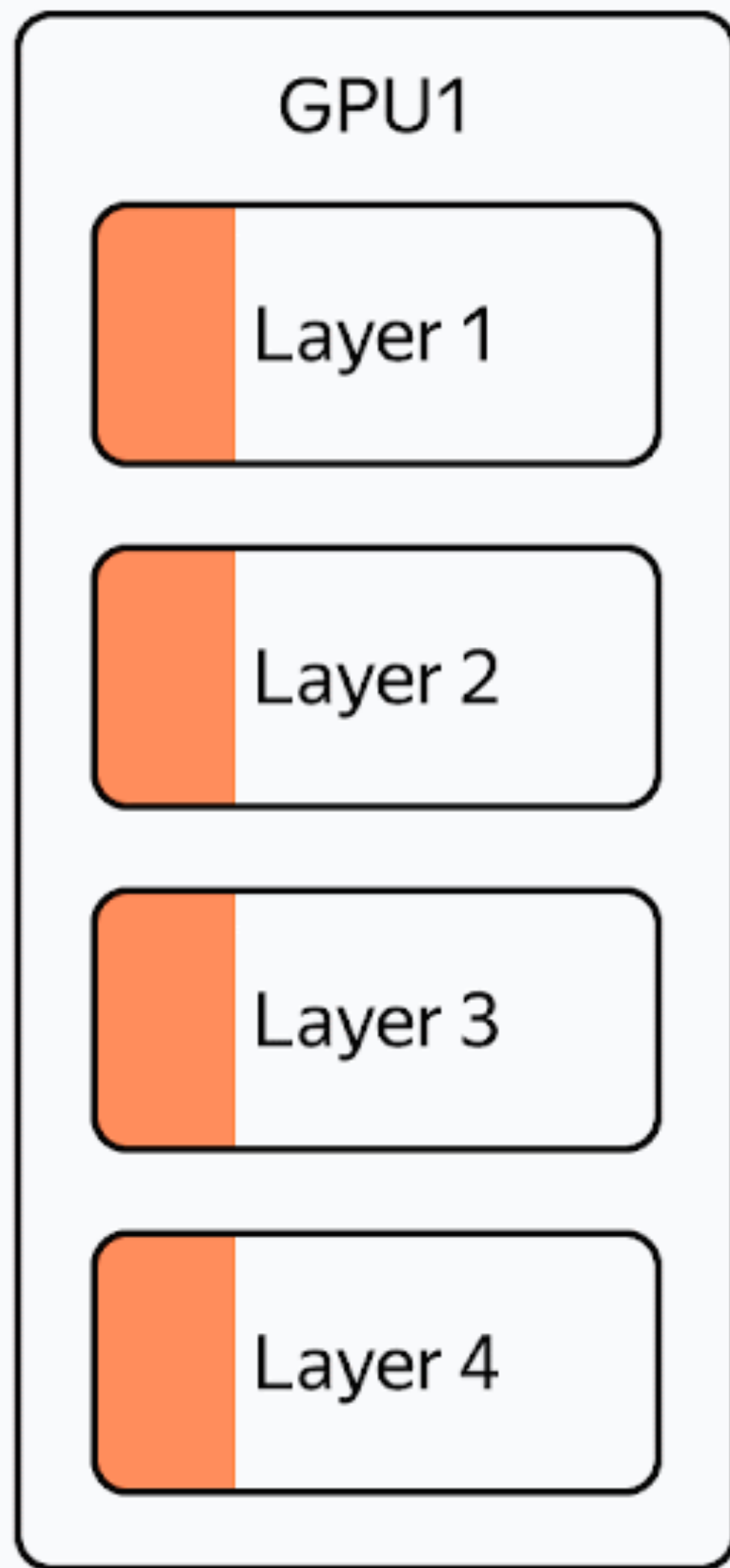
- FSDP tries to simulate DDP, but since each GPU only has access to a shard of the units, we have to **all-gather** a unit that we need for current part of the forward/backward pass
- Let's look at an example:

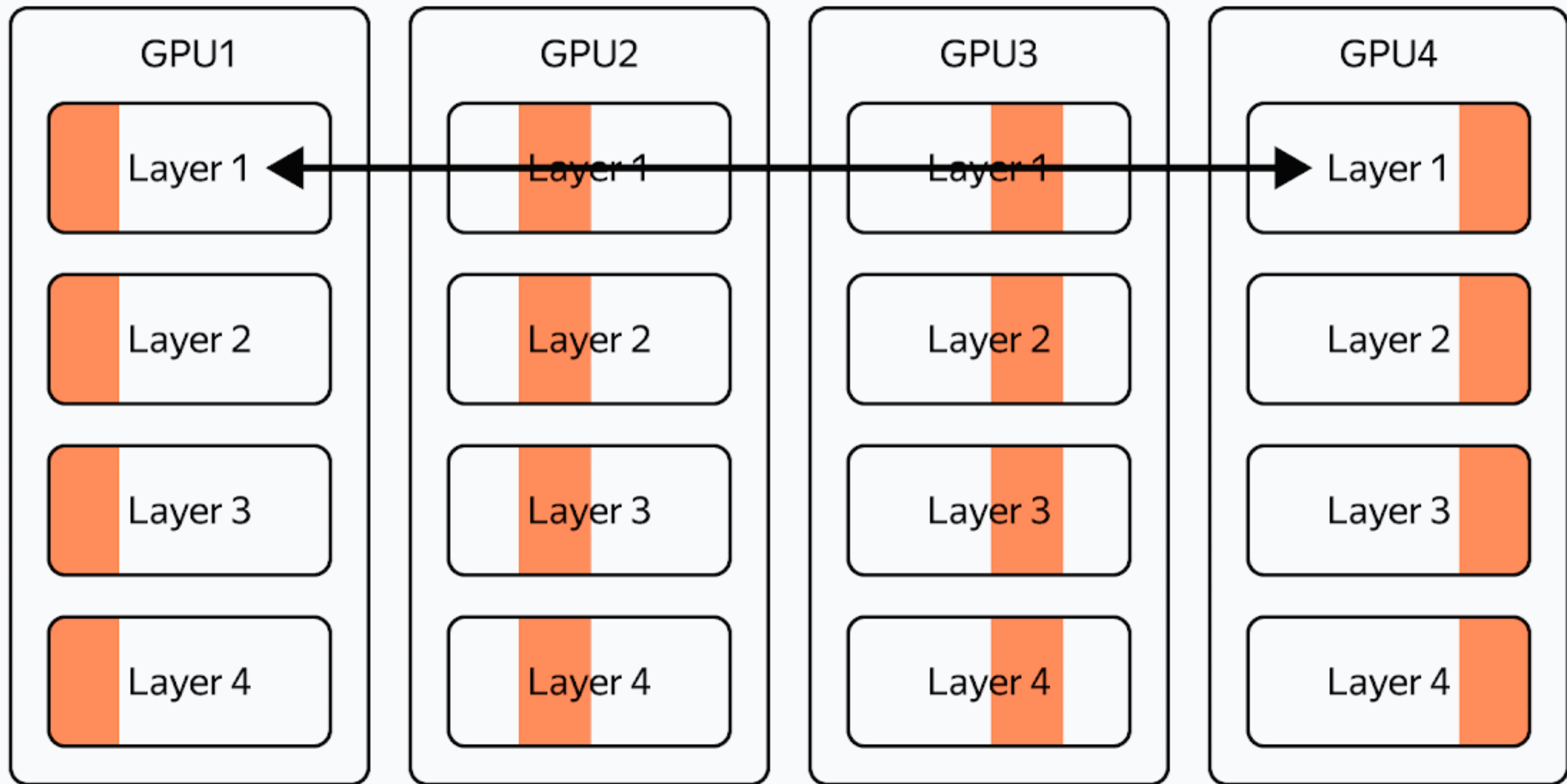


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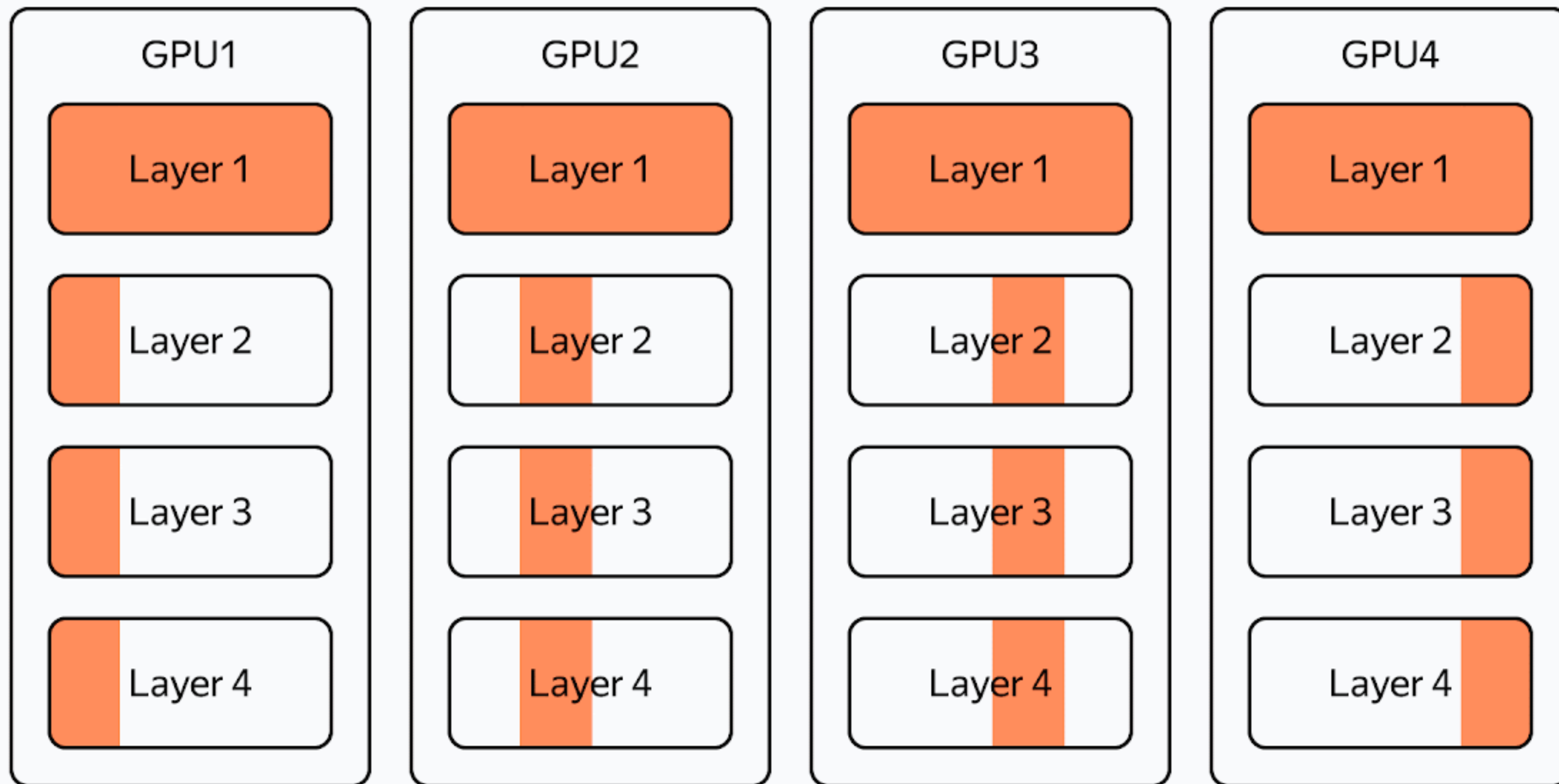
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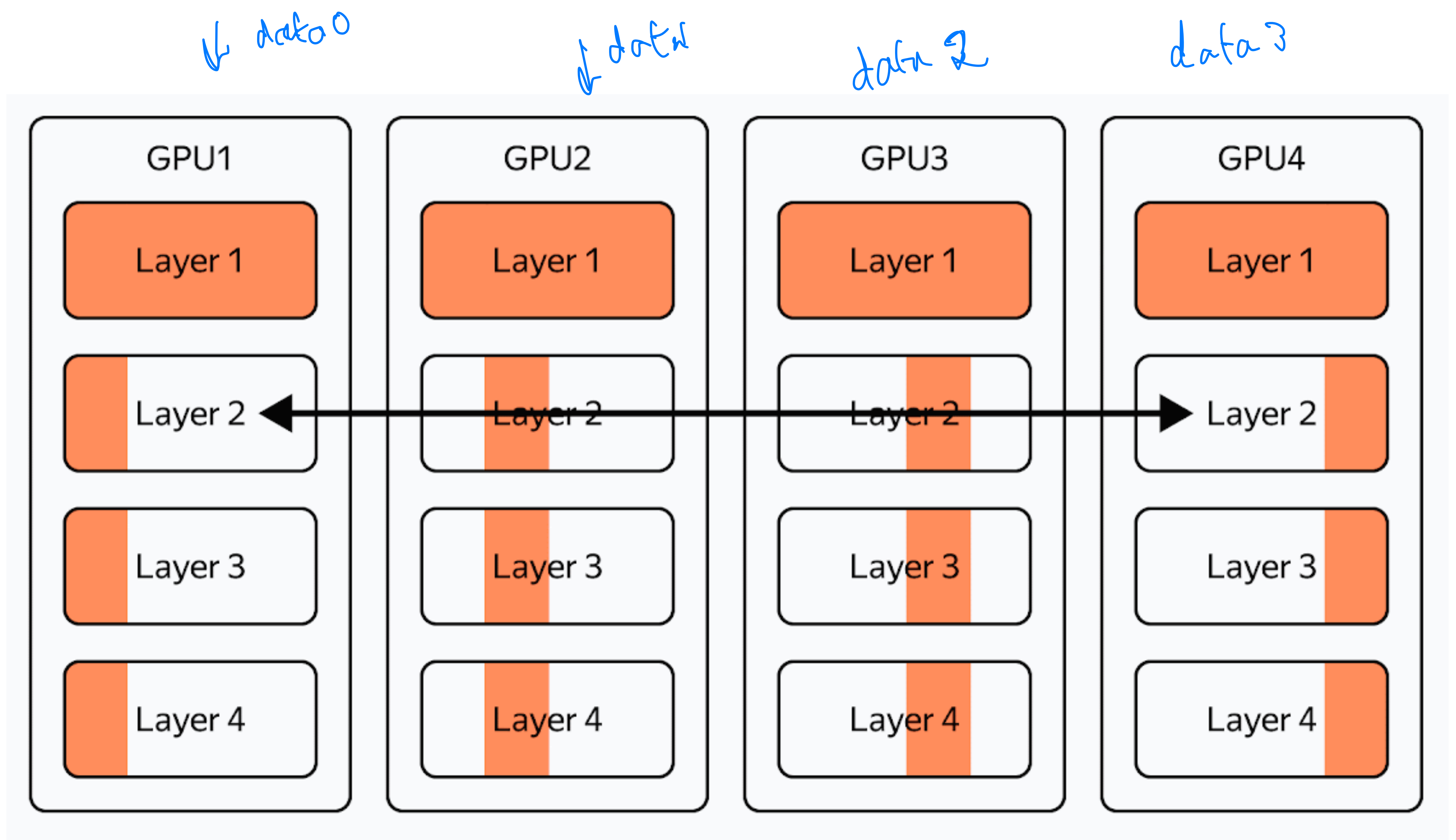




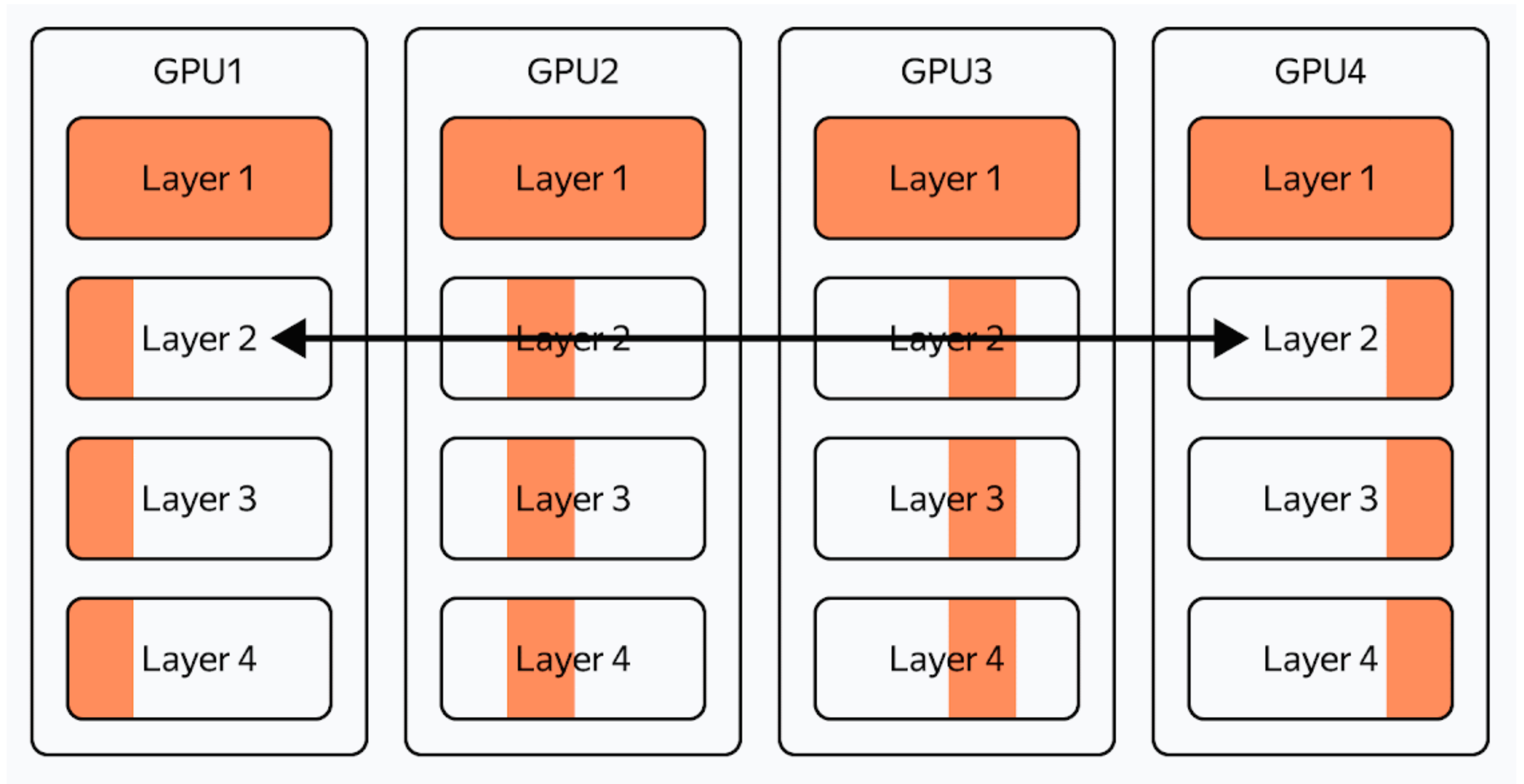


↔ = All-Gather

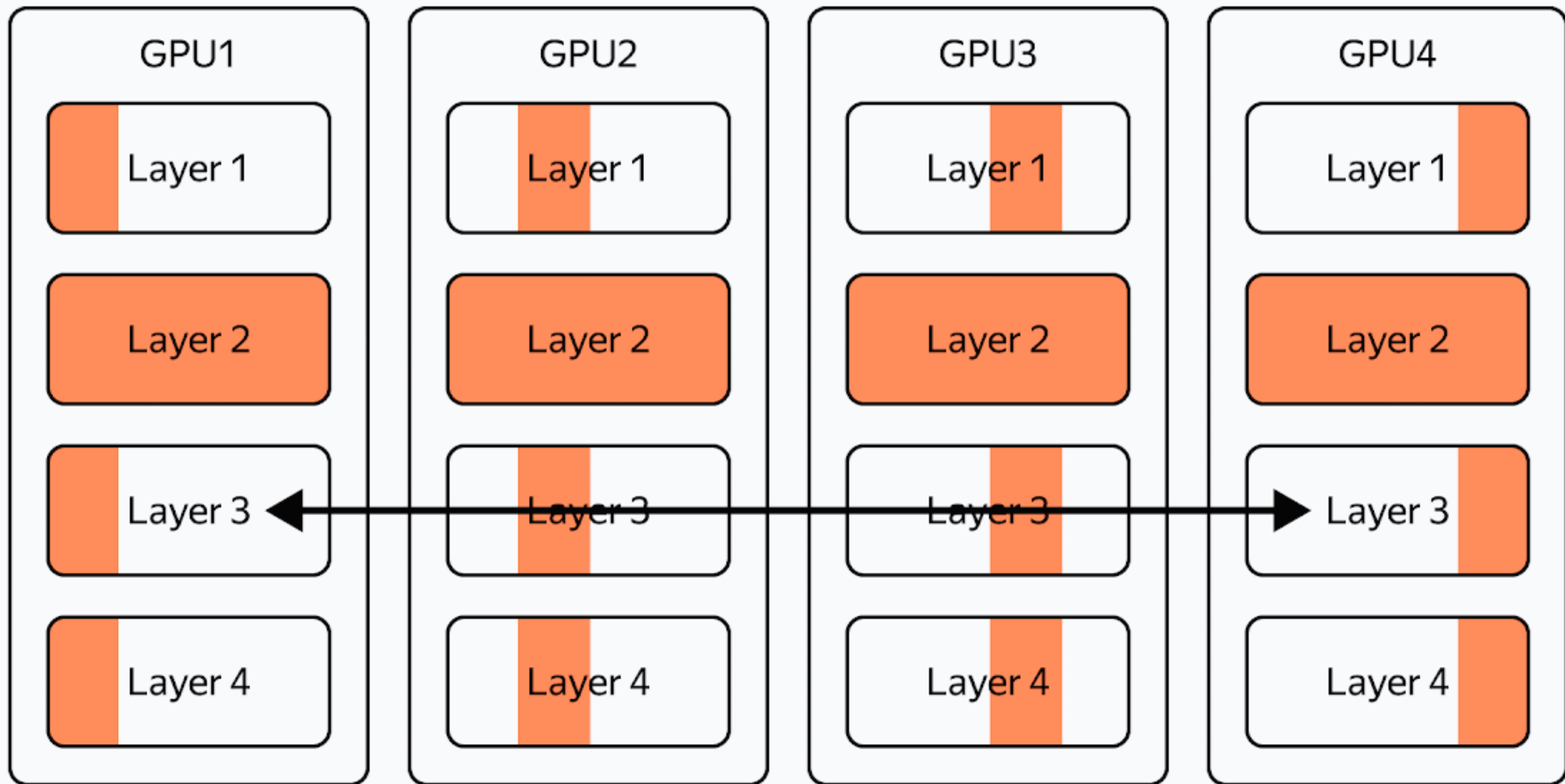


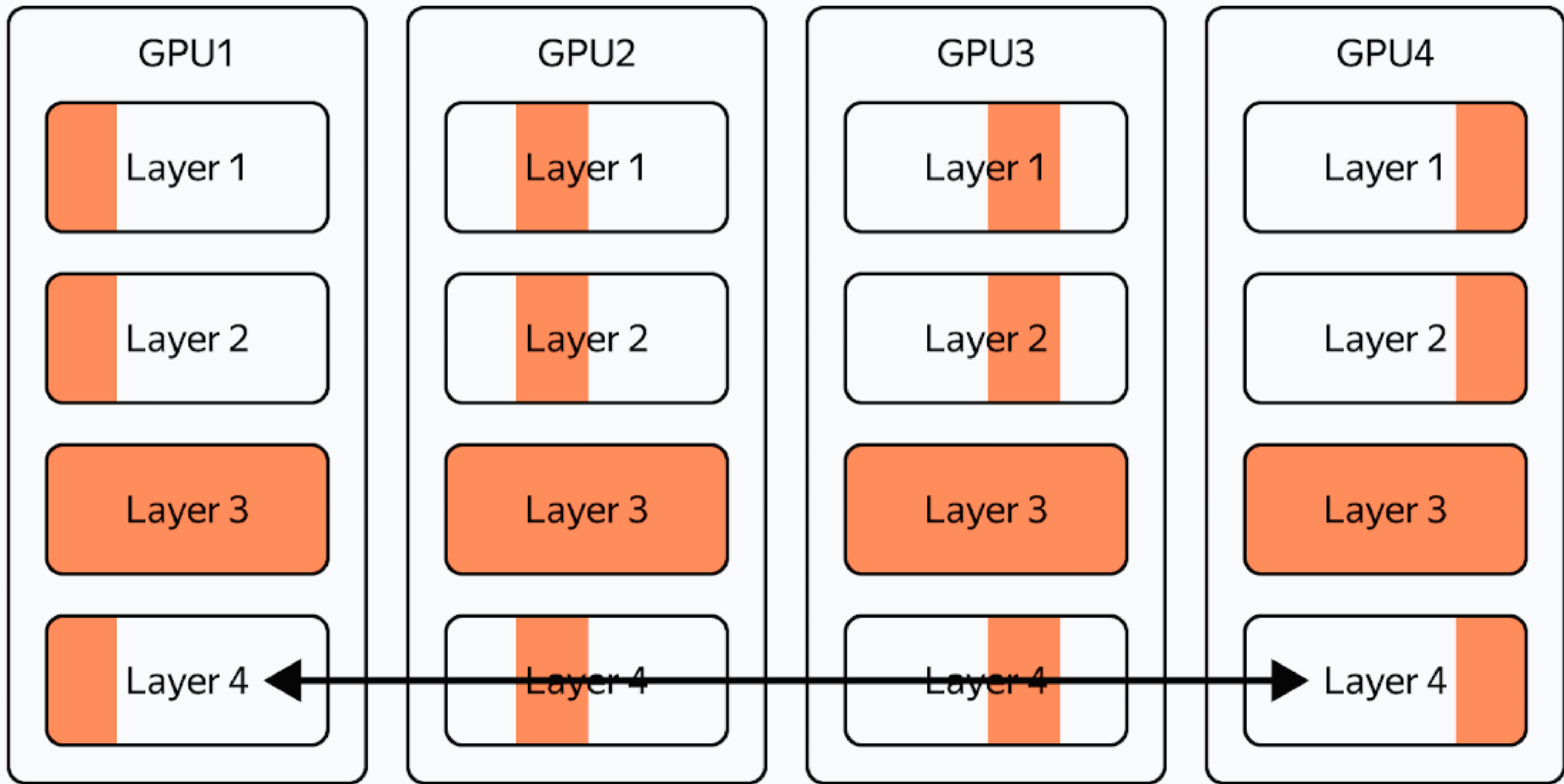


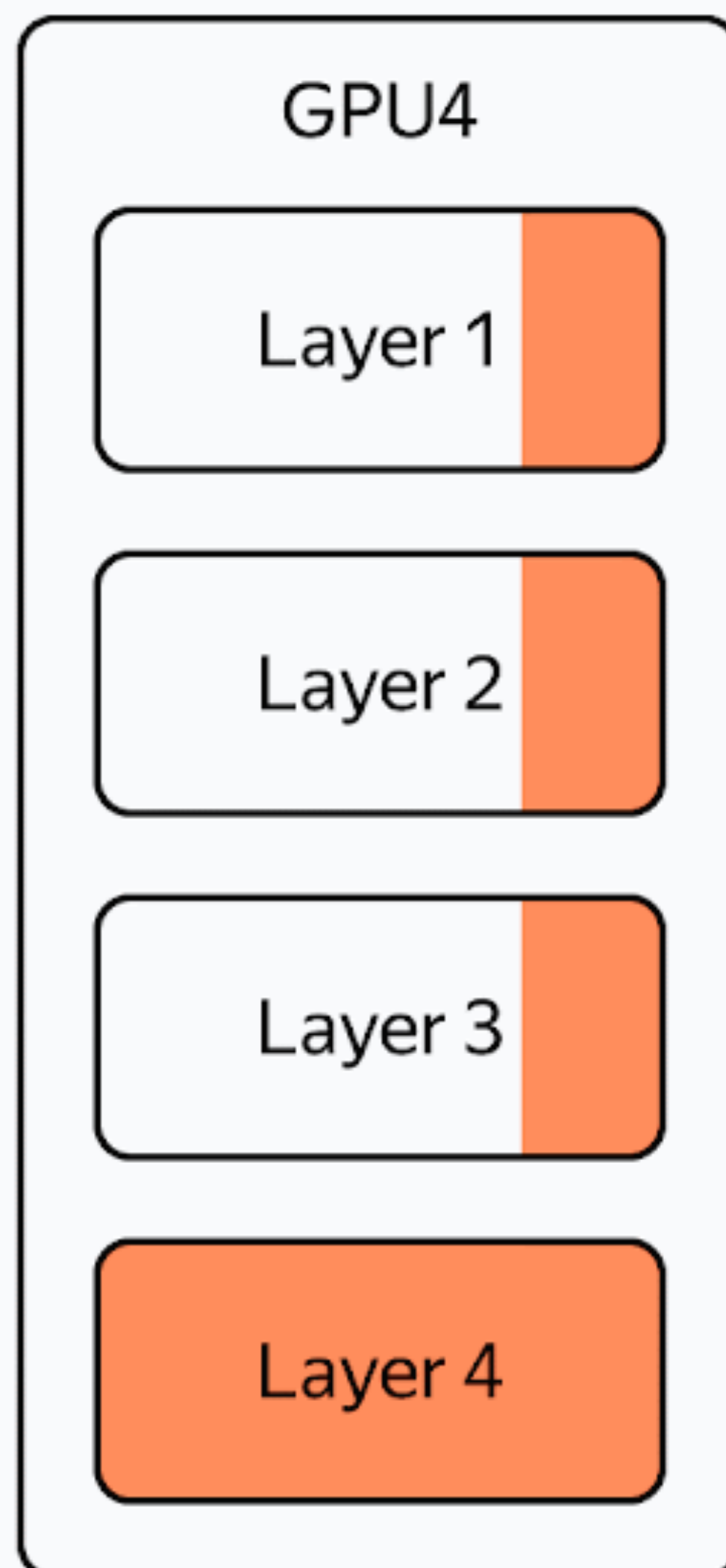
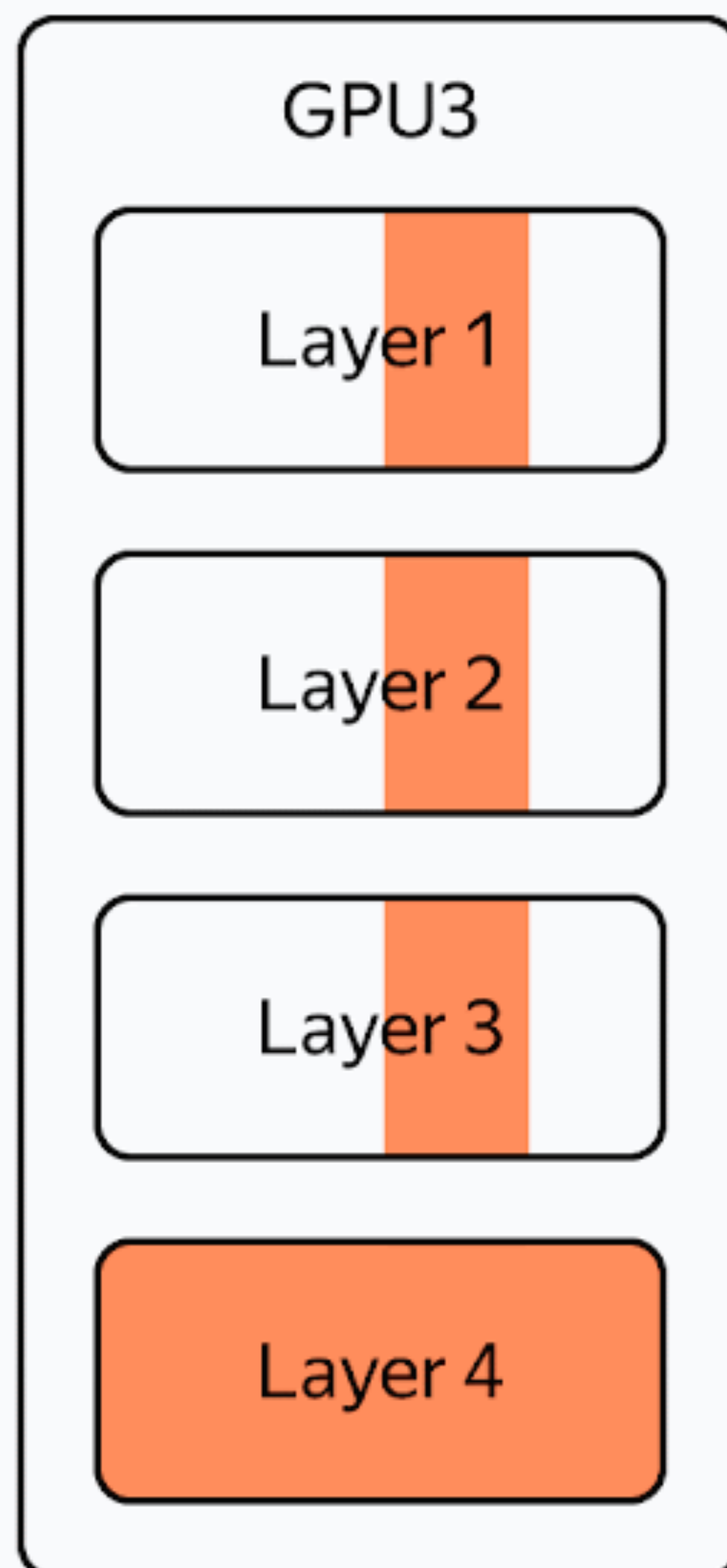
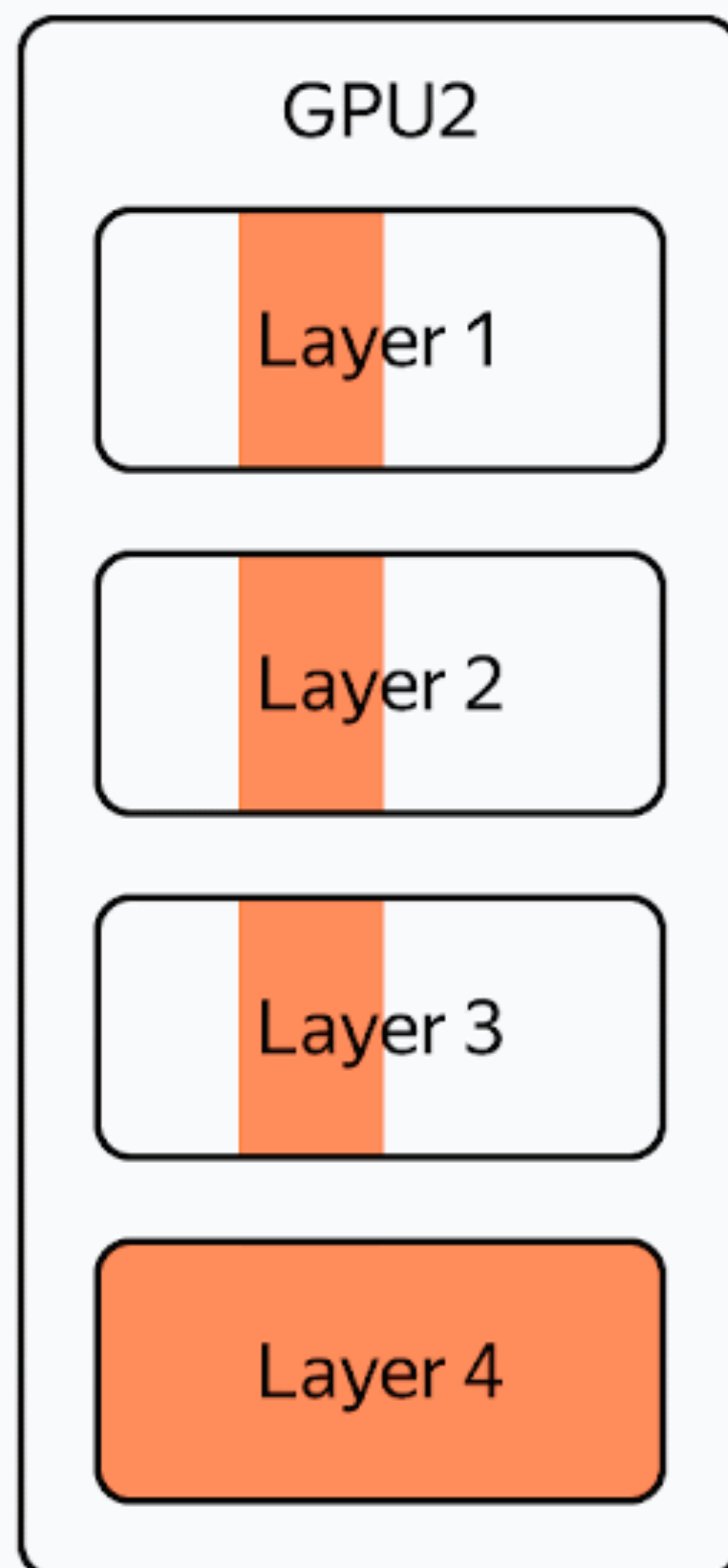
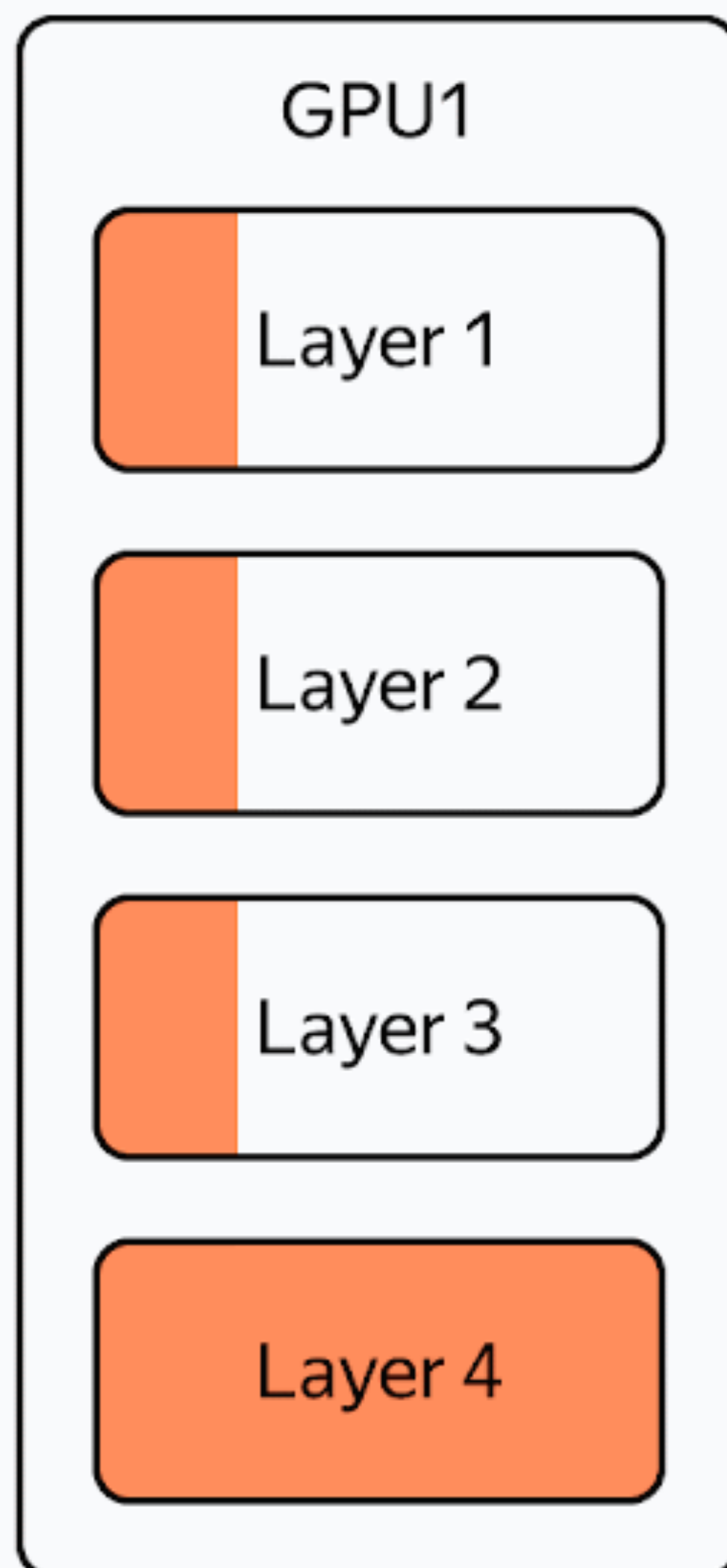
All-Gather later 2 while doing forward for Layer 1 (**communication/compute overlap**)

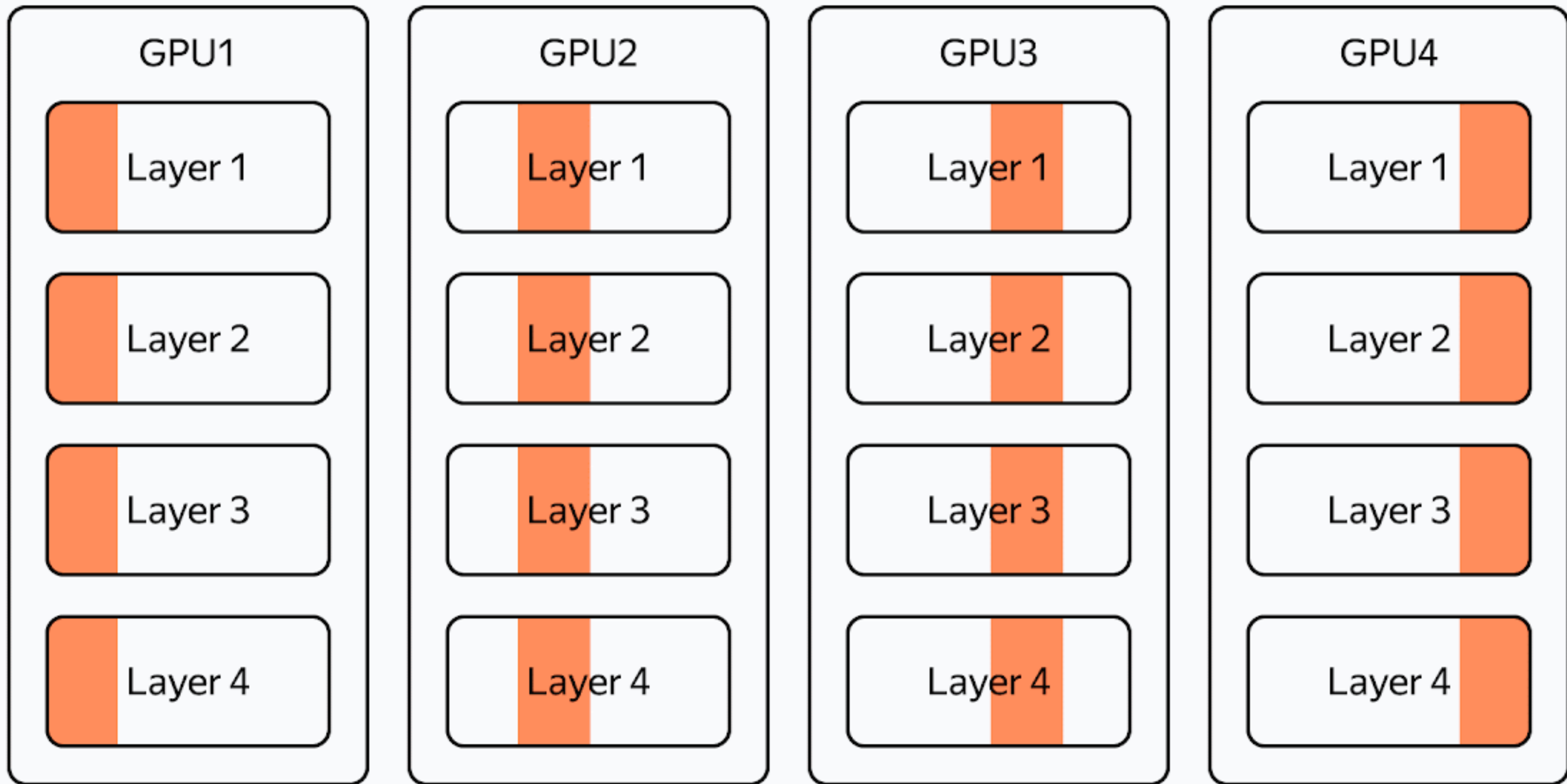


Clear layer 1 when done









And then do backwards pass!

FSDP Implementation

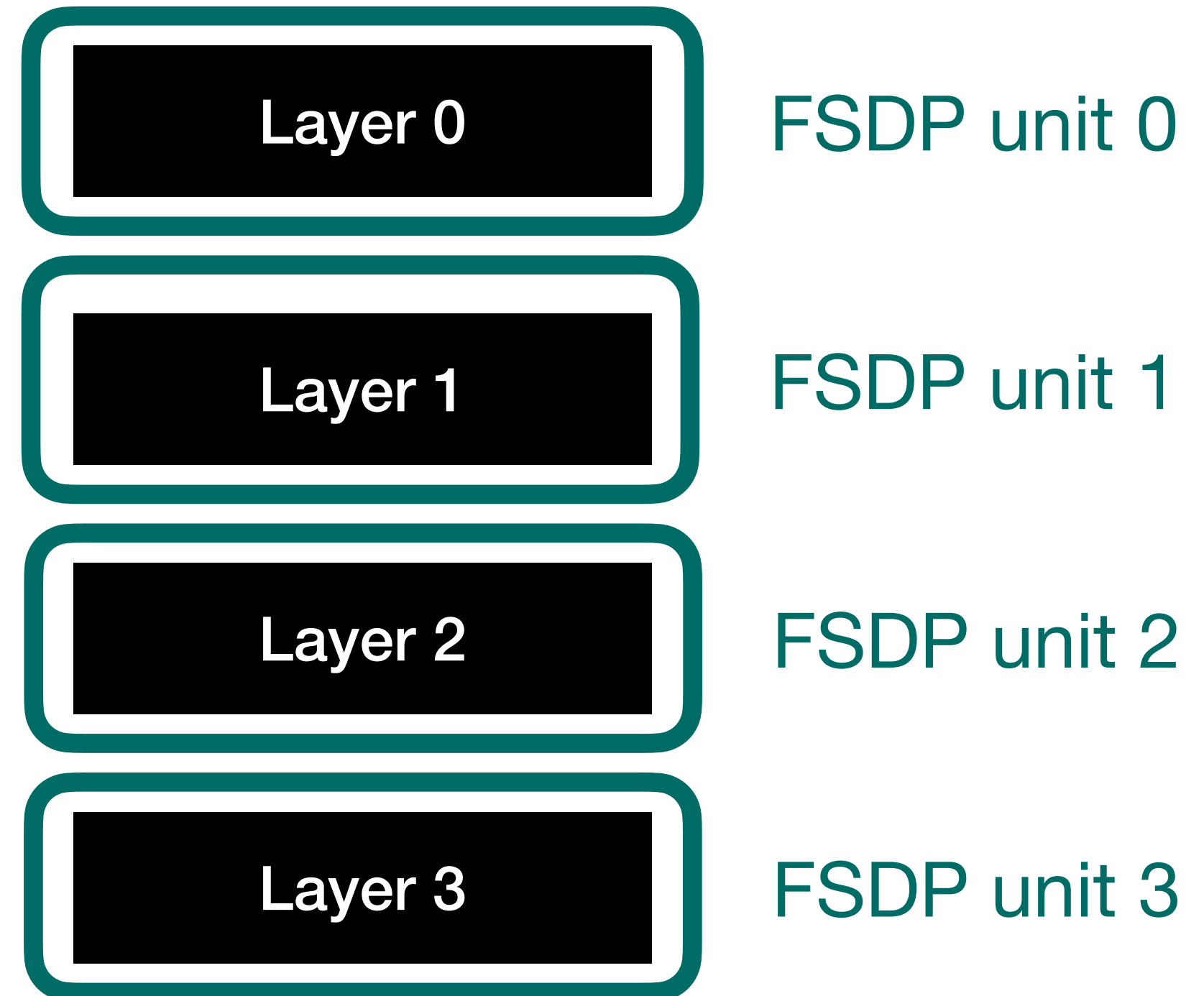
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FSDP forward pass:  
  for unit_i in units:  
    all-gather full weights for unit_i  
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    save activations for unit_i  
    discard full weights for unit_i
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FSDP backward pass:  
  for unit_i in units:  
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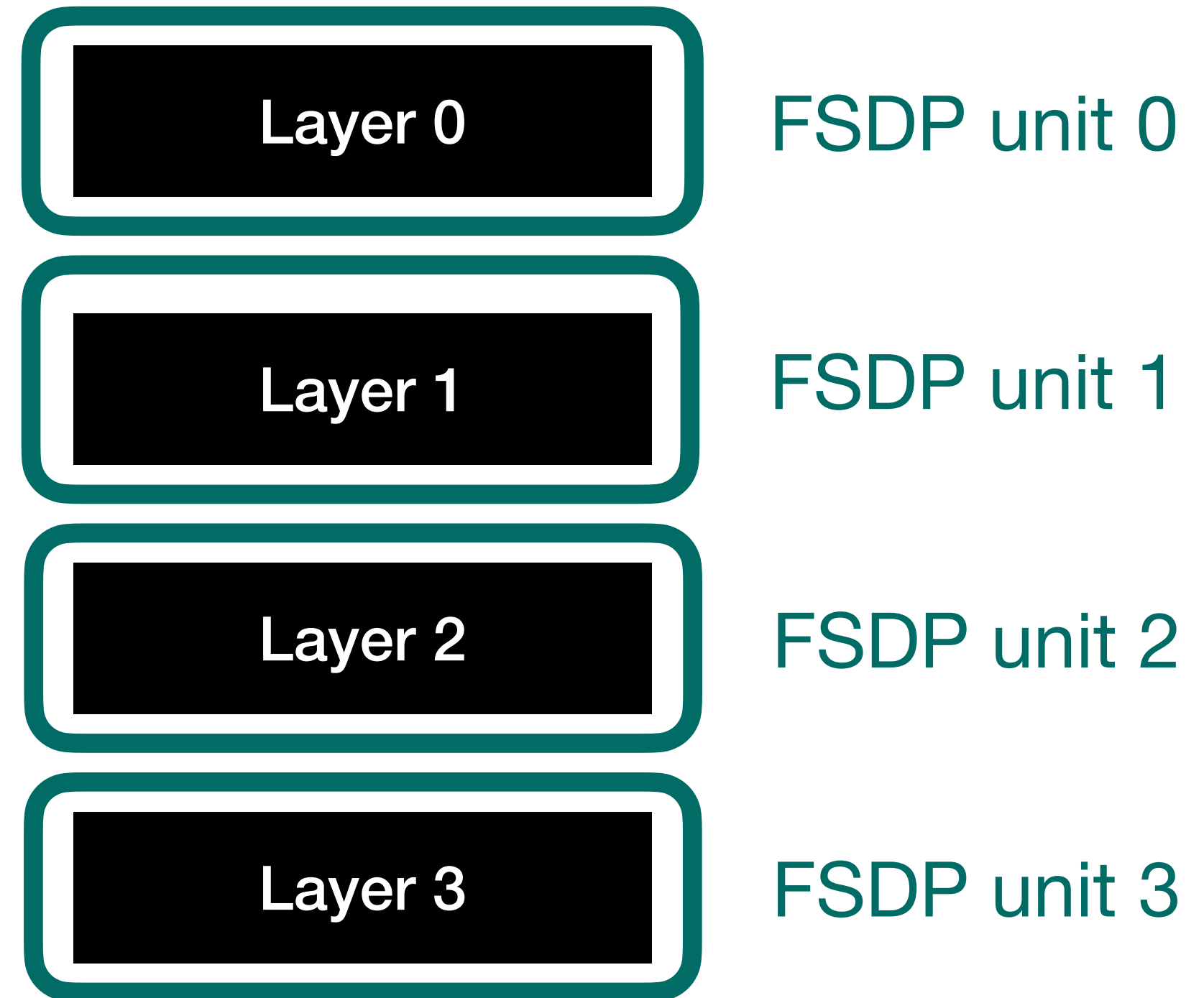
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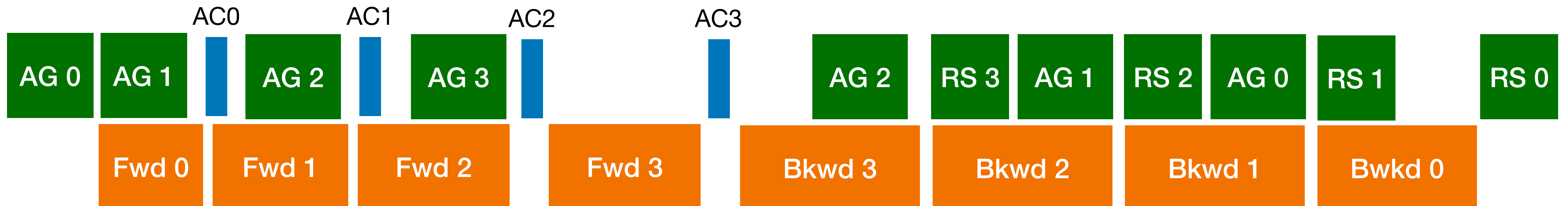
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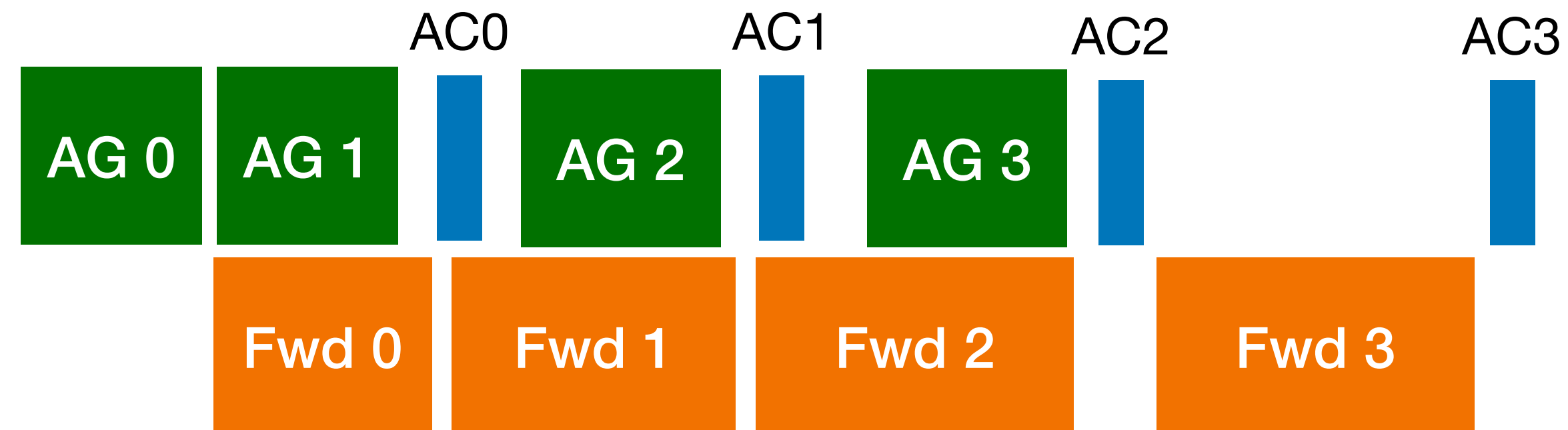
AG = all-gather, AC = activation checkpoint, RS = reduce-scatter



Computation vs communication overlaps

Cartoon is idealized setup. How much can we actually overlap?

Let's assume FSDP units are layers and we're looking at the forward pass for now



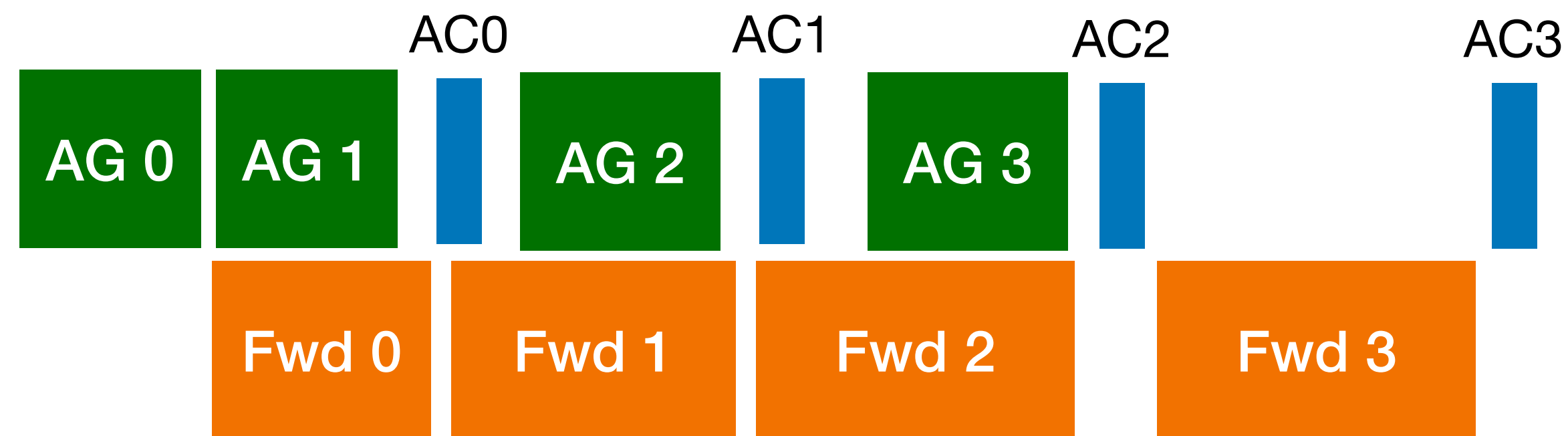
In theory, we are bottlenecked only when it takes longer to AG the next layer than computing the forward pass on the layer before it. When does this happen?

Today

- Recap++:
- Pipeline Parallelism
- FSDP
- ✓ • Theoretical Considerations
- Tensor Parallelism

Computation vs communication overlaps

In theory, we are bottlenecked only when it takes longer to all-gather the next layer than computing the forward pass on the layer before it



$$T^{\ell+1}_{\text{all-gather}} \geq T^{\ell}_{\text{forward}}$$

All-gather Time

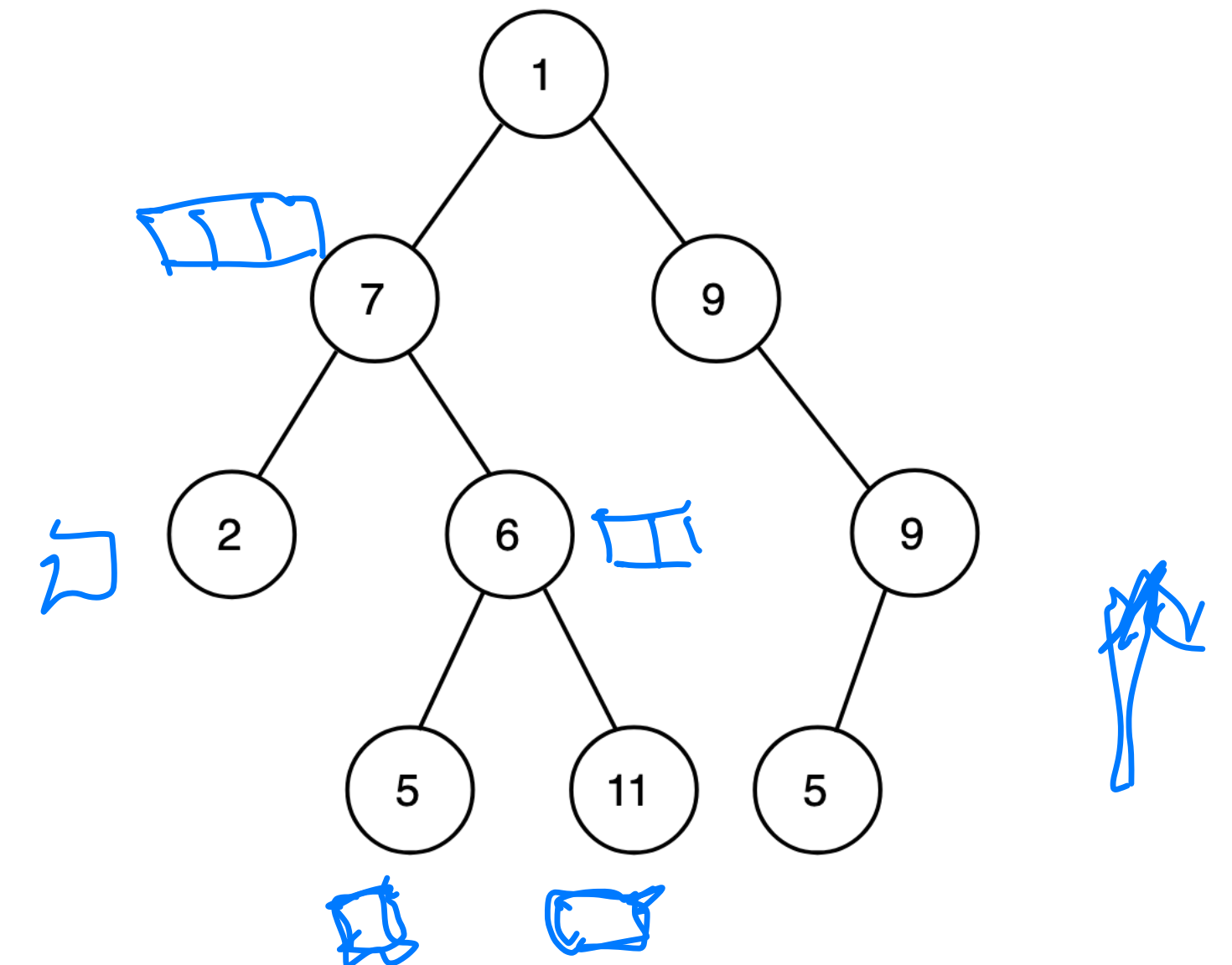
$$T_{\text{all-gather}} = \alpha \log p + \frac{1}{\beta} p N_{\text{message}}$$

α is startup latency to send a message, β is bandwidth,

p is number GPUs/nodes (11 in picture),

N_{message} is the size of the message/tensor to send (stored on nodes)

(in our setting, there are two different β 's (for intra/inter, i.e. gpu/nodes))



Handwritten notes in blue ink:

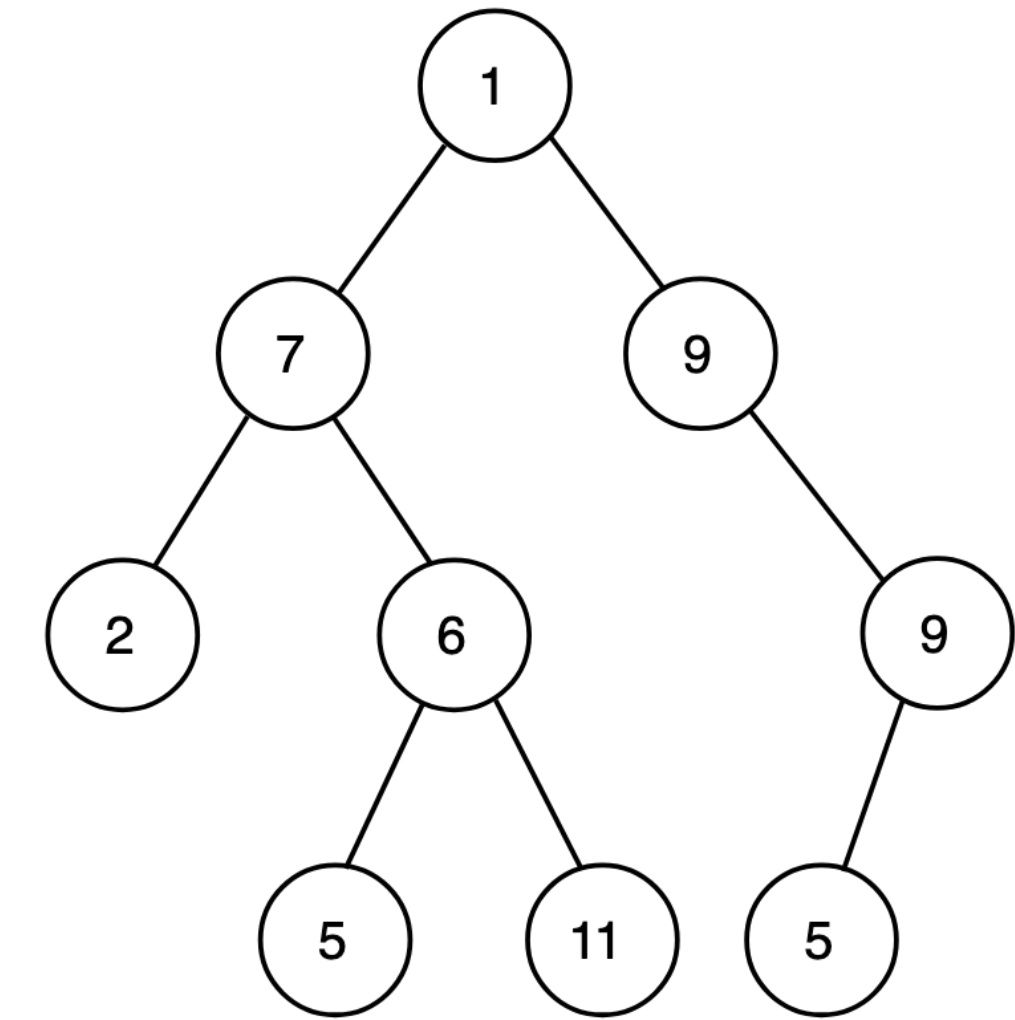
$$\sum_{i=0}^{\log p} (2^{i+1} \alpha)$$

Arrows point from the notes to the equation above and to the term $\alpha \log p$ in the main equation.

Below the notes, the terms pN and $\alpha \log p$ are written.

All-gather Time

$$T_{\text{all-gather}} = \alpha \log p + \frac{1}{\beta} p N_{\text{message}}$$



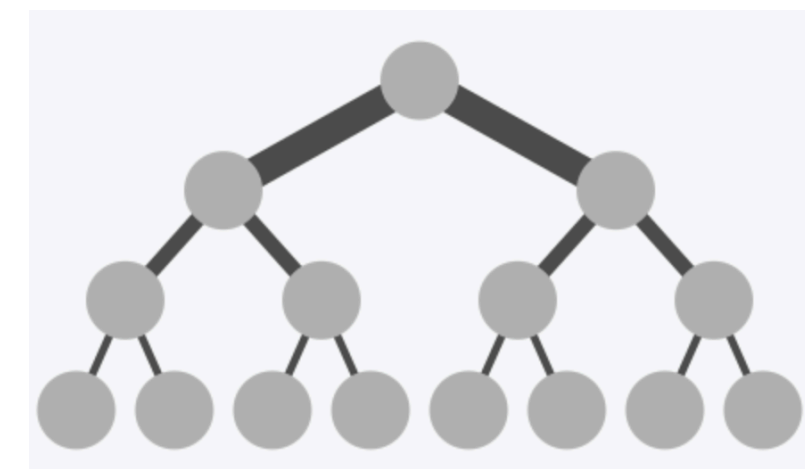
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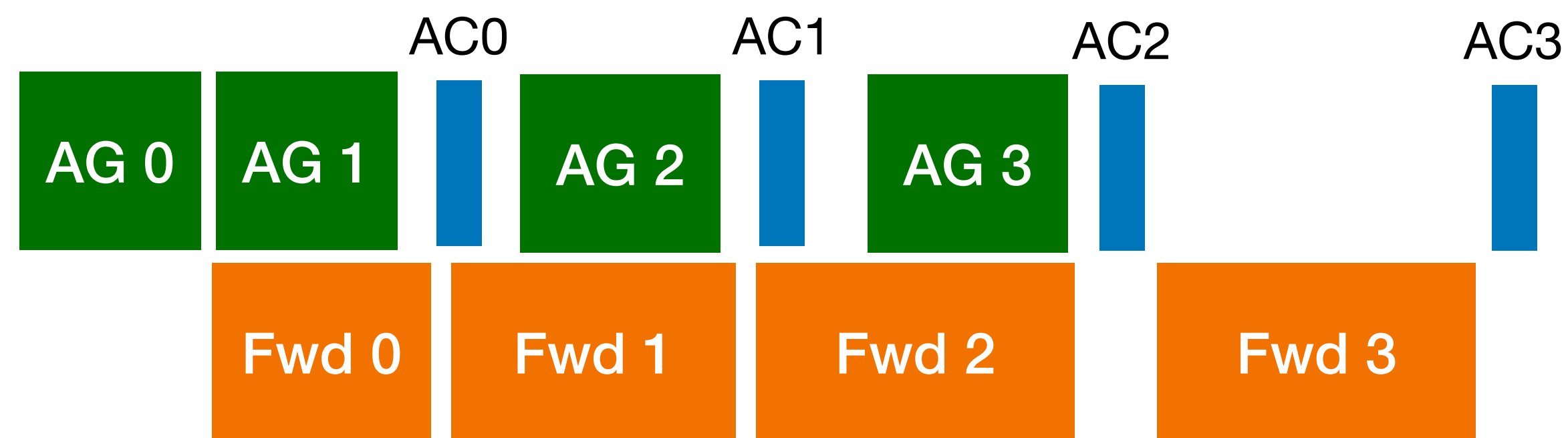
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Note: Nvidia uses “fat tree”



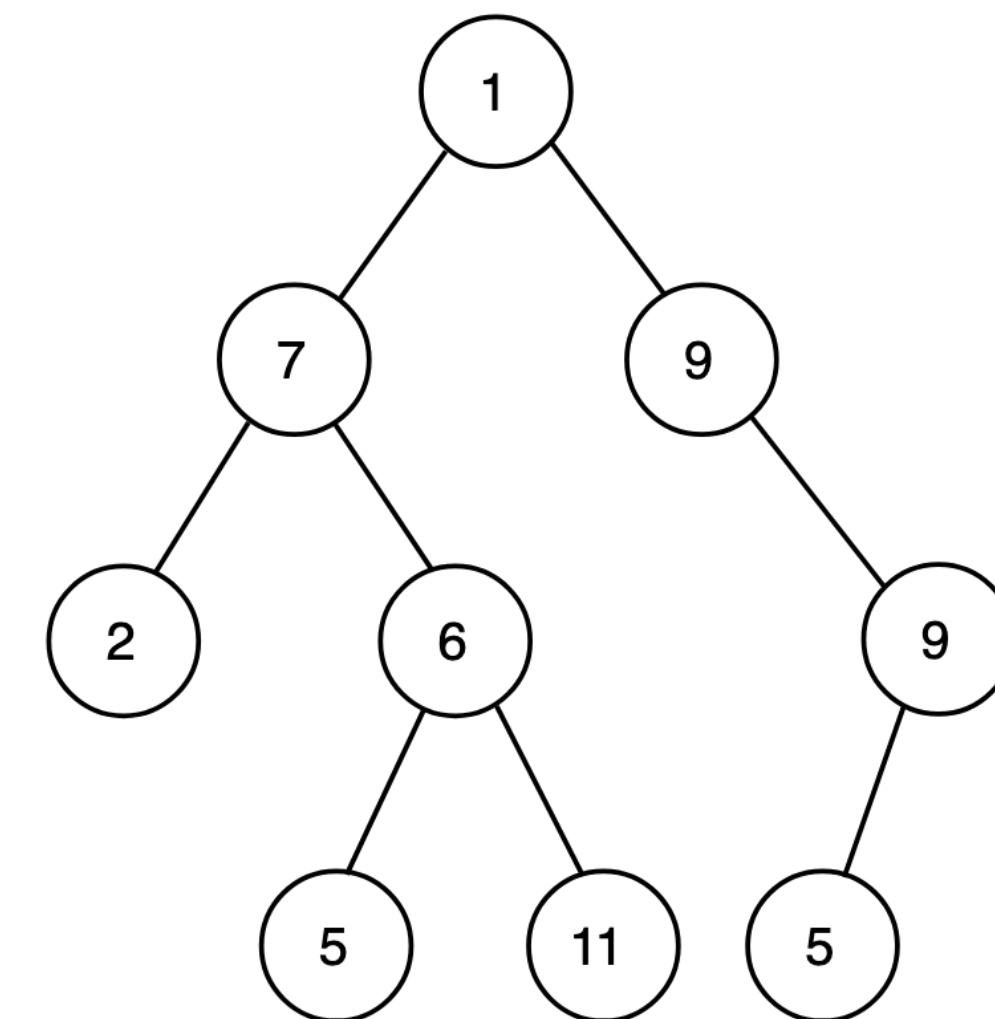
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Comm bound when $T^{\ell+1}_{\text{all-gather}} \geq T^{\ell}_{\text{forward}}$

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$$T^{\ell+1}_{\text{all-gather}} = \alpha \log p + \frac{1}{\beta} n$$

We set things up so that:

$$p N_{\text{message}} = n$$

α is startup latency to send a message, β is bandwidth, p is number GPUs, N_{message} is the size of the message/tensor to send, and n is num params per layer

Computation vs communication overlaps

Comm bound when $T^{\ell+1}_{\text{all-gather}} \geq T^{\ell}_{\text{forward}}$

$$T^{\ell+1}_{\text{all-gather}} = \alpha \log p + \frac{1}{\beta} n$$

$$T^{\ell}_{\text{forward}} = \frac{BSn}{C}$$

$$\alpha \log p + \frac{1}{\beta} n \geq \frac{BSn}{C} - \frac{L}{\beta} n$$

Batch size B , seq length S ,
FLOPs/GPU C

α is startup latency to send a message, β is bandwidth, p is number GPUs,
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Computation vs communication overlaps

$$\alpha \log p \leq \left(\frac{BS}{C} - \frac{1}{\beta} \right) n$$

Batch size B , seq length S ,
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Effectively balancing compute per parameter with how quickly those parameters can be communicated!

Note: if the model needs to fit across nodes, β is **internode** bandwidth which is >> bandwidth within a node

Numbers for inter and intranode

$$\alpha \log p \leq \left(\frac{BS}{C} - \frac{1}{\beta} \right) n$$

Inter (between nodes)

$$\alpha = 10^{-6} \text{ s}$$

$$\beta = 50 \text{ GB/s}$$

$$C = 1500 \text{ TFLOP/s}$$

$$S = 8 \times 10^3$$

$$\frac{1}{\beta} = 2 \times 10^{-11} \text{ s/byte}$$

$$\approx 2 \text{ ns/GB}$$

Intra (within a node)

$$\alpha = 10^{-6} \text{ s}$$

$$\beta = 1 \text{ TB/s}$$

$$C = 1500 \text{ TFLOP/s}$$

$$S = 8 \times 10^3$$

$$\frac{1}{\beta} = 1 \times 10^{-12} \text{ s/byte}$$

$$\approx 1 \text{ ps/GB}$$

$B \approx 10$

$$BS = \left(\frac{10^5}{1500 \times 10^6} - \frac{2}{8 \times 10^3} \right)$$

$$\approx 10^{-11} - 10^{-11}$$

Scaling FSDP: where does it break?

$$\alpha \log p \leq \left(\frac{BS}{C} - \frac{1}{\beta} \right) n$$

Batch size B , seq length S ,
FLOPs/GPU C

α is startup latency to send a message, β is
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params per layer

$$p \leq 2^{\alpha(-)} \rightarrow 0$$

→ **Also:** if the right hand side is “non-trivially” positive, then we can make p very large!
(so where does **FSDP** break?)

For internode: batch size $O(10)$ is needed but note that we have to have enough
memory to keep the activations around (which also grows with batch size)!

What about TPUs?

$$\alpha \log p \leq \left(\frac{BS}{C} - \frac{1}{\beta} \right) n$$

For TPUs, β is absurdly large

The following table shows the key chip specifications and their values for v5e.

Key chip specifications	v5e values
Peak compute per chip (bf16)	197 TFLOPs
HBM2 capacity and bandwidth	16 GB, 819 GBps
Interchip Interconnect BW	1600 Gbps

The following table shows Pod specifications and their values for v5e.

Key Pod specifications	v5e values
TPU Pod size	256 chips
Interconnect topology	2D Torus
Peak compute per Pod	100 PetaOps(Int8)
All-reduce bandwidth per Pod	51.2 TB/s
Bisection bandwidth per Pod	1.6 TB/s
Data center network bandwidth per Pod	6.4 Tbps

More generally,

$$\alpha \log p \leq \left(\frac{BS}{C} - \frac{1}{\beta} \right) n$$

Batch size B , seq length S ,
FLOPs/GPU C

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$$\alpha \log p \leq \left(\frac{B \cdot \text{compute_per_param}}{C} - \frac{1}{\beta} \right) n$$

What is the “unit”: here, we basically want the unit to be “small”, which gives us more flexibility (in TP, we will subdivide the layer)

More generally,

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Pipeline approach:

- We are communicating both the activations and the params (in the backward pass).
- Exactly the same issue as in FSDP. Bottlenecks inter-node communication.

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- Here, we can effectively make d bigger due to sharding the layer within a node (larger β)
- But, we can't keep increasing the depth (or width) due to both model and activation memory in the node

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FSDP+pipeline:

- Use FSDP to make the intra-node model larger
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Many mix-match approaches

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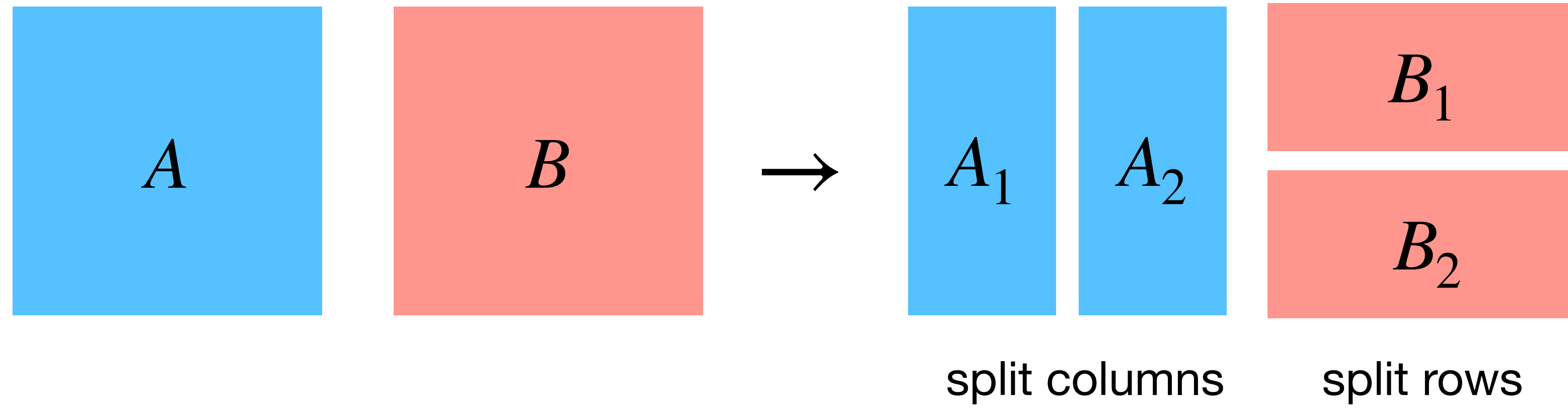
Linear Network: $Y = ABX$

- Where A, B are both $d \times d$ and X is $d \times m$.

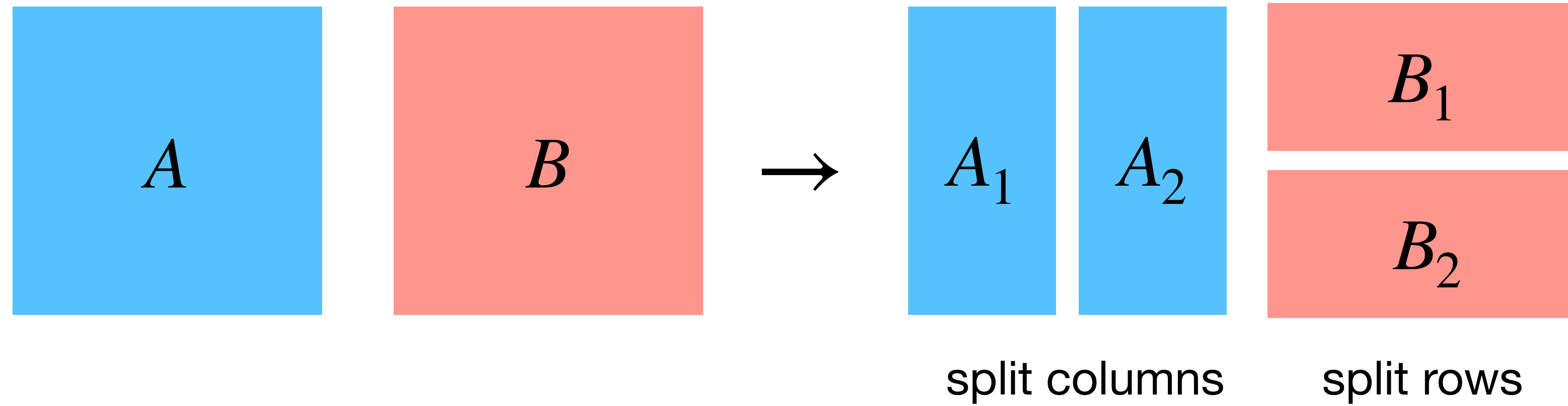
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Linear Network: $Y = ABX$
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- We will consider d to be large so that we want to break up A, B matrices.

The Basic Idea

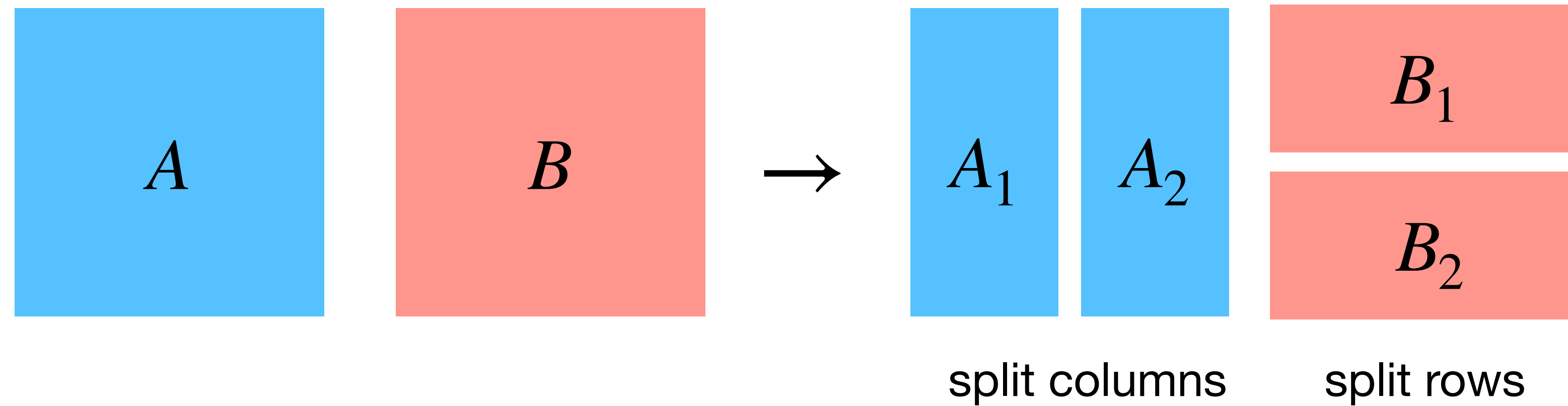


The Basic Idea



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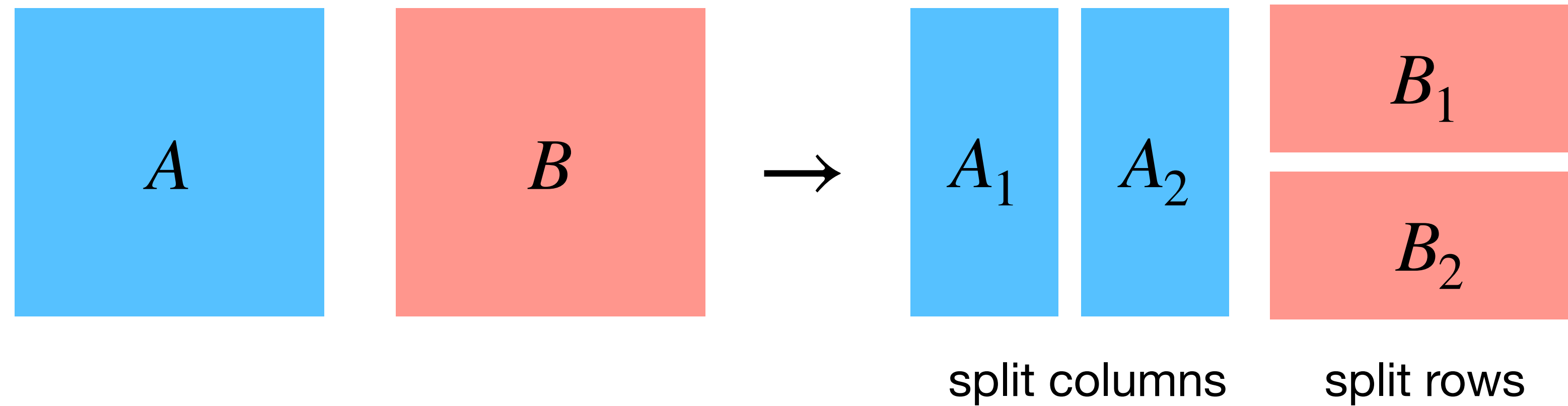


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$$AB = A_1B_1 + A_2B_2$$

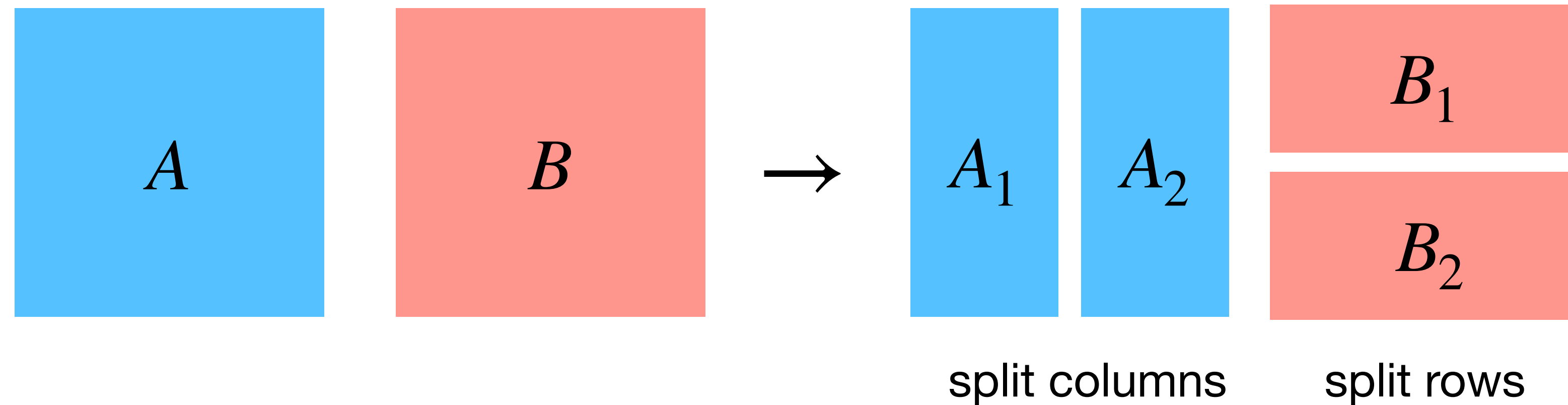
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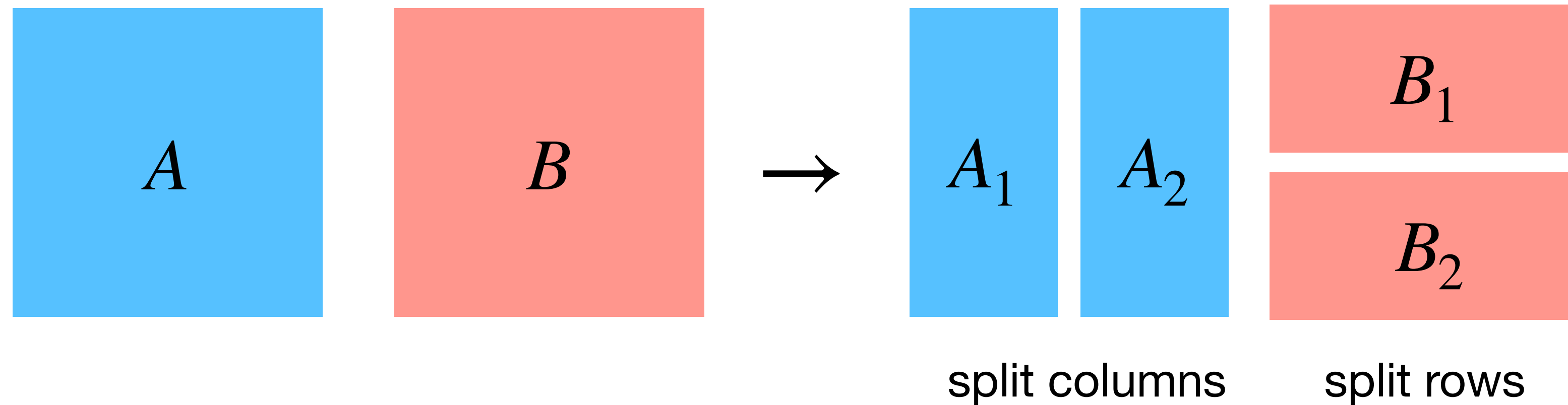
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gpu 1: holds A_1, B_1, X ,

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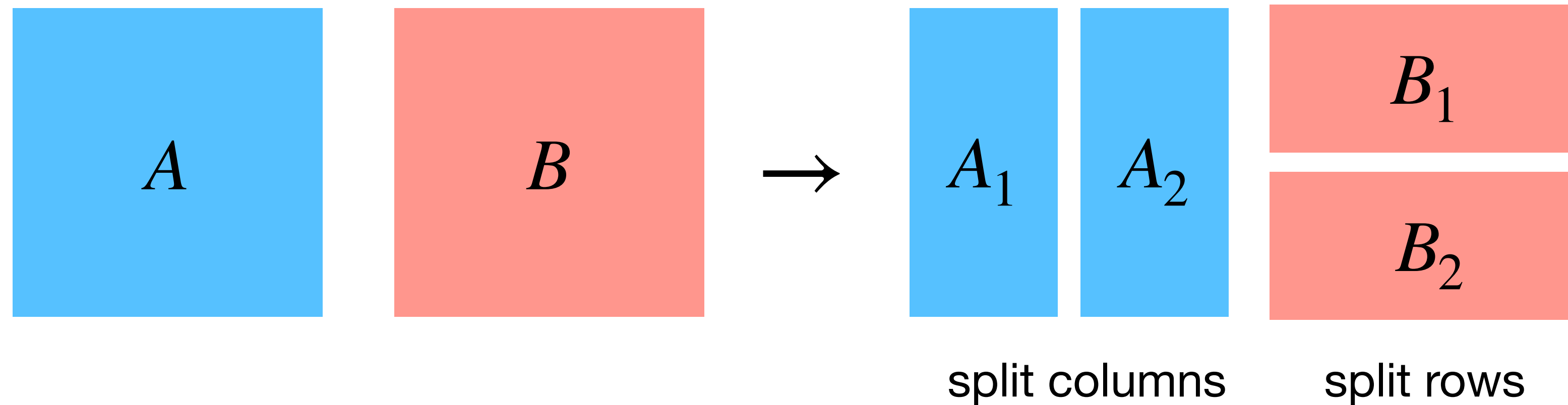
gpu 2: holds A_2, B_2, X

- Each device computes:

$$y_1 = A_1B_1X$$

$$y_2 = A_2B_2X$$

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gpu 2: holds A_2, B_2, X

- Each device computes:

$$y_1 = A_1B_1X$$

$$y_2 = A_2B_2X$$

- **All-reduce** the y 's:

$$Y = y_1 + y_2$$

Discussion

More general considerations and scalings:

$$\alpha \log p \leq \left(\frac{B \cdot \text{compute_per_param}}{C} - \frac{1}{\beta} \right) n$$

α is startup latency to send a message, β is bandwidth, p is number GPUs, n is num params per layer

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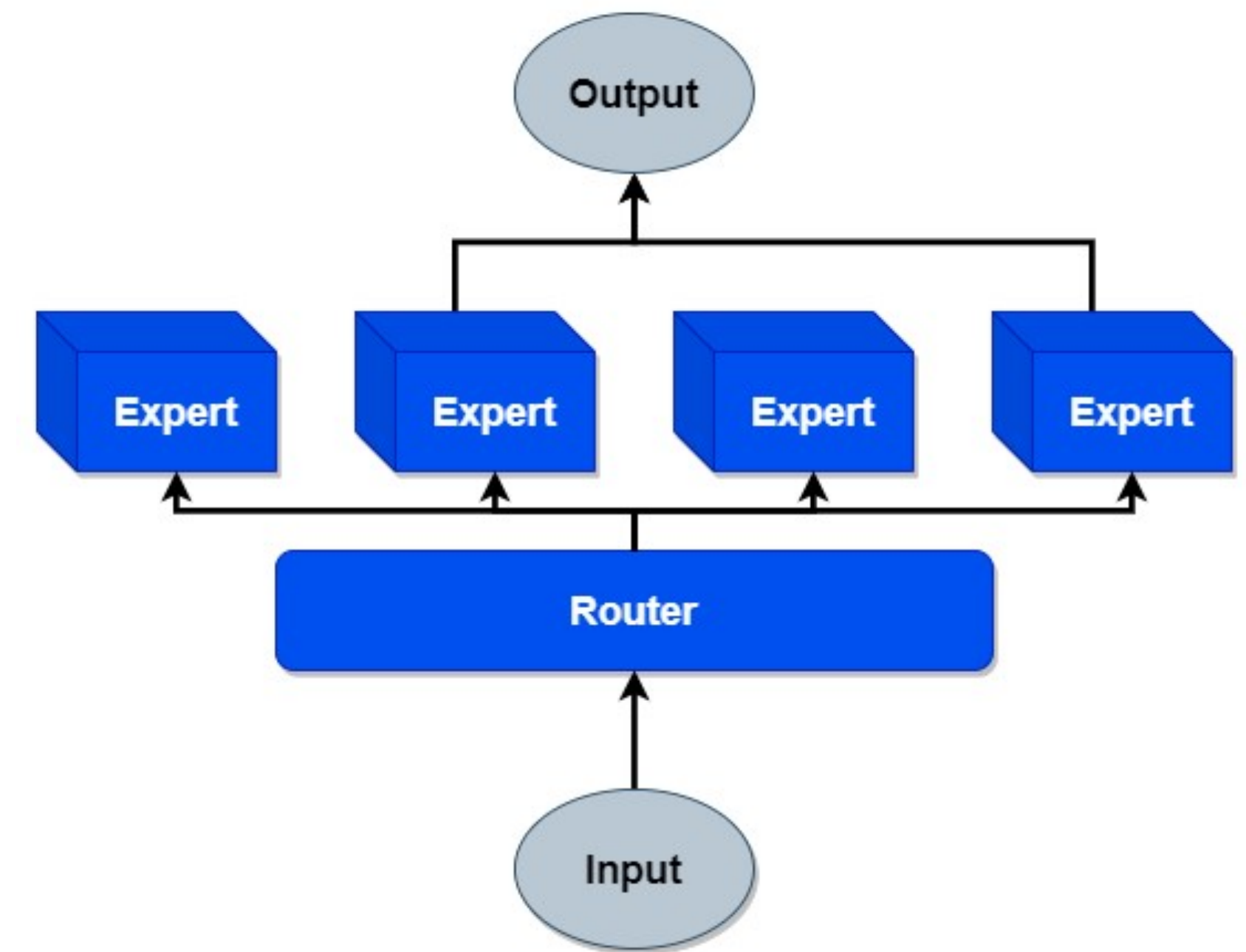
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- **Mixture of Experts:** Different compute_par_param scaling



GPUs	TP	CP	PP	DP	Seq. Len.	Batch size/DP	Tokens/Batch	TFLOPs/GPU	BF16 MFU
8,192	8	1	16	64	8,192	32	16M	430	43%
16,384	8	1	16	128	8,192	16	16M	400	41%
16,384	8	16	16	4	131,072	16	16M	380	38%

Table 4 Scaling configurations and MFU for each stage of Llama 3 405B pre-training. See text and Figure 5 for descriptions of each type of parallelism.

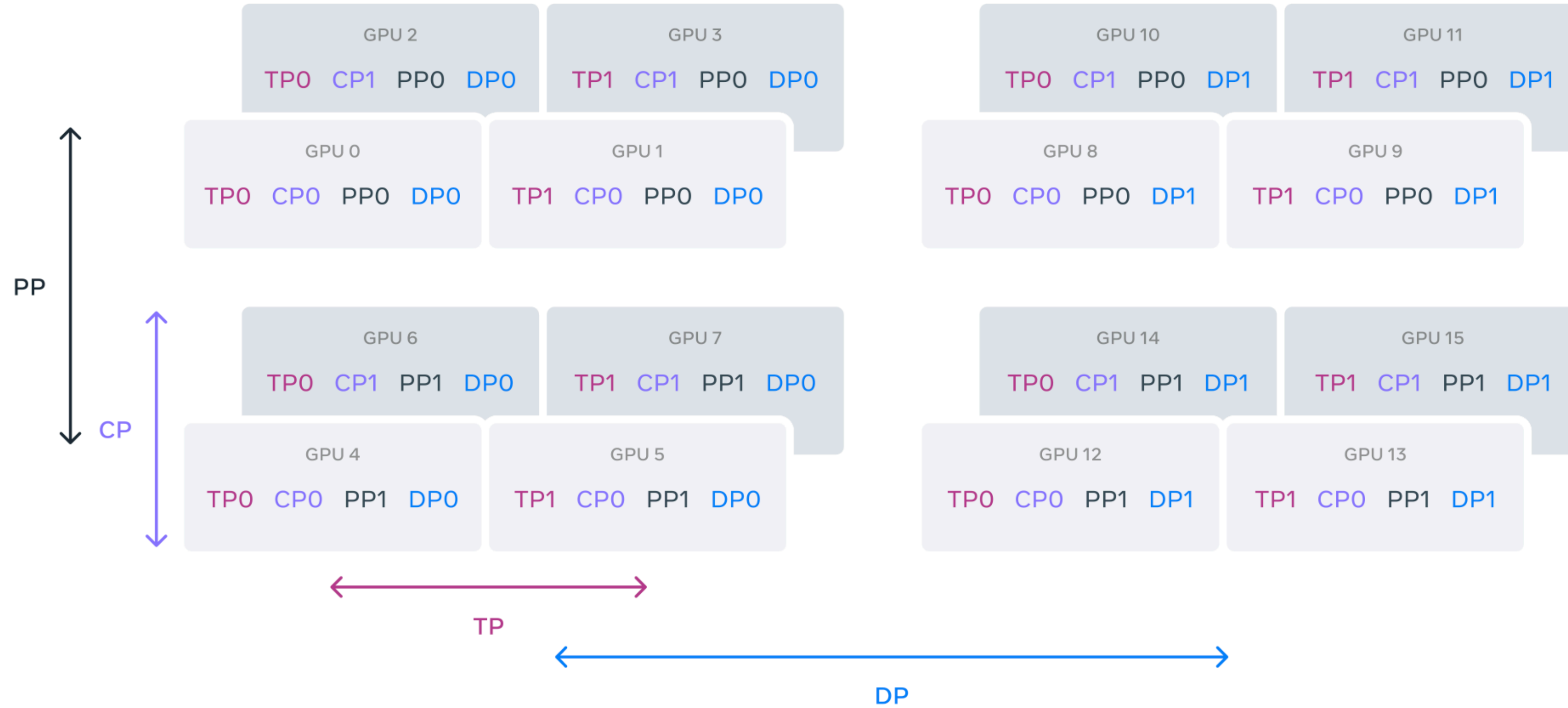


Figure 5 Illustration of 4D parallelism. GPUs are divided into parallelism groups in the order of [TP, CP, PP, DP], where DP stands for FSDP. In this example, 16 GPUs are configured with a group size of $|TP|=2$, $|CP|=2$, $|PP|=2$, and $|DP|=2$. A GPU's position in 4D parallelism is represented as a vector, $[D_1, D_2, D_3, D_4]$, where D_i is the index on the i -th parallelism dimension. In this example, GPU0[TP0, CP0, PP0, DP0] and GPU1[TP1, CP0, PP0, DP0] are in the same TP group, GPU0 and GPU2 are in the same CP group, GPU0 and GPU4 are in the same PP group, and GPU0 and GPU8 are in the same DP group.

Thanks!

1. Lots of parallelization approaches.
2. communication to compute ratio is important!