

Imitation Learning & Behavioral Cloning

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**CS/Stat 184: Introduction to Reinforcement Learning
Fall 2023**

Today



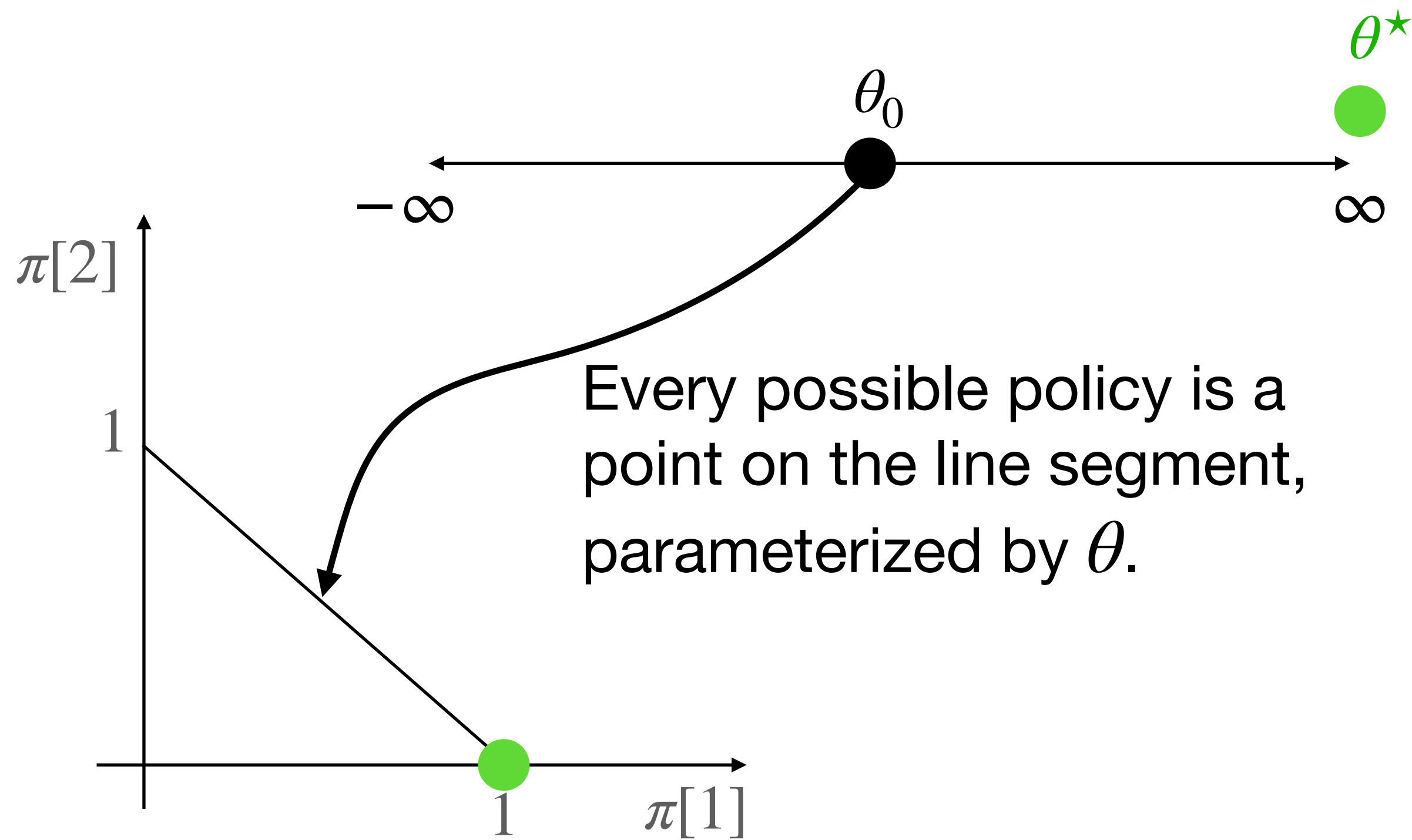
- Recap++
- Imitation Learning:
 - Behavioral Cloning
 - DAgger

Recap

Example of Natural Gradient on 1-d problem: 2 actions, 1 state

$$(\pi_\theta[1], \pi_\theta[2]) := \left(\frac{\exp(\theta)}{1 + \exp(\theta)}, \frac{1}{1 + \exp(\theta)} \right)$$

$$J(\theta) = 100 \cdot \pi_\theta[1] + 1 \cdot \pi_\theta[2]$$



$$\text{Gradient: } J'(\theta) = \frac{99 \exp(\theta)}{(1 + \exp(\theta))^2}$$

$$\text{Exact PG: } \theta^{k+1} = \theta^k + \eta \frac{99 \exp(\theta^k)}{(1 + \exp(\theta^k))^2}$$

i.e., vanilla GA moves to $\theta = \infty$ with smaller and smaller steps, since $J'(\theta) \rightarrow 0$ as $\theta \rightarrow \infty$

$$\text{Fisher information scalar: } F_\theta = \frac{\exp(\theta)}{(1 + \exp(\theta))^2}$$

$$\text{NPG: } \theta^{k+1} = \theta^k + \eta \frac{J'(\theta^k)}{F_{\theta^k}} = \theta_k + \eta \cdot 99$$

NPG moves to $\theta = \infty$ much more quickly (for a fixed η)

Meta-Approach: CPI/TRPO/NPG/PPO are all pretty similar.

1. Init π_0

2. For $k = 0, \dots, K$:

$$\pi^{k+1} \approx \arg \max_{\theta} \Delta_k(\pi^{\theta}),$$

$$\text{where } \Delta_k(\pi) = \mathbb{E}_{s_0, \dots, s_{H-1} \sim \rho_{\pi^k}} \left[\sum_{h=0}^{H-1} \mathbb{E}_{a_h \sim \pi(s_h)} A^{\pi^k}(s_h, a_h) \right]$$

such that ρ_{θ} is “close” to ρ_{θ^k}

- **CPI**: conservative policy iteration

uses unconstrained optimization: $\tilde{\pi} \approx \arg \max_{\theta} \Delta_k(\pi^{\theta}),$

enforces closeness with “mixing”: $\pi^{k+1} = (1 - \alpha) \cdot \pi^k + \alpha \cdot \tilde{\pi}^{k+1}$

- **TRPO**: use KL to enforce closeness.
- **NPG**: is TRPO up to “leading order” (via Taylor’s theorem).
- **PPO**: uses a Lagrangian relaxation (i.e. regularization)

3. Return π_K

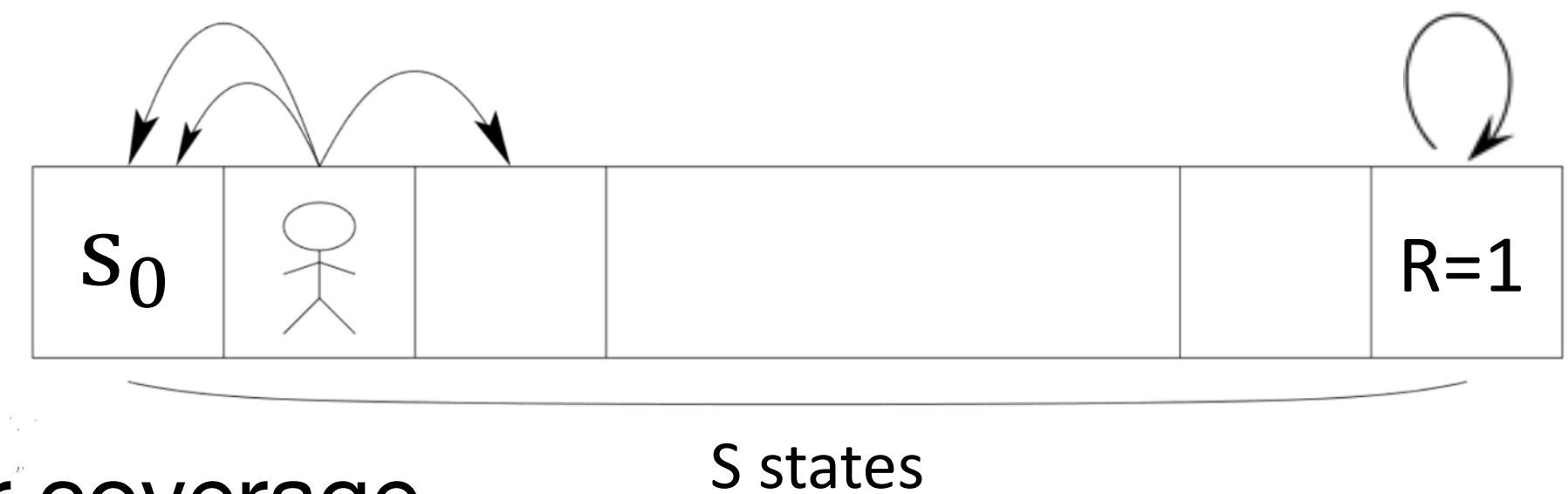
“Lack of Exploration” leads to Optimization and Statistical Challenges



Thrun '92

- Suppose $H \approx \text{poly}(|S|)$ & $\mu(s_0) = 1$ (i.e. we start at s_0).
- A randomly initialized policy π^0 has prob. $O(1/3^{|S|})$ of hitting the goal state in a trajectory.
- Implications:
 - The following sample based approach, with $\mu(s_0) = 1$, require $O(3^{|S|})$ trajectories.
 - Holds for (sample based) Fitted DP
 - Holds for (sample based) PG/CPI/TRPO/NPG/PPO
- Basically, for these approaches, we are stuck without exploration, if $\mu(s_0) = 1$.

Let's examine the role of μ



Thrun '92

- Suppose that somehow the distribution μ had better coverage.
 - e.g, μ was uniform over the all states in our toy problem, then all approaches we covered would work (with mild assumptions)
 - Theory: **CPI/TRPO/NPG/PPO have better guarantees than fitted DP methods** (assuming some “coverage”)
- **Strategies:**
 - If we have a simulator, sometimes we can **design μ to have better coverage.**
 - this is helpful for robustness as well.
 - **Imitation learning**
 - An expert gives us samples from a “good” μ .
 - **Explicit exploration:**
 - **UCB-VI:** we'll merge two good ideas!
 - Encourage exploration in PG methods.
 - Try with **reward shaping**

Today:

What about guarantees for PG methods? (vs fitted-DP methods)

- The hope is that if (average case) “supervised learning” worked, then RL would also work.

$$\pi_{\theta}(a | s) = \frac{\exp(\theta^{\top} \phi(s, a))}{\sum_{a'} \exp(\theta^{\top} \phi(s, a'))}$$

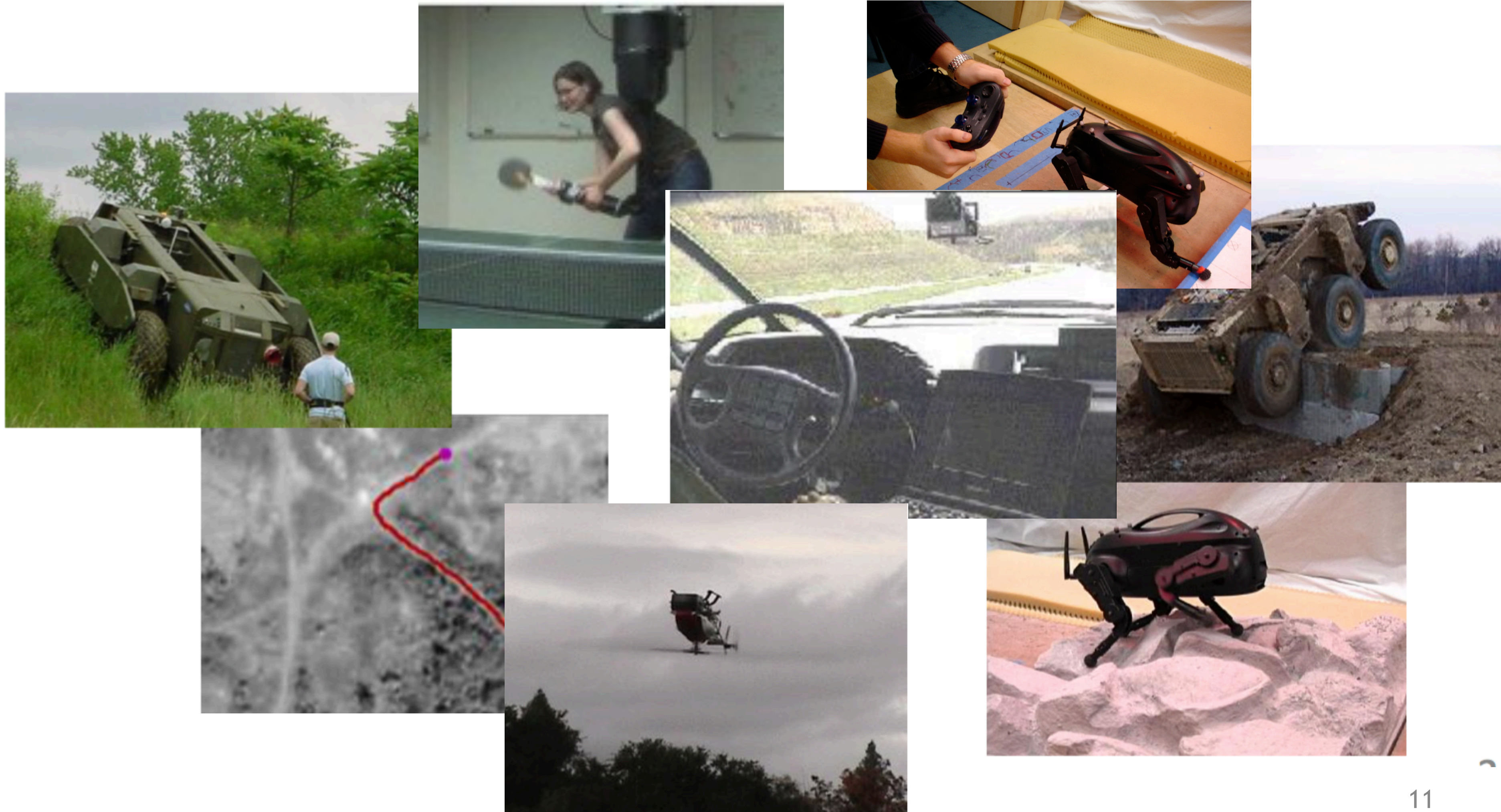
Issues: let's consider log-linear policies.

- **Approximation error:** For log linear policies, how good does ϕ need to be?
(comment: hopefully some average case condition for approximating $A^{\pi}(s, a)$)
- **Sample size:** hope to use a # samples that is poly in $\dim(\phi)$ & $1/\epsilon_{accuracy}$.
- **Coverage:** need some coverage condition over the state space.
(comment: hopefully the coverage conditions are only in “ ϕ -space”)
- **Computation:** we want NPG to find something good with poly in $d, 1/\epsilon_{accuracy}, H$ iterations.
- **Theory:** (see AJKS Ch 4+13, for formal log linear policies)
There are (somewhat subtle) approx/coverage conditions where NPG converges to an $\epsilon_{accuracy}$ -opt policy with poly sample, poly computation time.
(Conditions are weaker than those for fitted-DP methods).

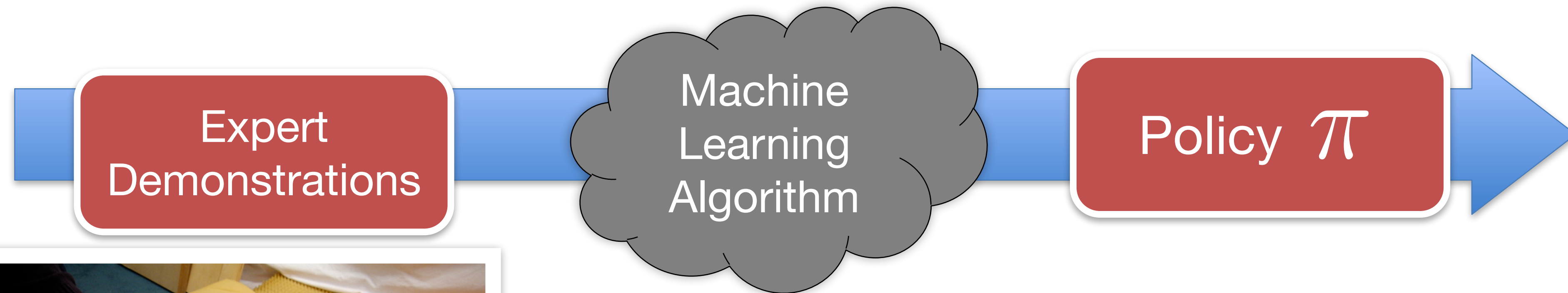
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Imitation Learning



Imitation Learning



- SVM
- Gaussian Process
- Kernel Estimator
- Deep Networks
- Random Forests
- LWR
- ...

Maps *states* to actions

Learning to Drive by Imitation

[Pomerleau89, Saxena05, Ross11a]

Input:



Camera Image



Output:

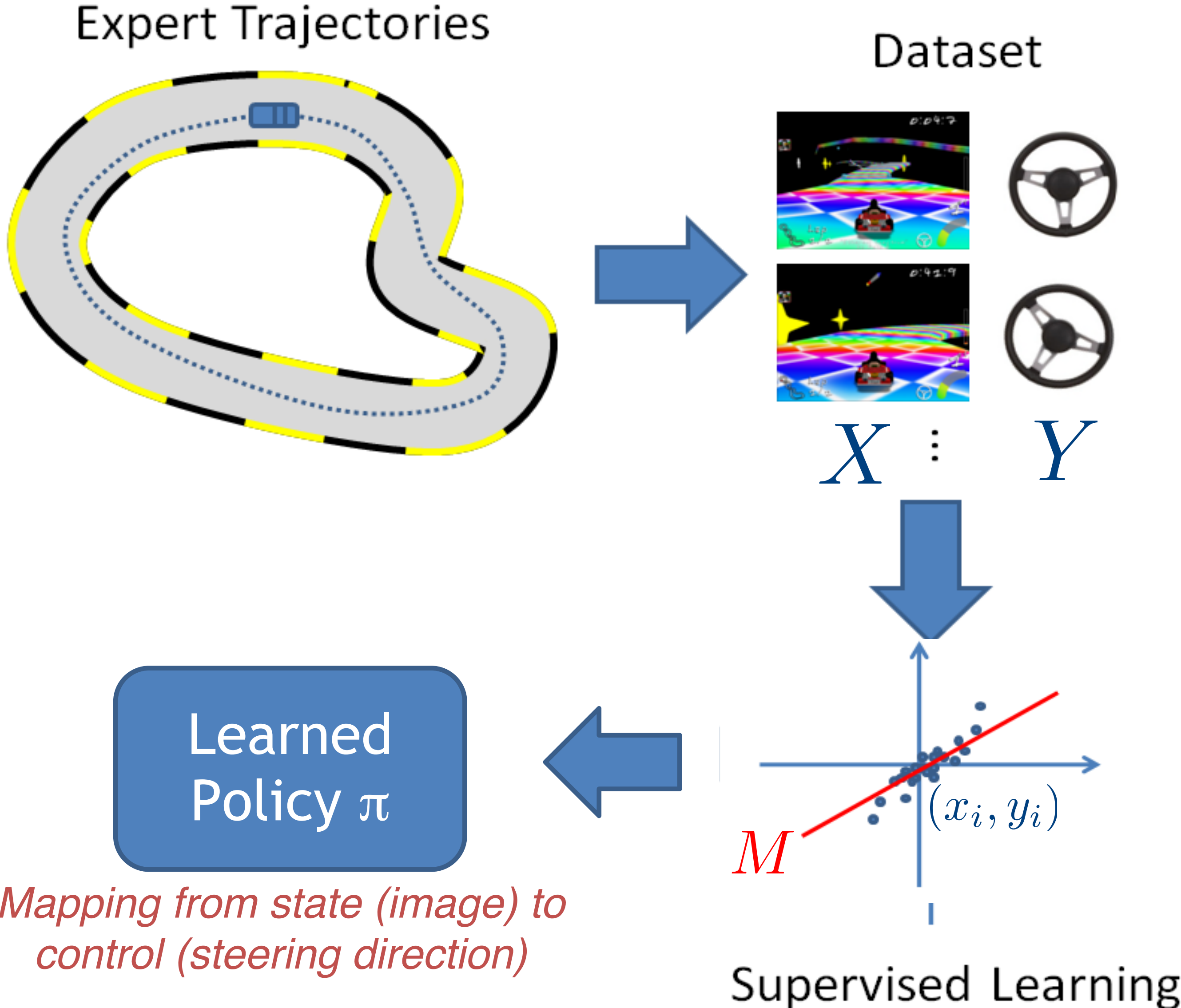


Steering Angle
in $[-1, 1]$

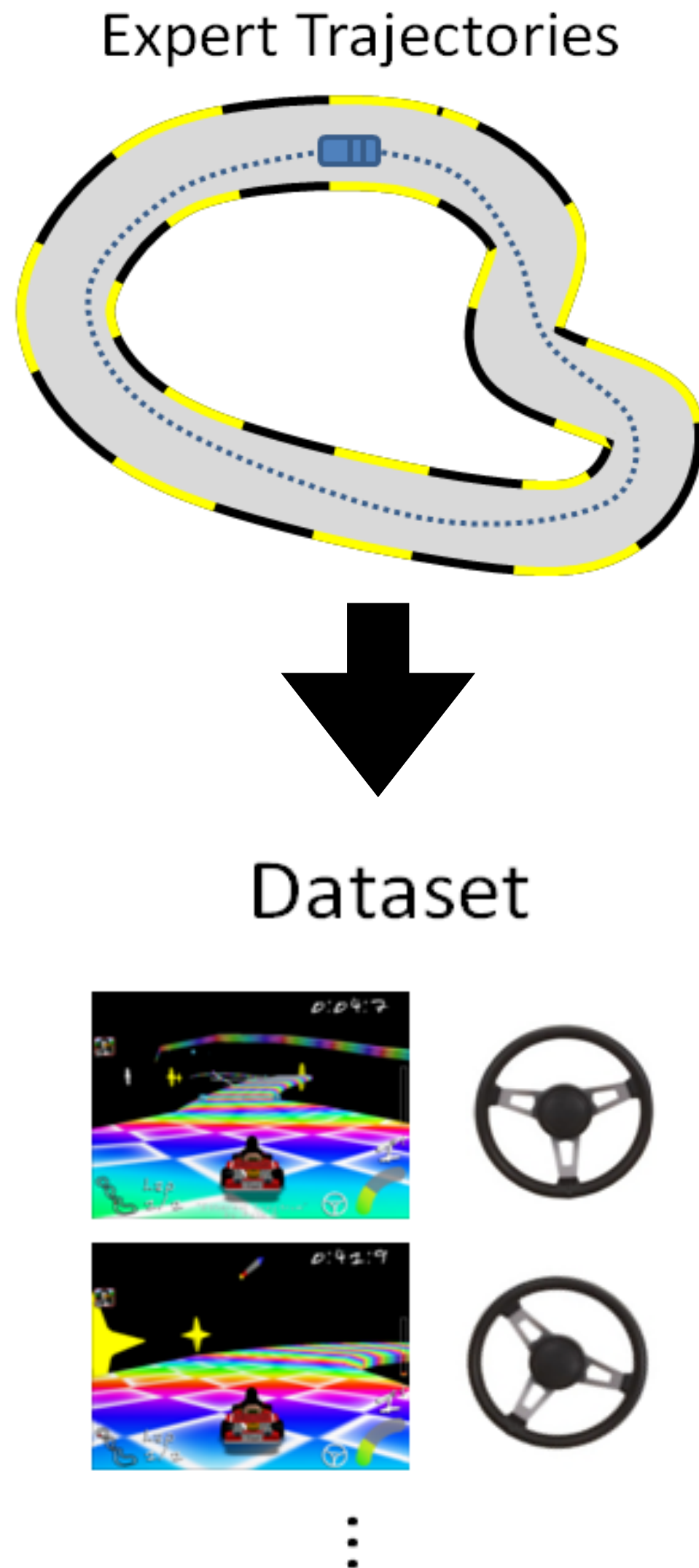
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Supervised Learning Approach: Behavior Cloning



Let's formalize the offline IL Setting and the Behavior Cloning algorithm



Finite horizon MDP \mathcal{M}

Ground truth reward $r(s, a) \in [0, 1]$ is unknown;
Assume the expert has a good policy π^* (not necessarily opt)

We have a dataset of M trajectories: $\mathcal{D} = \{\tau_1, \dots, \tau_M\}$,
where $\tau_i = (s_h^i, a_h^i)_{h=0}^{H-1} \sim \rho_{\pi^*}$

Goal: learn a policy from \mathcal{D} that is as good as the expert π^*

Let's formalize the Behavior Cloning algorithm

BC Algorithm input: a restricted policy class $\Pi = \{\pi : S \mapsto \Delta(A)\}$

BC is a Reduction to Supervised Learning:

$$\hat{\pi} = \arg \min_{\pi \in \Pi} \sum_{i=1}^M \sum_{h=0}^{H-1} \ell(\pi, s_h^i, a_h^i)$$

Many choices of loss functions:

1. Negative log-likelihood (NLL): $\ell(\pi, s, a) = -\ln \pi(a | s)$
2. square loss (i.e., regression for continuous action): $\ell(\pi, s, a) = \|\pi(s) - a\|_2^2$

Theorem: IL is (almost) as easy as SL

$$\hat{\pi} = \arg \min_{\pi \in \Pi} \sum_{i=1}^M \sum_{h=0}^{H-1} \ell(\pi, s_h^i, a_h^i)$$

Note a training and testing “mismatch”

Theorem [BC Performance]:

suppose we assume supervised learning succeeds, with ϵ classification error:

$$\mathbb{E}_{\tau \sim \rho_{\pi_{\pi^*}}} \left[\frac{1}{H} \sum_{h=0}^{H-1} \mathbf{1} [\hat{\pi}(s_h) \neq \pi^*(s_h)] \right] \leq \epsilon,$$

(where π^* is the experts policy, which need not be optimal)

then, under μ , we have:

$$|V^{\pi^*} - V^{\hat{\pi}}| \leq H^2 \epsilon$$

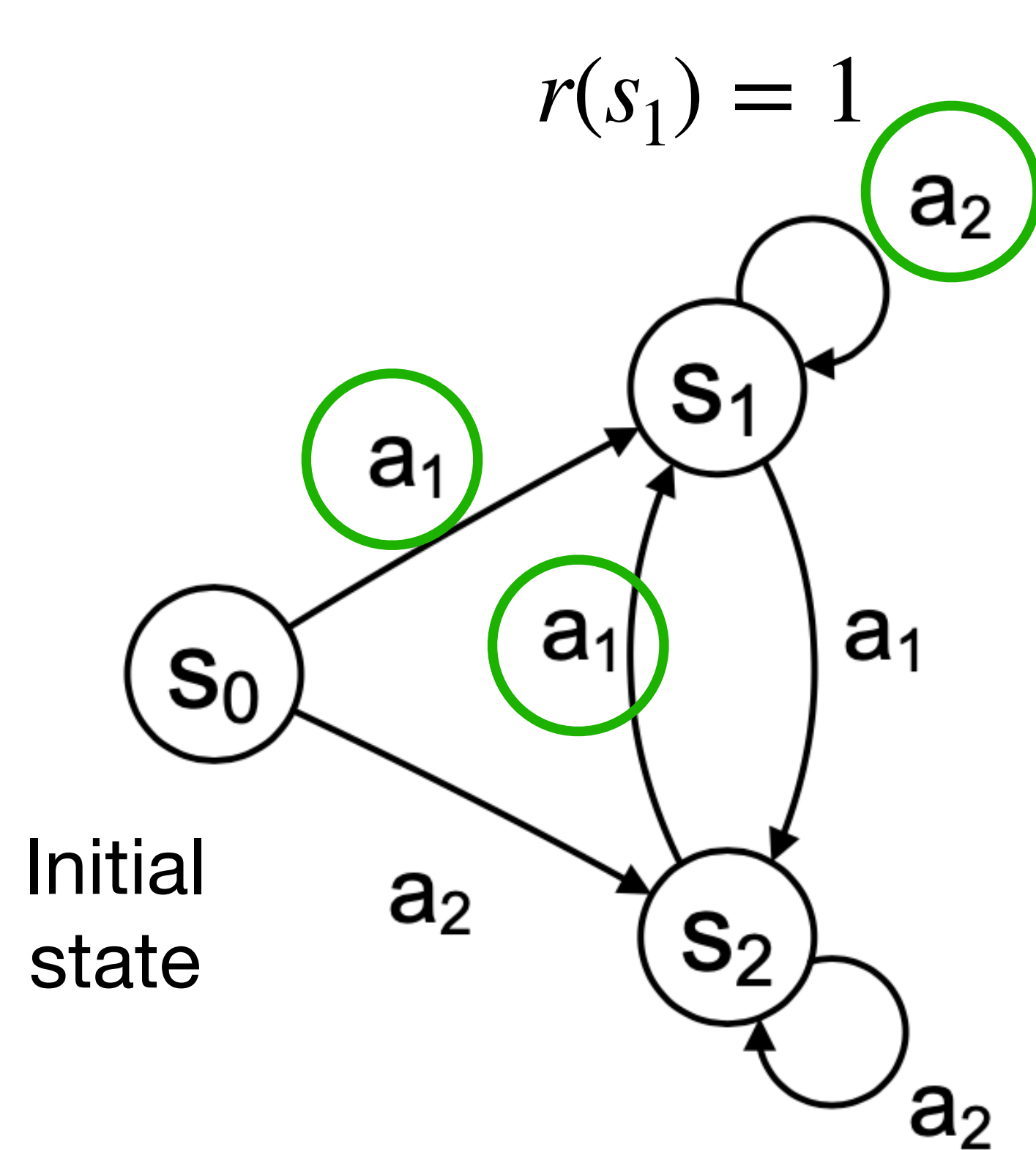
The quadratic amplification is annoying

Proof:

By the PDL

$$\begin{aligned} |V^{\pi^*}(s) - V^{\hat{\pi}}(s)| &= \left| \mathbb{E}_{\tau \sim \rho_{\pi^*}} \left[\sum_{h=0}^{H-1} A_h^{\hat{\pi}}(s_h, a_h) \right] \right| \\ &= \left| \mathbb{E}_{s_1, \dots, s_H \sim \rho_{\pi^*}} \left[\sum_{h=0}^{H-1} A_h^{\hat{\pi}}(s_h, \pi^*(s_h)) \right] \right| \\ &\leq H \left| \mathbb{E}_{\tau \sim \rho_{\pi^*}} \left[\sum_{h=0}^{H-1} \mathbf{1} \left[\hat{\pi}(s_h) \neq \pi^*(s_h) \right] \right] \right| \\ &\leq H^2 \epsilon \end{aligned}$$

Distribution Shift Example (H^2 factor is tight)



Assume SL returns the policy $\hat{\pi}$:

$$\hat{\pi}(s_0) = \begin{cases} a_1 & \text{w/ prob } 1 - H\epsilon \\ a_2 & \text{w/ prob } H\epsilon \end{cases}, \quad \hat{\pi}(s_1) = a_2, \hat{\pi}(s_2) = a_2$$

This policy has good supervised learning error:

$$\mathbb{E}_{\tau \sim \rho_{\pi^*}} \left[\frac{1}{H} \sum_{h=0}^{H-1} \mathbf{1} [\hat{\pi}(s_h) \neq \pi^*(s_h)] \right] = \epsilon$$

note: while $\hat{\pi}(s_2) \neq \pi^*(s_2)$, state s_2 is never visited under π^*

We have **quadratic degradation** (in H):

$$V_H^{\pi^*}(s_0) = (1 - H\epsilon) \cdot V_H^{\pi^*}(s_0) + H\epsilon \cdot 0 = V_H^{\pi^*}(s_0) - \epsilon H(H - 1)$$

Intuition: once we make a mistake at s_0 , we end up in s_2 which is not in the training data!

Opt policy:

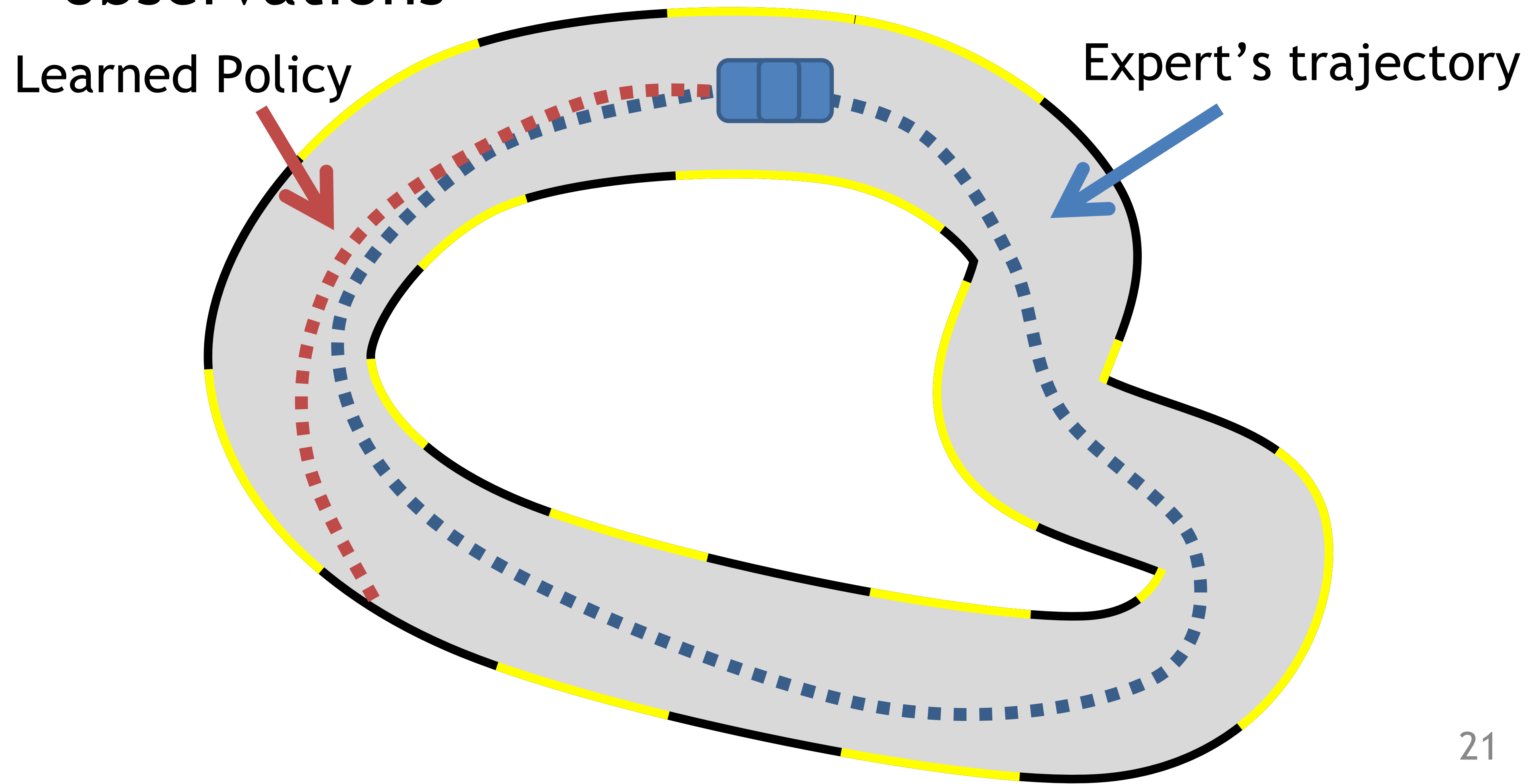
Under ρ_{π^*} , trajectory is s_0, s_1, s_1, \dots

$$\rho_{\pi^*}(s_h = s_2) = 0$$

$$V_H^{\pi^*}(s_0) = H - 1$$

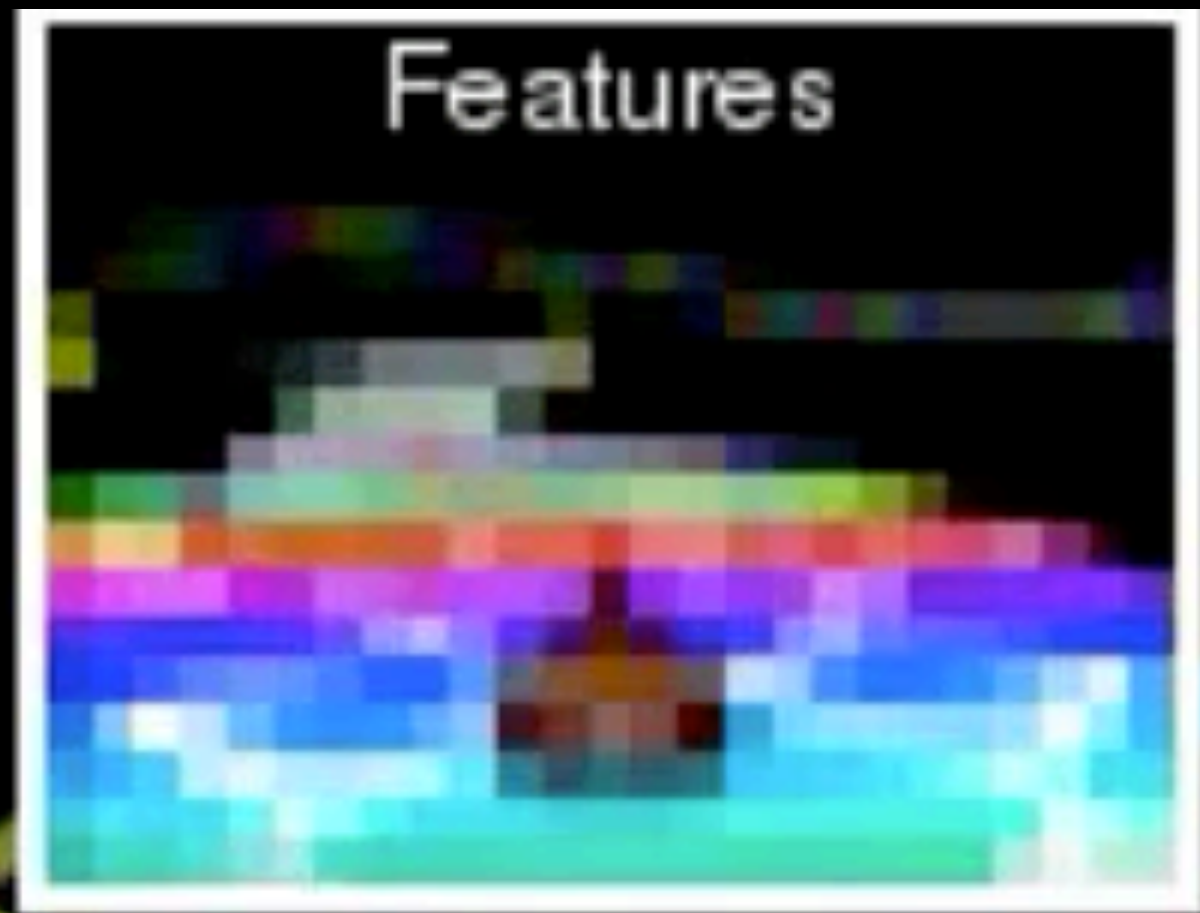
What could go wrong?

- Predictions affect future inputs/ observations



Expert Demos





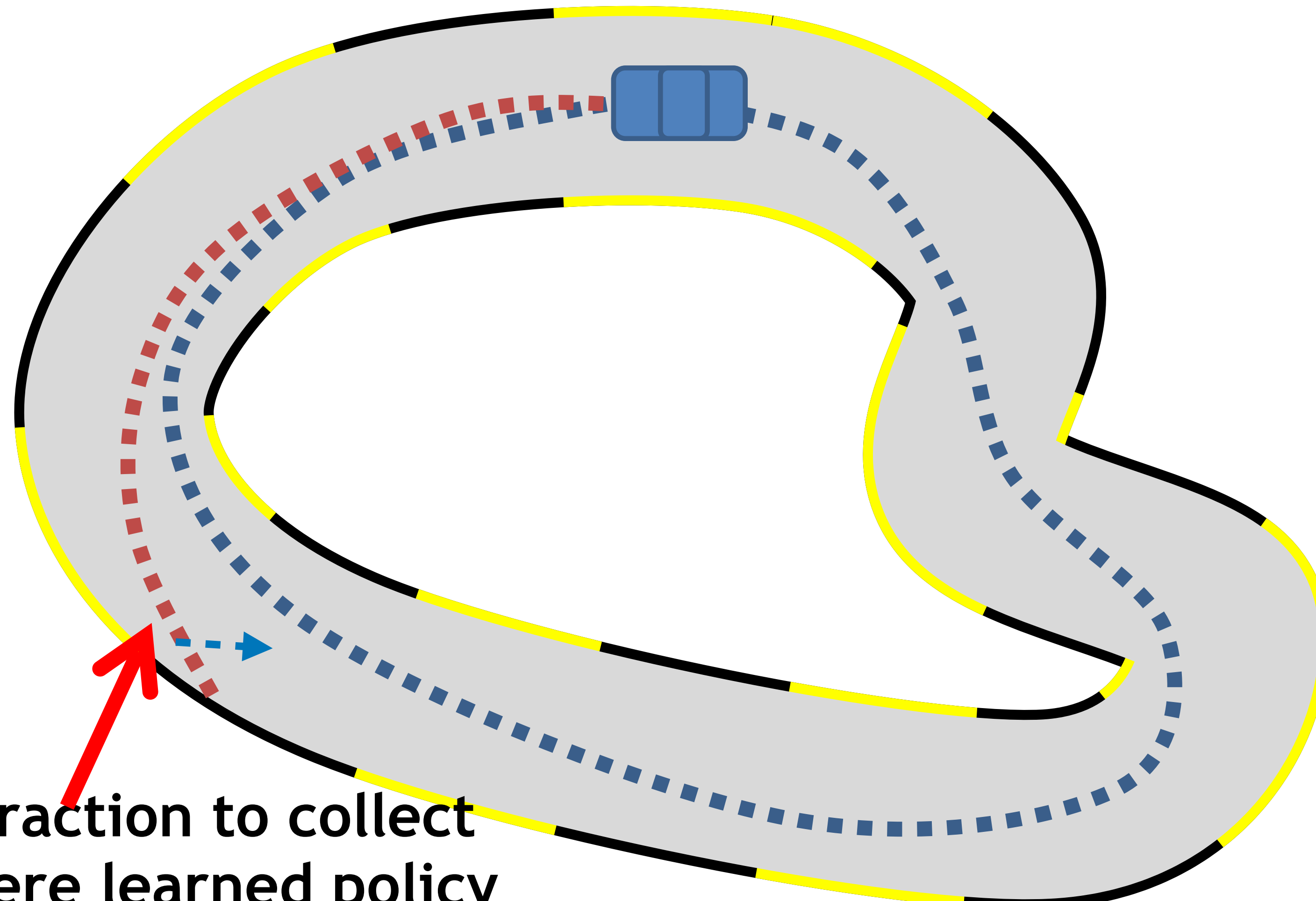
BC Policy

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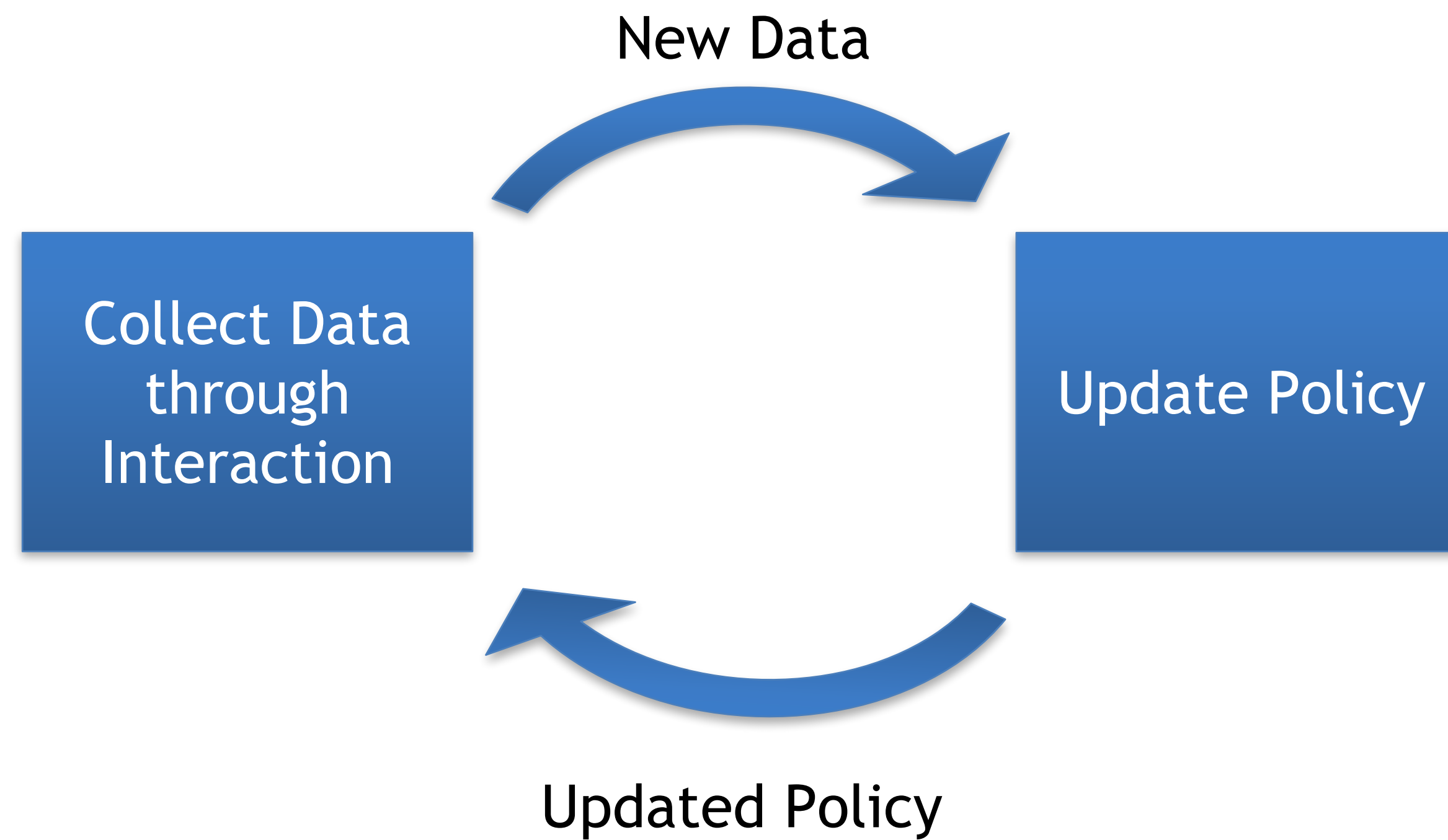
- ✓ • DAgger

Intuitive solution: Interaction



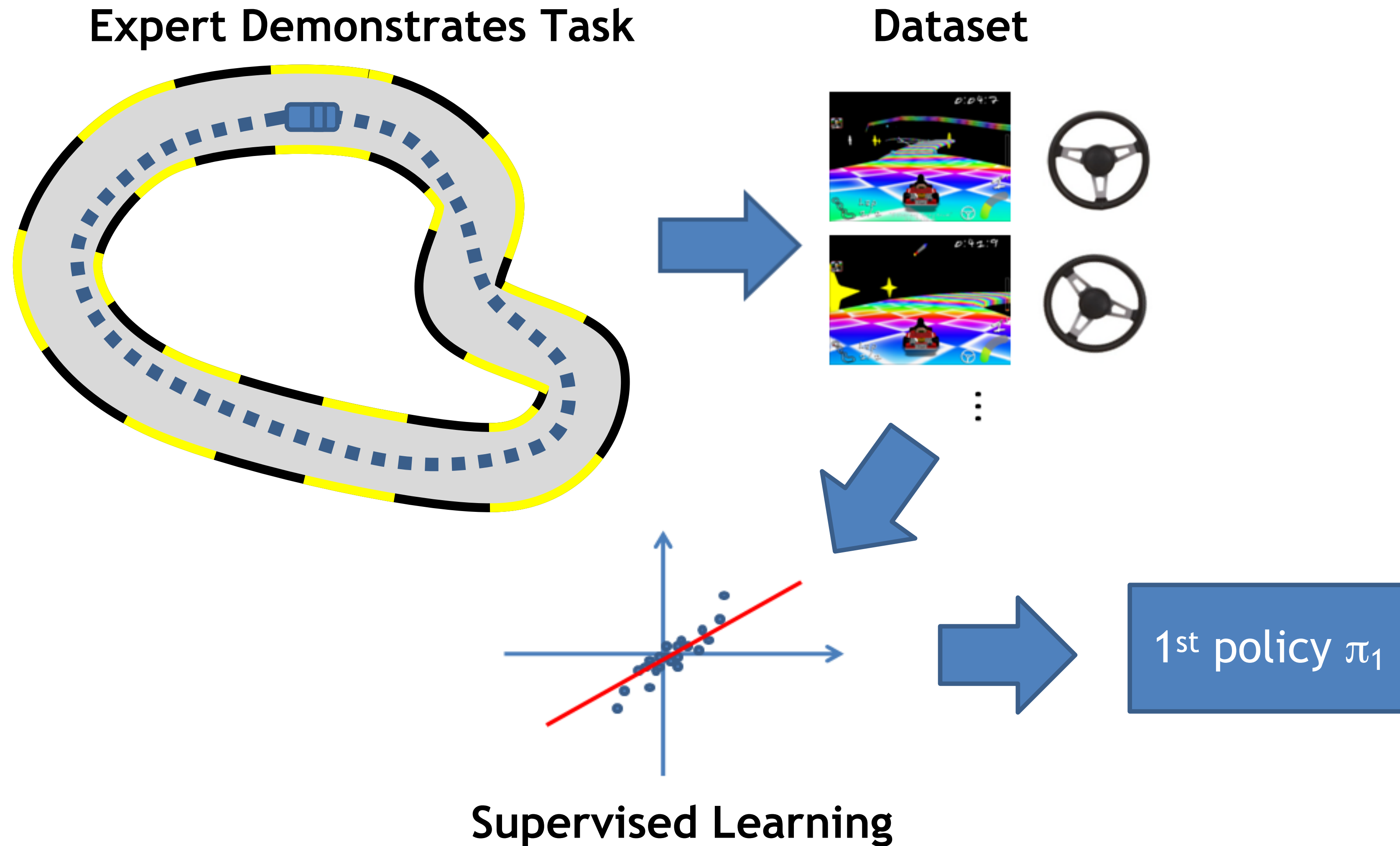
Use interaction to collect data where learned policy goes

General Idea: Iterative Interactive Approach



Dagger: Dataset Aggregation ^[Ross11a]

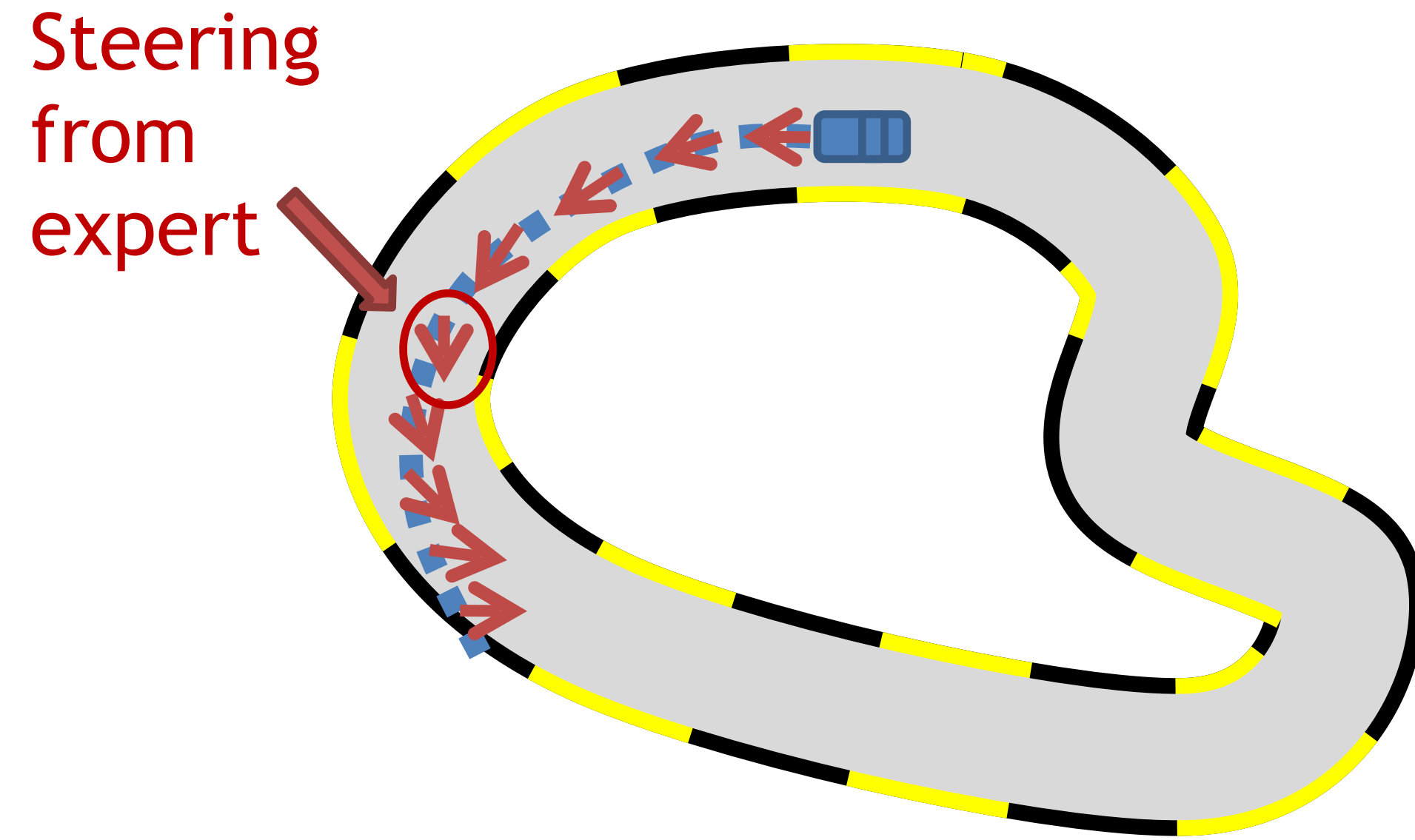
0th iteration



Dagger: Dataset Aggregation ^[Ross11a]

1st iteration

Execute π_1 and Query Expert

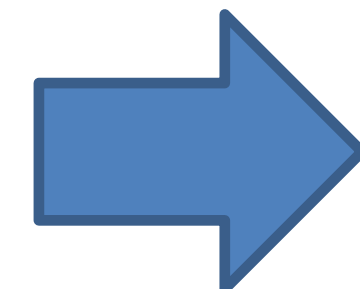
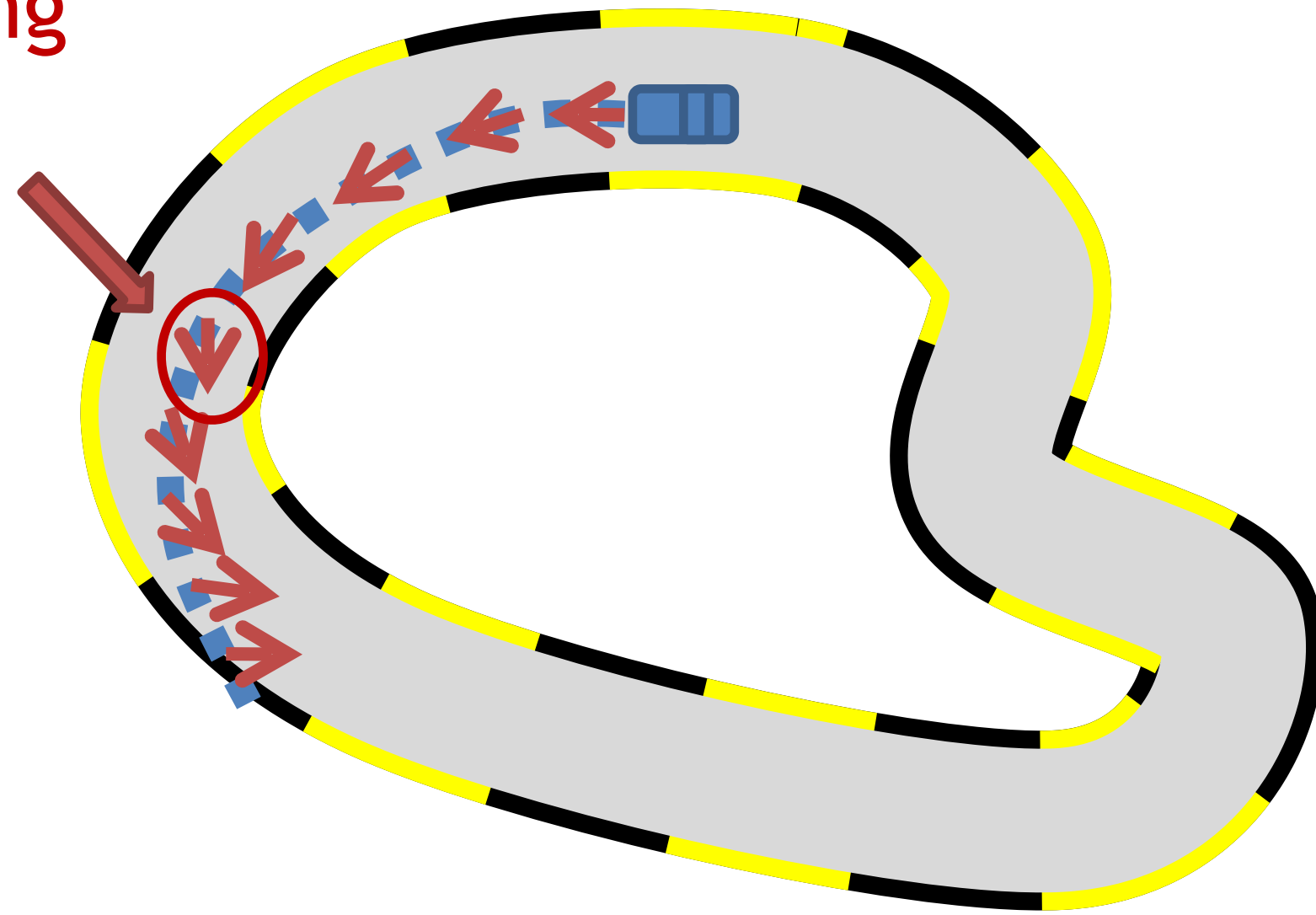


Dagger: Dataset Aggregation ^[Ross11a]

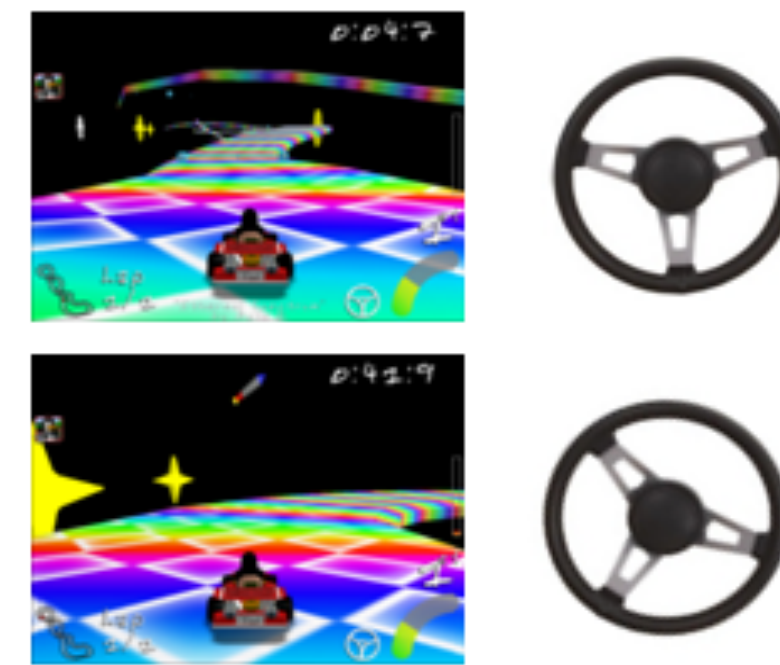
1st iteration

Execute π_1 and Query Expert

Steering
from
expert



New Data



States from
the learned policy

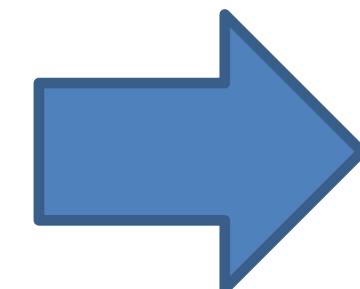
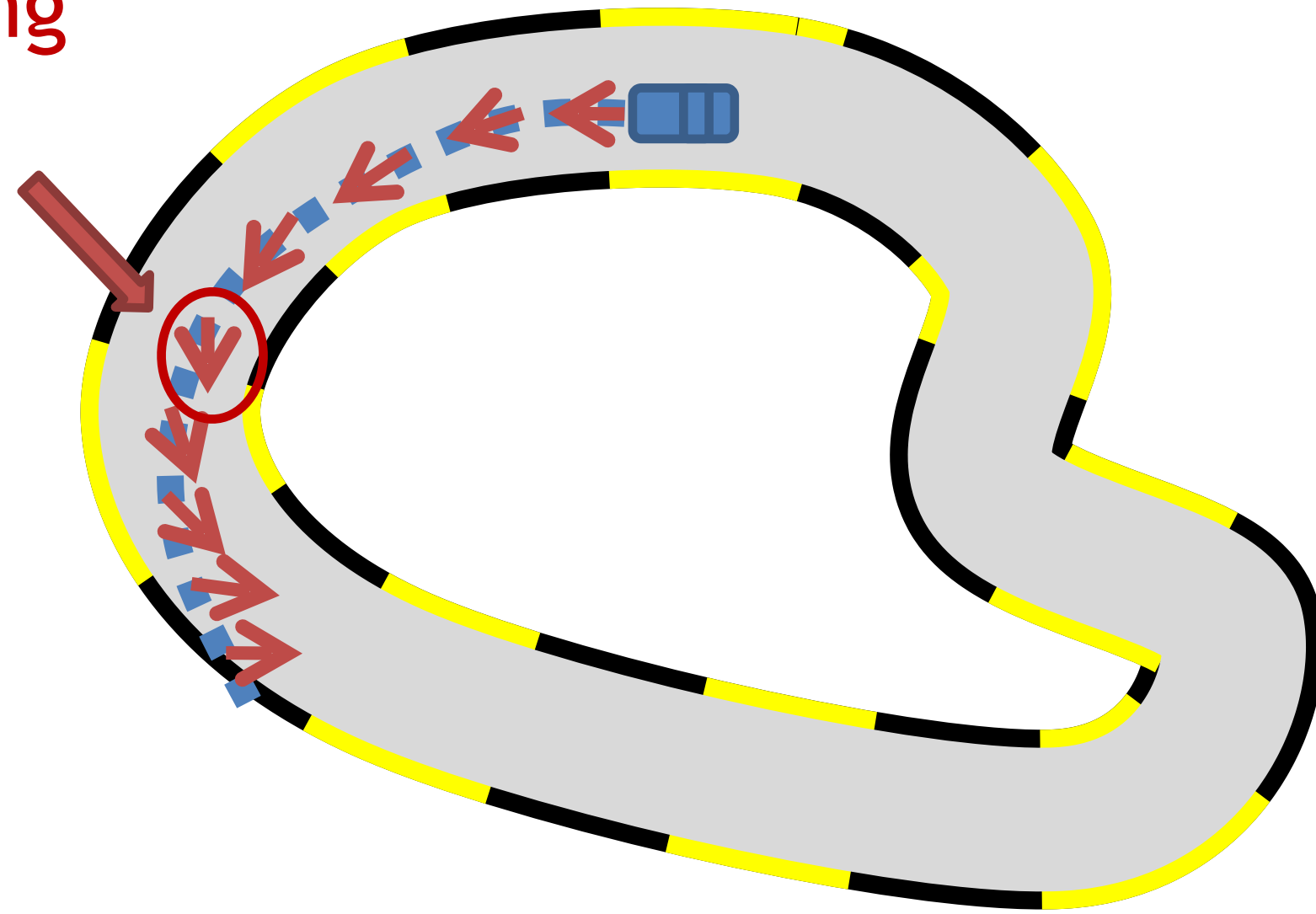


Dagger: Dataset Aggregation ^[Ross11a]

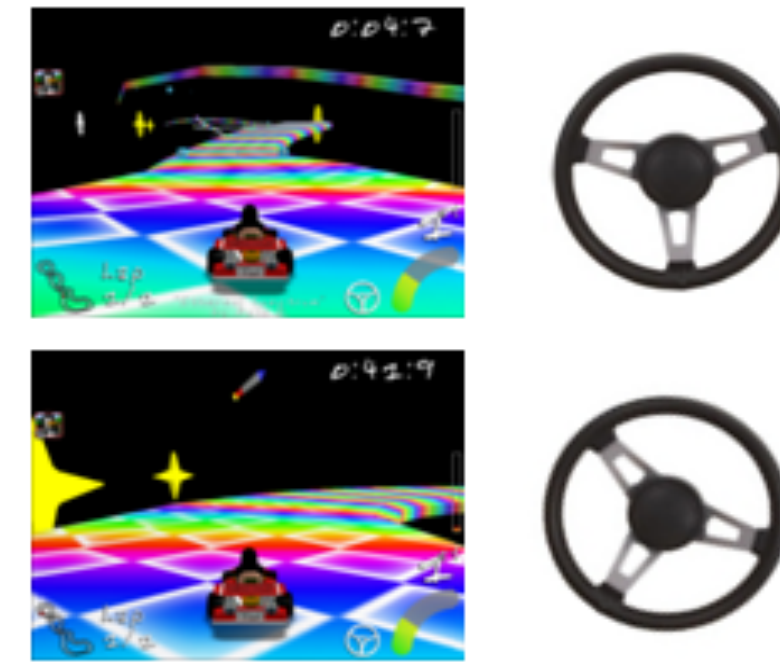
1st iteration

Execute π_1 and Query Expert

Steering
from
expert



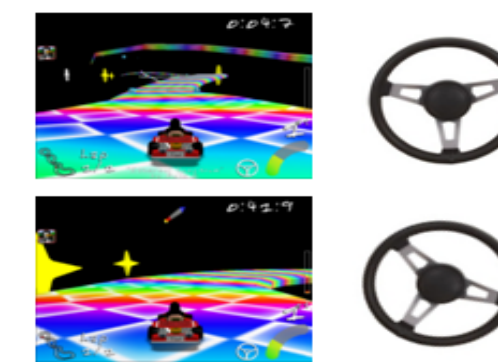
New Data



⋮



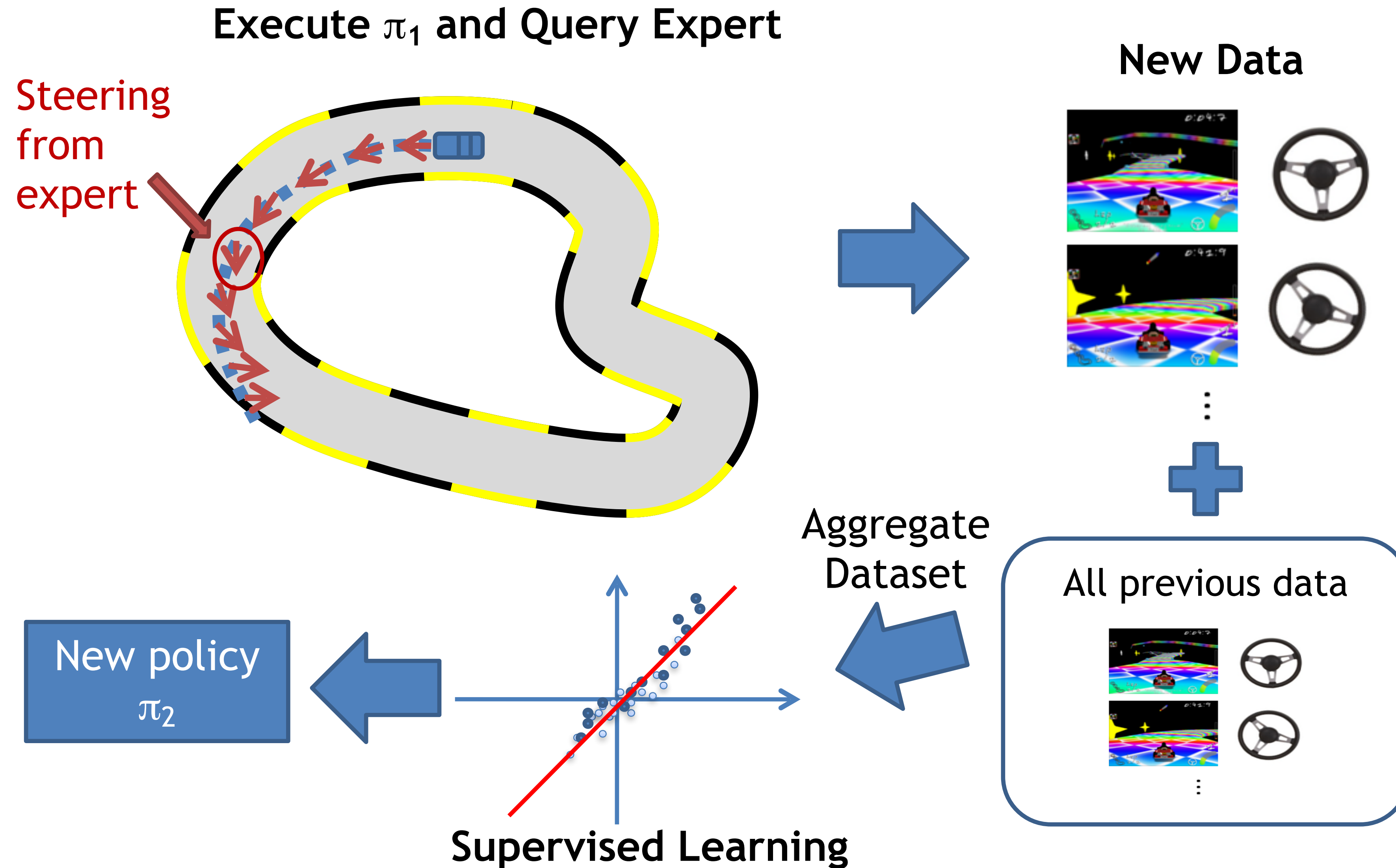
All previous data



⋮

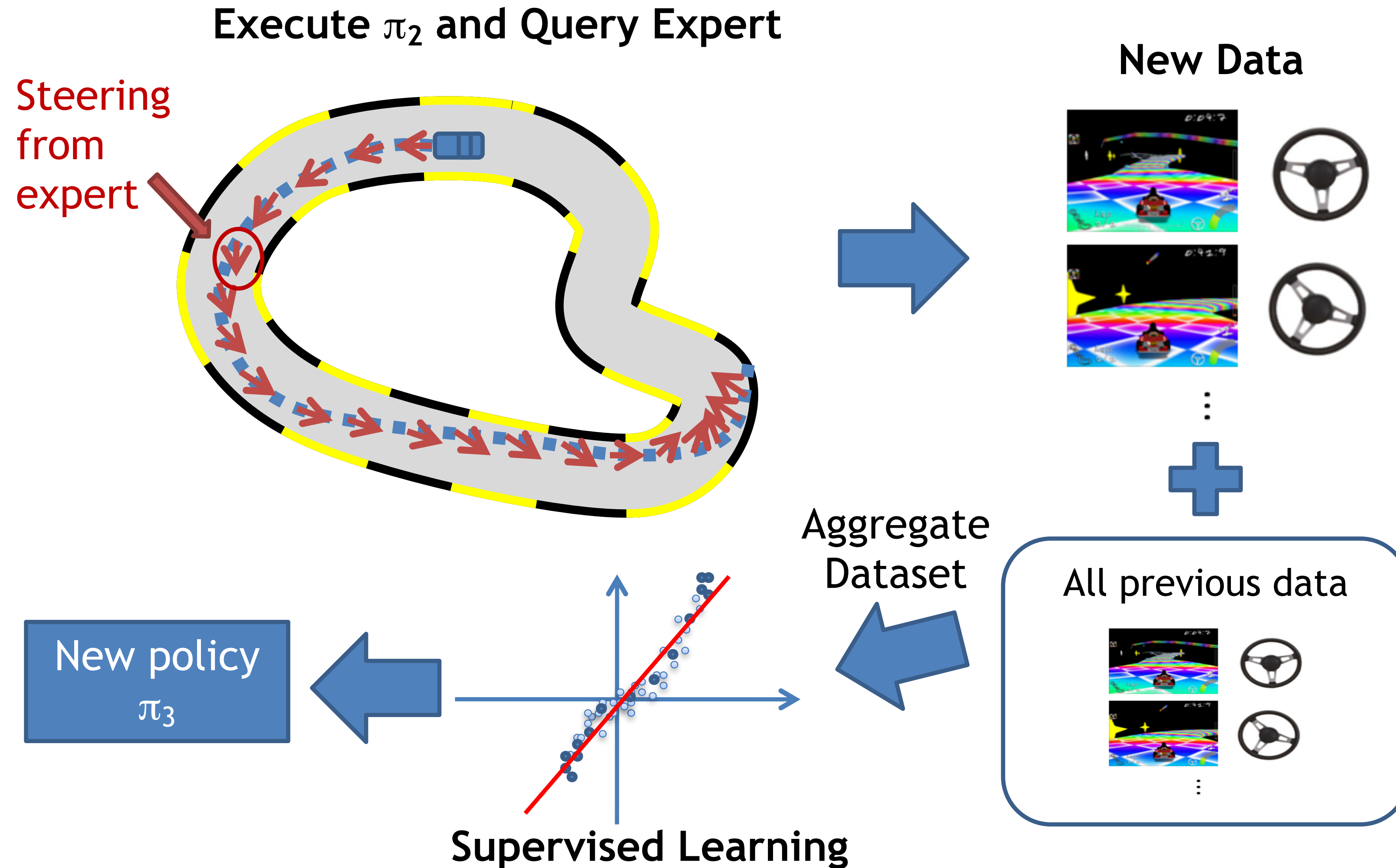
Dagger: Dataset Aggregation [Ross11a]

1st iteration



Dagger: Dataset Aggregation [Ross11a]

2nd iteration

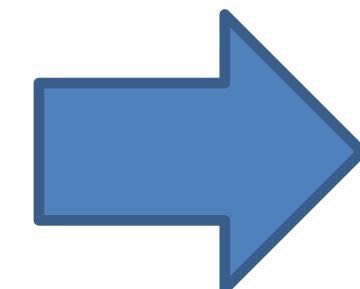
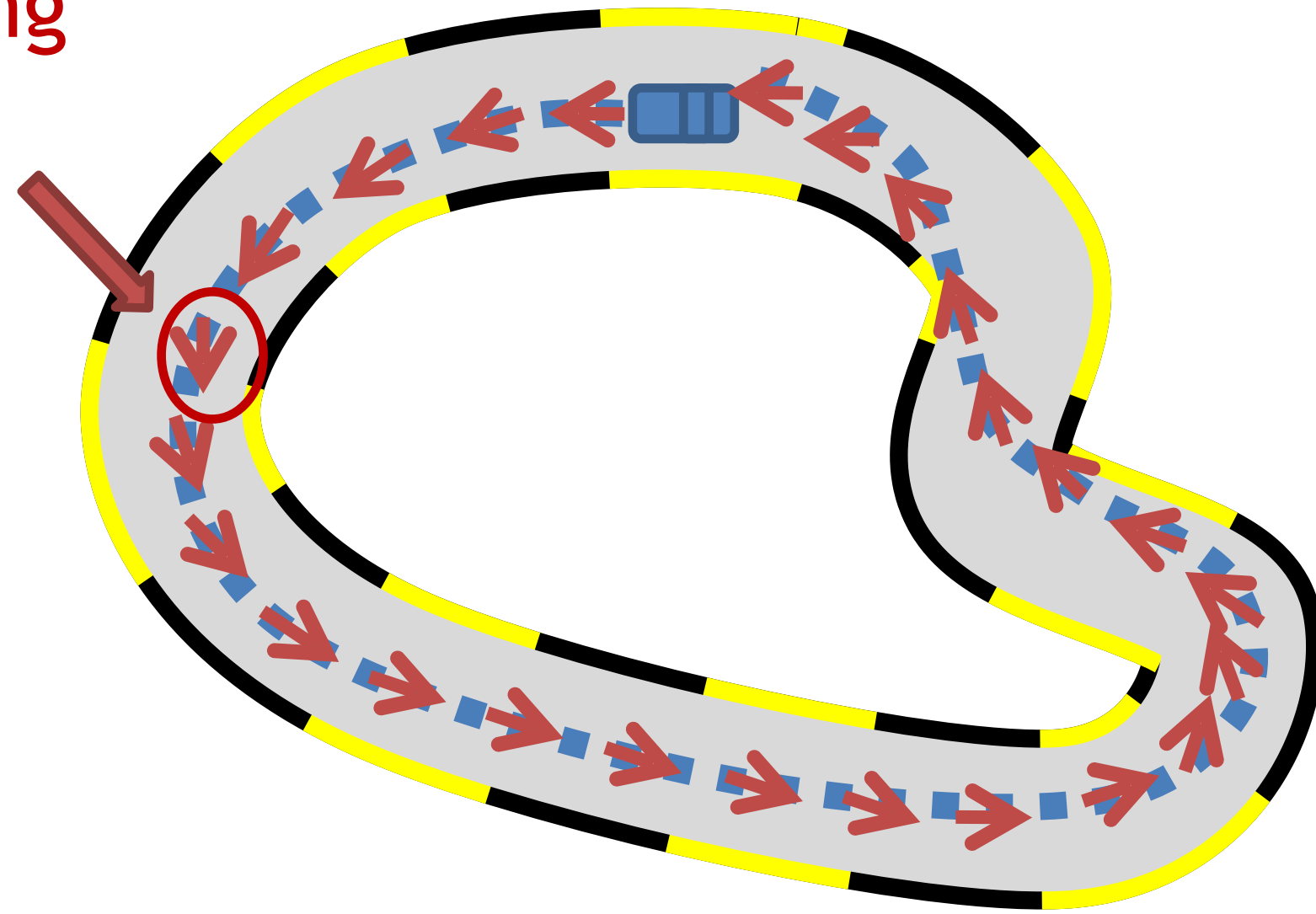


Dagger: Dataset Aggregation [Ross11a]

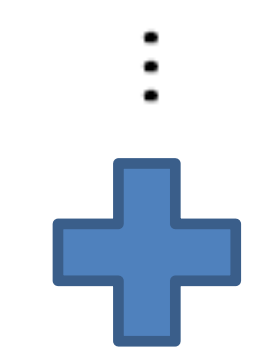
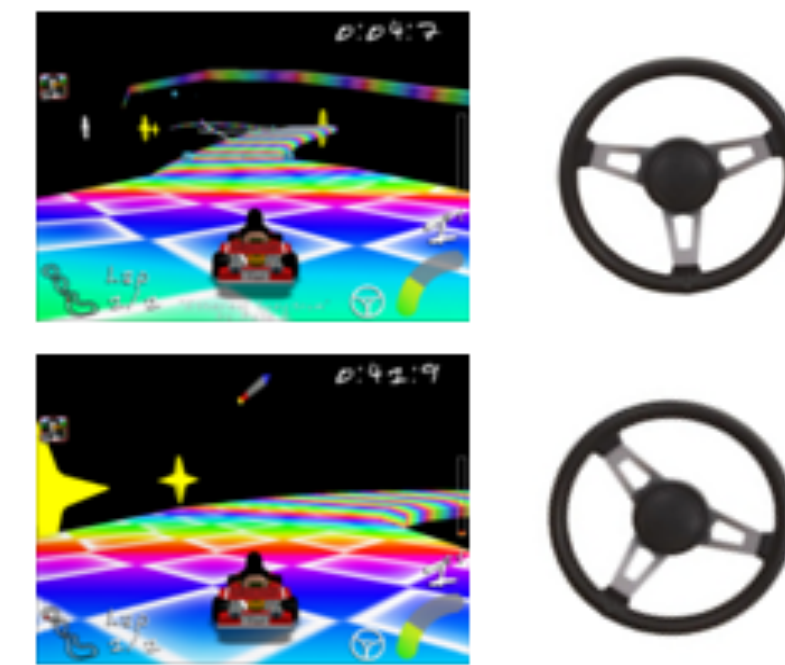
n^{th} iteration

Execute π_{n-1} and Query Expert

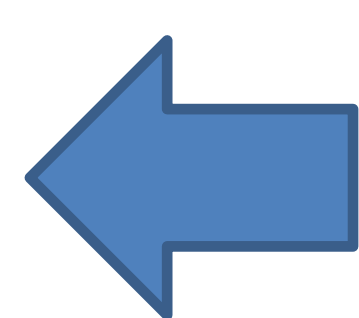
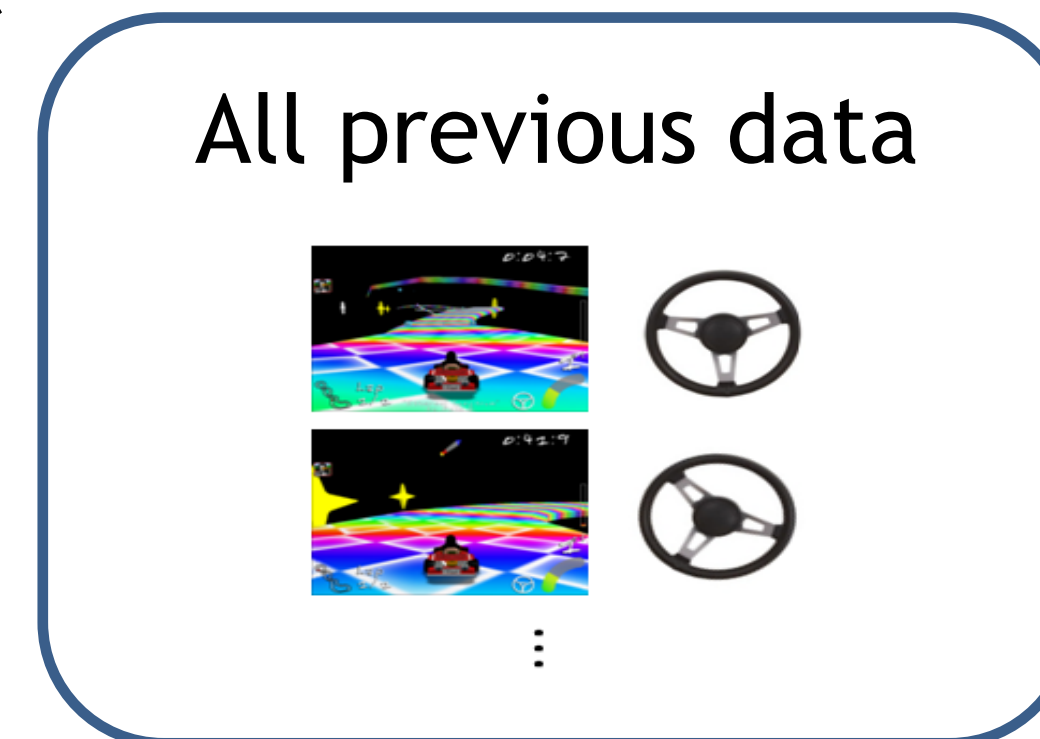
Steering
from
expert



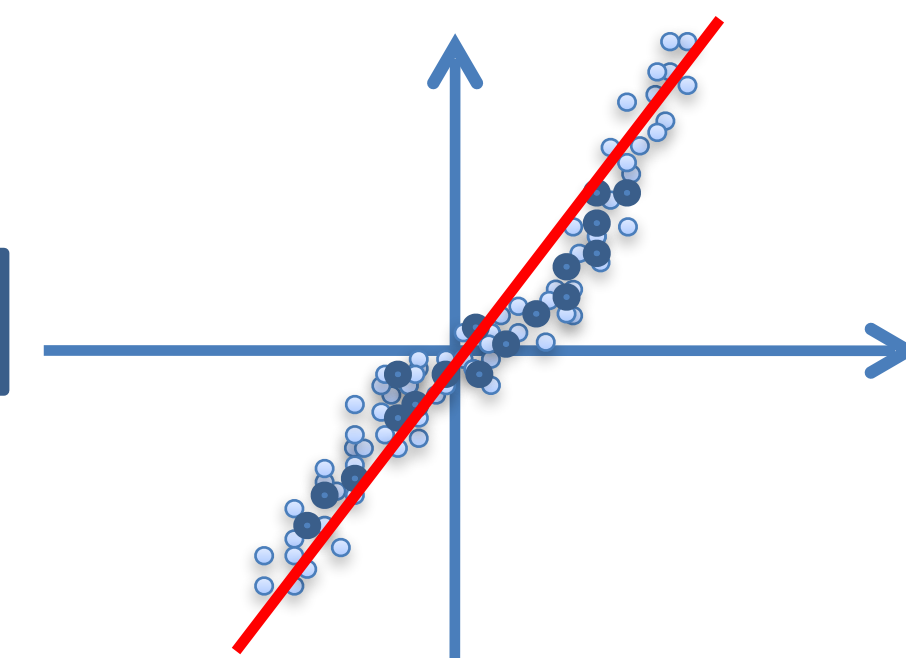
New Data



Aggregate
Dataset



New policy
 π_n



Supervised Learning

The DAgger algorithm

Initialize π^0 , and dataset $\mathcal{D} = \emptyset$

For $t = 0 \rightarrow T - 1$:

1. W/ π^t , generate dataset of trajectories $\mathcal{D}^t = \{\tau_1, \tau_2, \dots\}$

where for all trajectories $s_h \sim \rho_{\pi^t}$, $a_h = \pi^*(s_h)$

2. **Data aggregation:** $\mathcal{D} = \mathcal{D} \cup \mathcal{D}^t$

3. **Update policy via Supervised-Learning:** $\pi^{t+1} = \text{SL}(\mathcal{D})$

In practice, the DAgger algorithm requires less human labeled data than BC.

[\[Informal Theorem\]](#) Under more assumptions + assuming ϵ SL error is achievable, the DAgger algorithm has error: $|V^{\pi^*} - V^{\hat{\pi}}| \leq H\epsilon$

Success!

[Ross AISTATS 2011]



Summary:

1. NPG: a simpler way to do TRPO, a “pre-conditioned” gradient method.
2. PPO: “first order” approx to TRPO

Attendance:

bit.ly/3RcTC9T



Feedback:

bit.ly/3RHtlxy

